# Radial Bright Channel Prior for Single Image Vignetting Correction

#### Supplementary Material

Hojin Cho, Hyunjoon Lee, and Seungyong Lee

POSTECH

#### Relation with the camera response function

- The proposed algorithm does NOT explicitly consider the camera response function (CRF).
  - In Sec.3, our key observation on natural images indicates that the radial bright channel of an image is near horizontal (i.e., near constant intensity).
  - If we apply the inverse of a CRF for each image, then the intensities of the radial bright channel would be mapped to a similar exposure value and our observation still holds in the calibrated image.
  - Thus, we estimate the vignetting curve with just the observed image based on Eq.(1) regardless of the CRF.

#### Synthetic Example: Description

- We tested with various vignetting functions:
  - Genereted using the extended Kang-Weiss model in Eqs.(7)-(9) of the main paper
  - With the three different focal lengths  $f \in \{250, 500, 1300\}$
- Synthetic examples show how much robust our algorithm is for various images and different vignetting effects.
  - We also include quantitative evaluation results (i.e., PSNR).

#### Synthetic Example 1 (f=250)



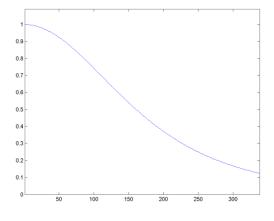


Ground truth I

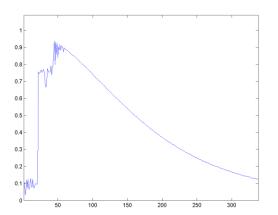
0.9
0.8
0.7
0.6
0.5
0.4
0.3
0.2
0.1
0.0
50
100
150
200
250
300

Radial bright channel IRB

Ground truth *V* 



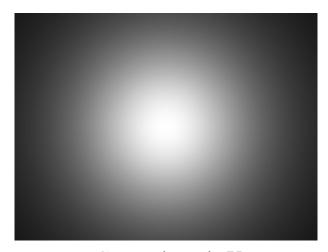
Radial bright channel VRB



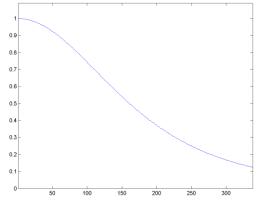
Synthetic input *Z* 

Radial bright channel ZRB 4

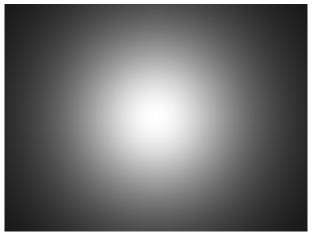
## Synthetic Example 1 (f=250)



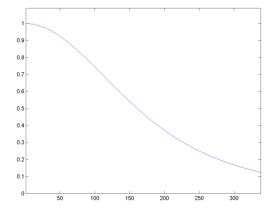
Ground truth V



Radial bright channel VRB



Our result  $V_E$  estimated from Z

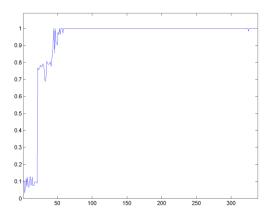


Radial bright channel  $V_E^{RB}$ 

# Synthetic Example 1 (f=250)



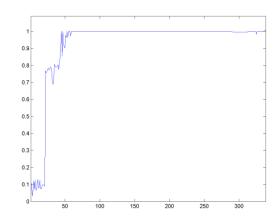
Ground truth I



Radial bright channel IRB



Our result  $I_E$  (PSNR: 58.15)



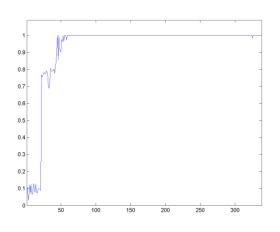
Radial bright channel  $I_E^{RB}$ 

## Synthetic Example 1 (f=500)



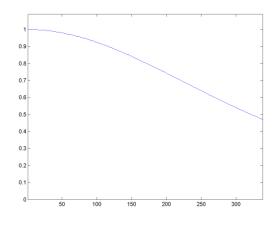


Ground truth I



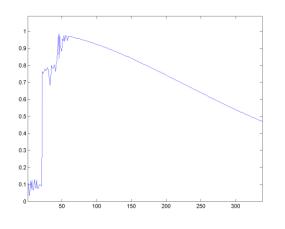
Radial bright channel IRB

Ground truth *V* 



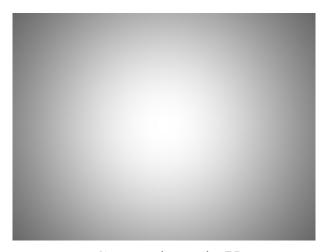
Radial bright channel VRB

Synthetic input Z

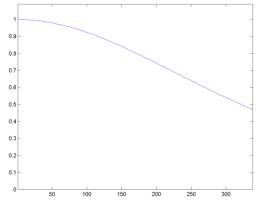


Radial bright channel ZRB 7

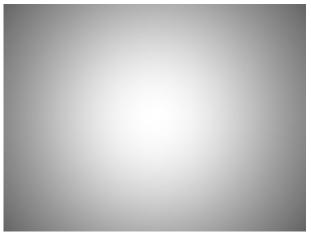
#### Synthetic Example 1 (f=500)



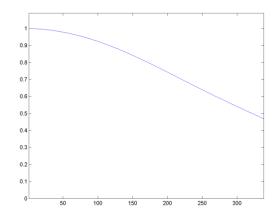
Ground truth V



Radial bright channel VRB



Our result  $V_E$  estimated from Z

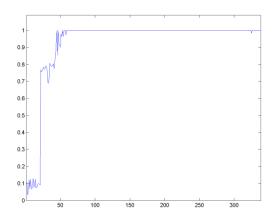


Radial bright channel  $V_E^{RB}$ 

# Synthetic Example 1 (f=500)



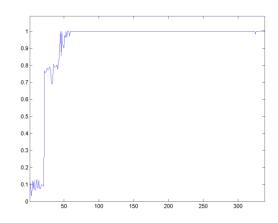
Ground truth I



Radial bright channel IRB



Our result  $I_E$  (PSNR: 57.48)

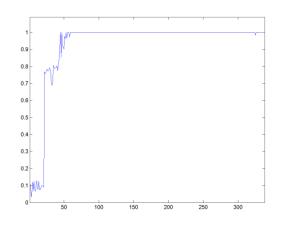


Radial bright channel  $I_E^{RB}$ 

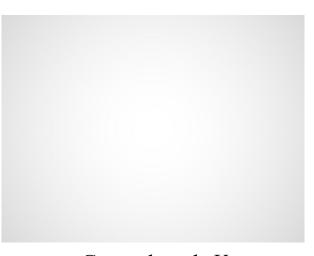
## Synthetic Example 1 (f=1300)



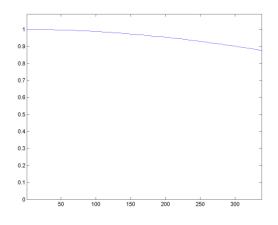
Ground truth *I* 



Radial bright channel IRB



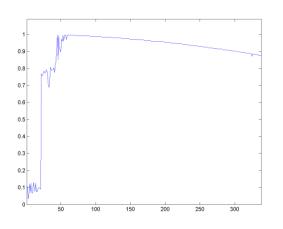
Ground truth V



Radial bright channel VRB

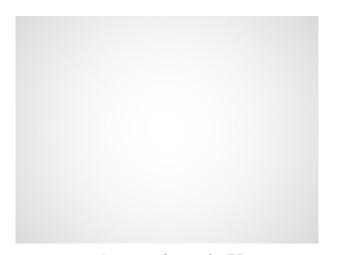


Synthetic input *Z* 

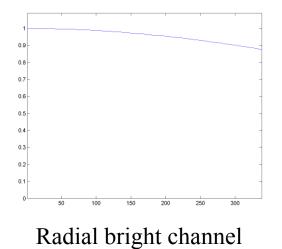


Radial bright channel  $Z^{RB}$  10

# Synthetic Example 1 (f=1300)

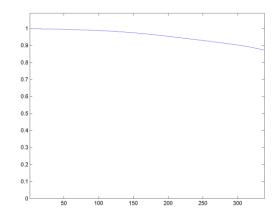


Ground truth V



VRB

Our result  $V_E$  estimated from Z

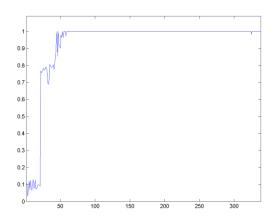


Radial bright channel  $V_F^{RB}$ 

# Synthetic Example 1 (f=1300)



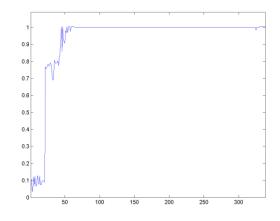
Ground truth I



Radial bright channel IRB



Our result  $I_E$  (PSNR: 56.47)

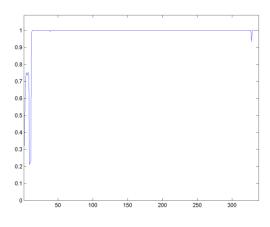


Radial bright channel  $I_E^{RB}$ 

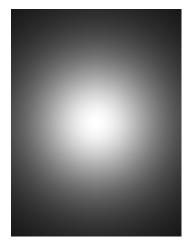
## Synthetic Example 2 (f=250)



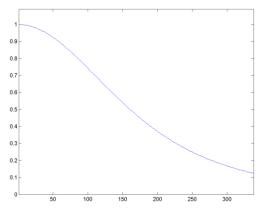
Ground truth I



Radial bright channel IRB



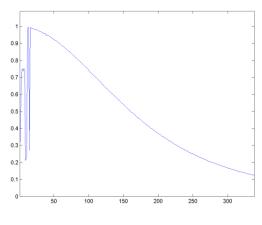
Ground truth *V* 



Radial bright channel VRB



Synthetic input *Z* 

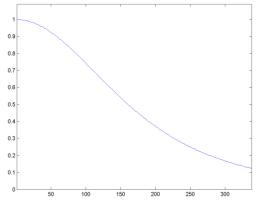


Radial bright channel  $Z^{RB}$  13

## Synthetic Example 2 (f=250)



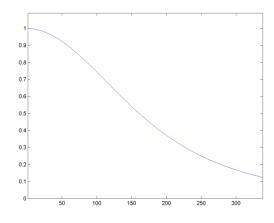
Ground truth V



Radial bright channel <sub>I/RB</sub>



Our result  $V_E$  estimated from Z

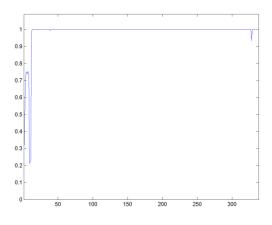


Radial bright channel  $V_F^{RB}$ 

# Synthetic Example 2 (f=250)



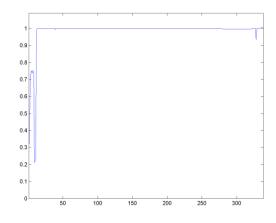
Ground truth I



Radial bright channel IRB



Our result  $I_E$  (PSNR: 53.91)

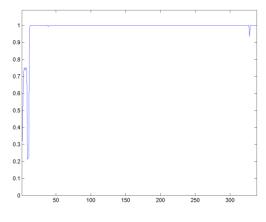


Radial bright channel  $I_F^{RB}$ 

## Synthetic Example 2 (f=500)



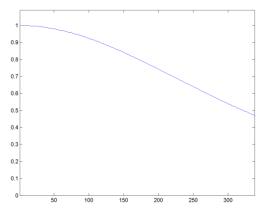
Ground truth I



Radial bright channel IRB



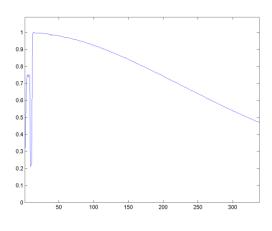
Ground truth V



Radial bright channel VRB

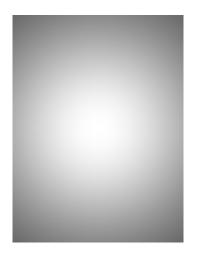


Synthetic input Z

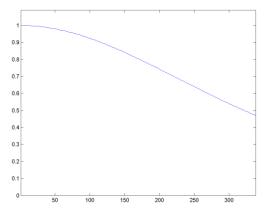


Radial bright channel  $Z^{RB}$  16

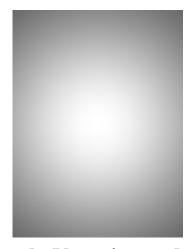
#### Synthetic Example 2 (f=500)



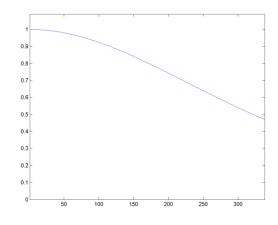
Ground truth V



Radial bright channel <sub>I/RB</sub>



Our result  $V_E$  estimated from Z

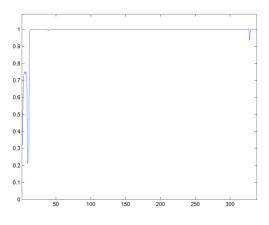


Radial bright channel  $V_E^{\ \mathrm{RB}}$ 

## Synthetic Example 2 (f=500)



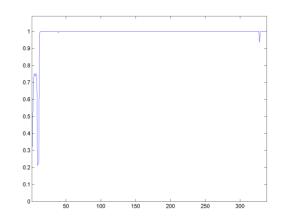
Ground truth I



Radial bright channel IRB



Our result  $I_E$  (PSNR: 80.46)

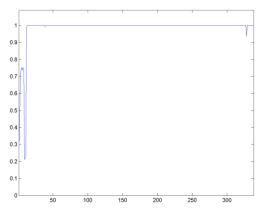


Radial bright channel  $I_E^{RB}$ 

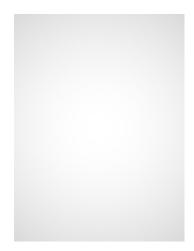
# Synthetic Example 2 (f=1300)



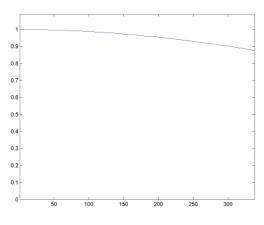
Ground truth I



Radial bright channel IRB



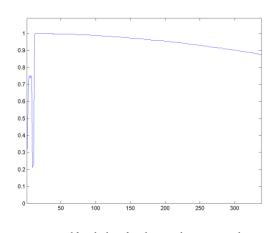
Ground truth V



Radial bright channel VRB



Synthetic input *Z* 

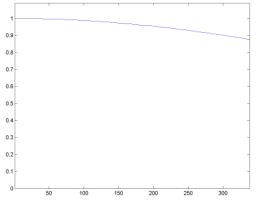


Radial bright channel  $Z^{RB}$  19

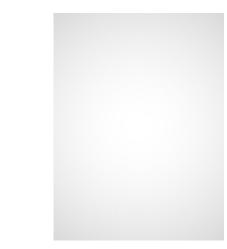
## Synthetic Example 2 (f=1300)



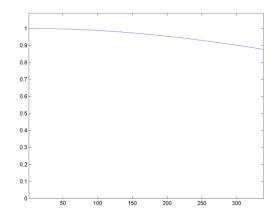
Ground truth V



Radial bright channel VRB



Our result  $V_E$  estimated from Z

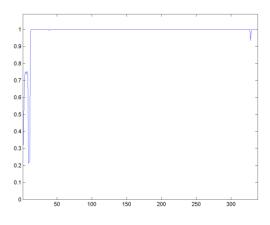


Radial bright channel  $V_F^{RB}$ 

# Synthetic Example 2 (f=1300)



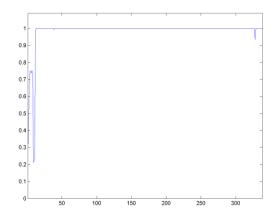
Ground truth I



Radial bright channel IRB

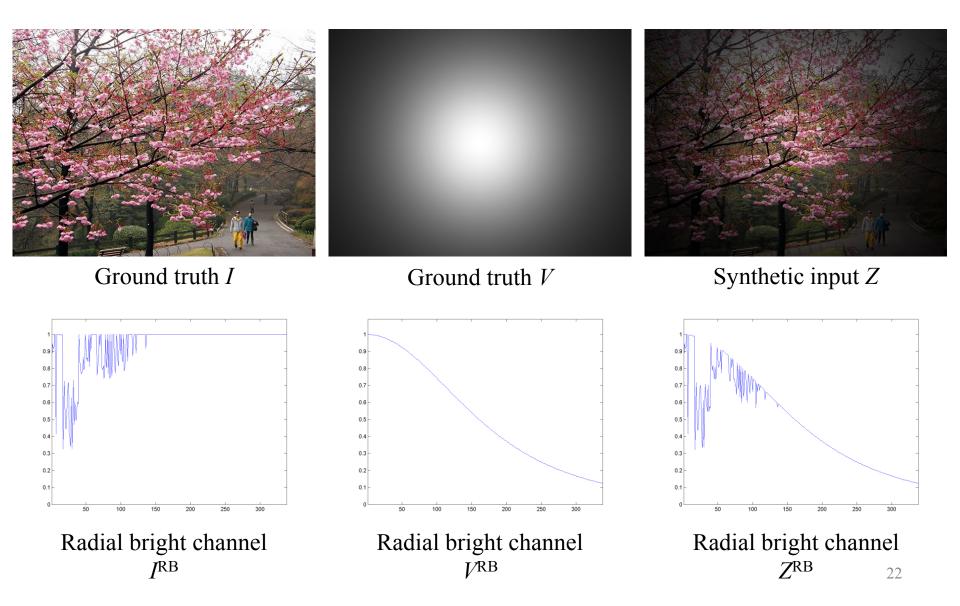


Our result  $I_E$  (PSNR: 90.24)

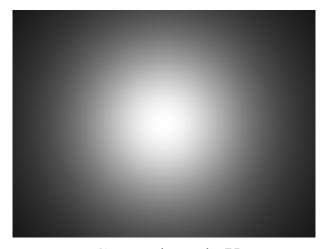


Radial bright channel  $I_F^{RB}$ 

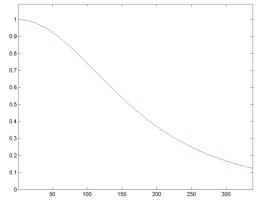
# Synthetic Example 3 (f=250)



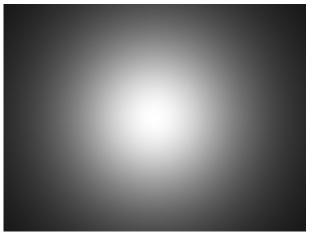
#### Synthetic Example 3 (f=250)



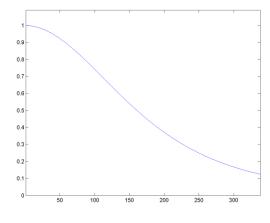
Ground truth V



Radial bright channel VRB



Our result  $V_E$  estimated from Z

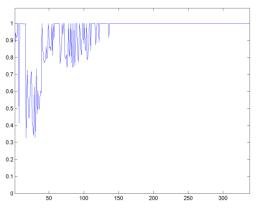


Radial bright channel  $V_E^{\ \mathrm{RB}}$ 

# Synthetic Example 3 (f=250)



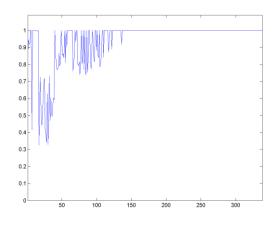
Ground truth I



Radial bright channel IRB

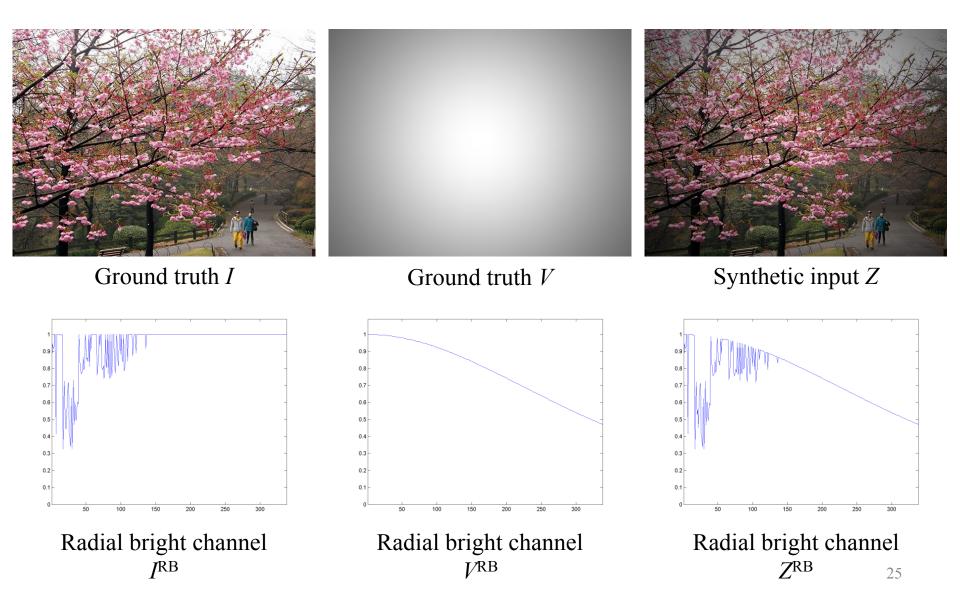


Our result  $I_E$  (PSNR: 71.68)

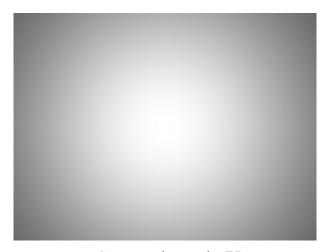


Radial bright channel  $I_E^{RB}$ 

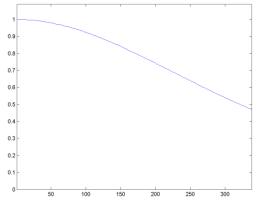
## Synthetic Example 3 (f=500)



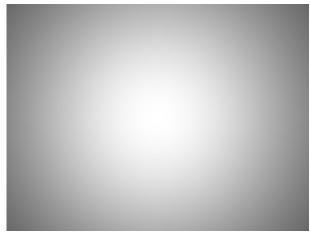
#### Synthetic Example 3 (f=500)



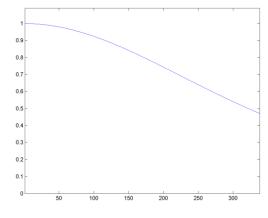
Ground truth V



Radial bright channel VRB



Our result  $V_E$  estimated from Z

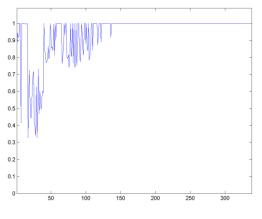


Radial bright channel  $V_F^{RB}$ 

# Synthetic Example 3 (f=500)



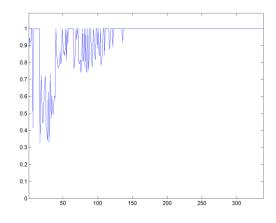
Ground truth I



Radial bright channel IRB

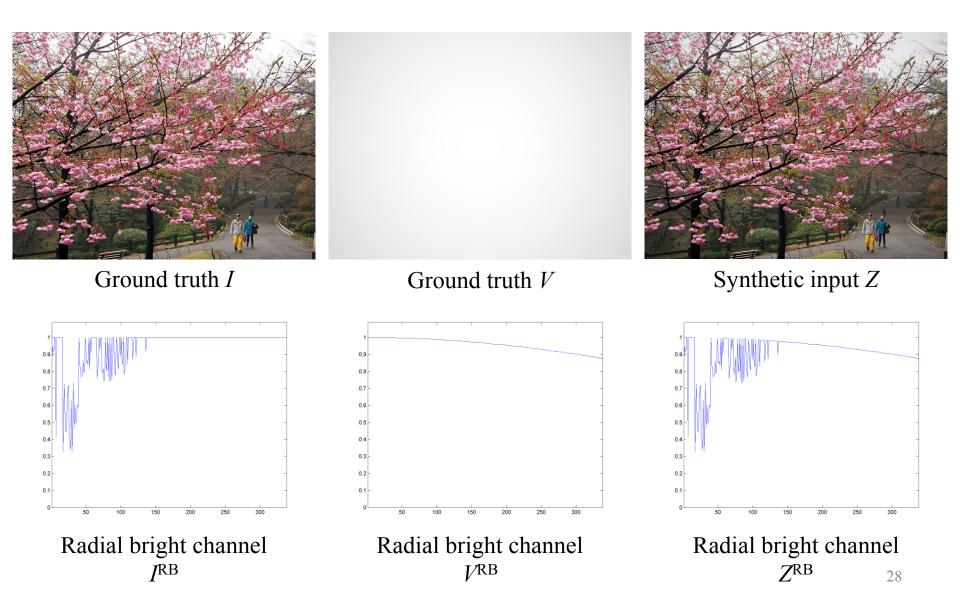


Our result  $I_E$  (PSNR: 76.98)

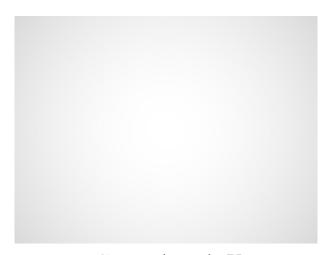


Radial bright channel  $I_F^{RB}$ 

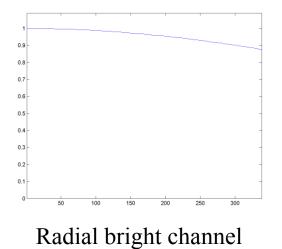
## Synthetic Example 3 (f=1300)



## Synthetic Example 3 (f=1300)

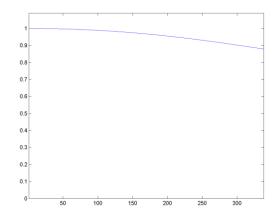


Ground truth V



VRB

Our result  $V_E$  estimated from Z

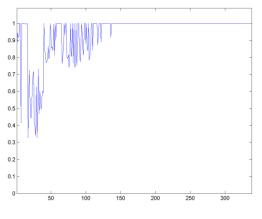


Radial bright channel  $V_F^{RB}$ 

# Synthetic Example 3 (f=1300)



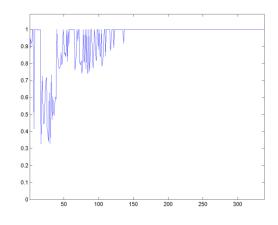
Ground truth I



Radial bright channel IRB



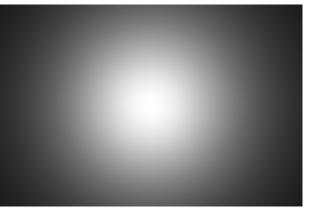
Our result  $I_E$  (PSNR: 65.09)



Radial bright channel  $I_E^{RB}$ 

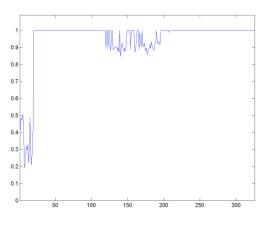
# Synthetic Example 4 (f=250)





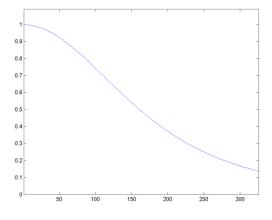


Ground truth I



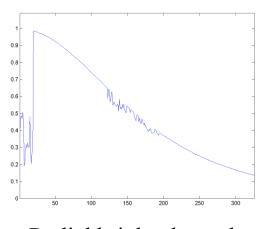
Radial bright channel IRB

Ground truth *V* 



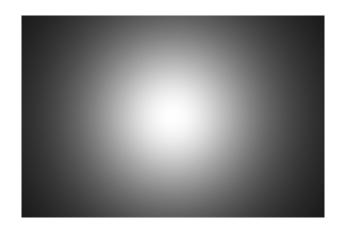
Radial bright channel VRB

Synthetic input Z

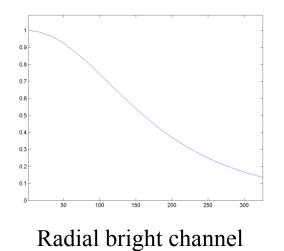


Radial bright channel  $Z^{RB}$  31

#### Synthetic Example 4 (f=250)

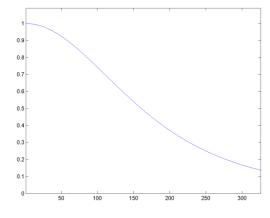


Ground truth V



**V**RB

Our result  $V_E$  estimated from Z

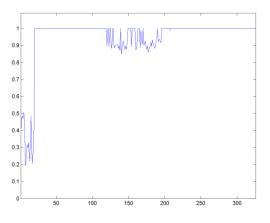


Radial bright channel  $V_F^{RB}$ 

# Synthetic Example 4 (f=250)



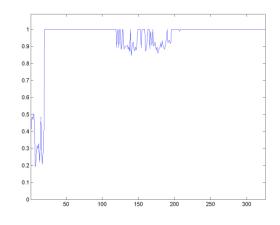
Ground truth I



Radial bright channel IRB



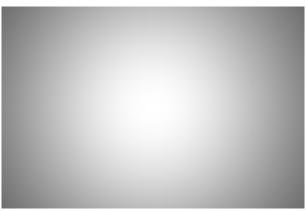
Our result  $I_E$  (PSNR: 70.26)



Radial bright channel  $I_E^{RB}$ 

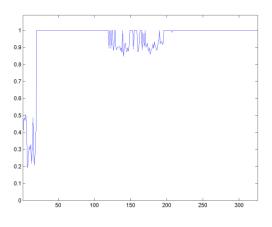
## Synthetic Example 4 (f=500)





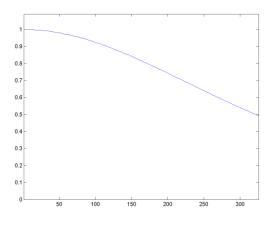


Ground truth I



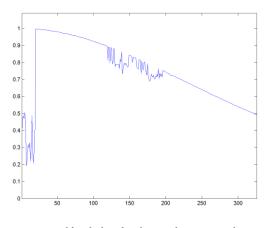
Radial bright channel IRB

Ground truth V



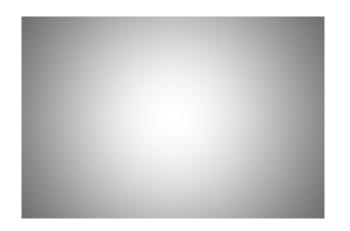
Radial bright channel VRB

Synthetic input Z

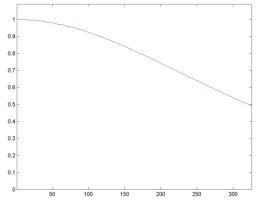


Radial bright channel  $Z^{RB}$  34

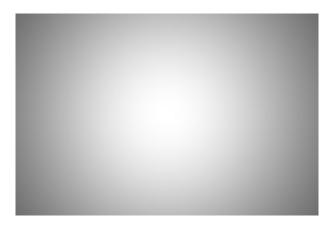
#### Synthetic Example 4 (f=500)



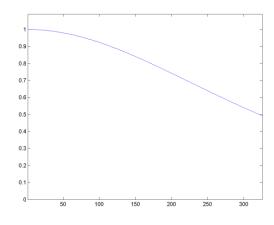
Ground truth V



Radial bright channel VRB



Our result  $V_E$  estimated from Z



Radial bright channel  $V_F^{RB}$ 

# Synthetic Example 4 (f=500)

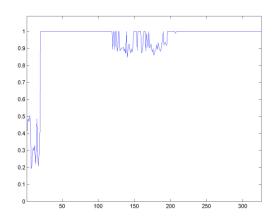


Ground truth *I* 

1 0.9 0.8 0.7 0.6 0.5 0.4 0.3 0.2 0.1 0.5 0.1 0.0 150 200 250 300

Radial bright channel *I*<sup>RB</sup>

Our result  $I_E$  (PSNR: 75.56)



Radial bright channel  $I_F^{RB}$ 

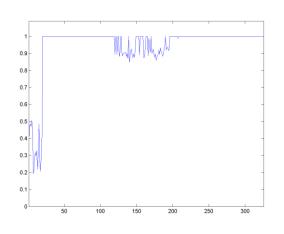
## Synthetic Example 4 (f=1300)





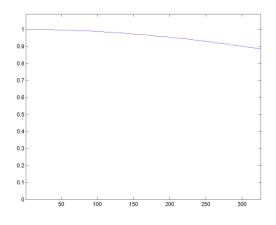


Ground truth I



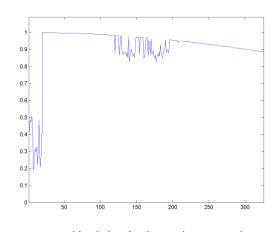
Radial bright channel IRB

Ground truth V



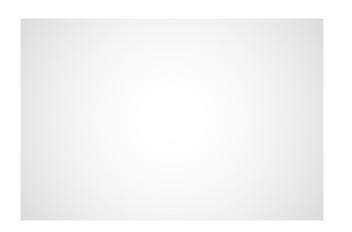
Radial bright channel VRB

Synthetic input Z

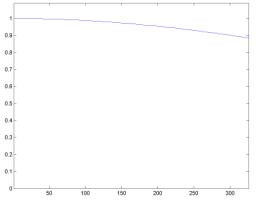


Radial bright channel  $Z^{RB}$  37

#### Synthetic Example 4 (f=1300)



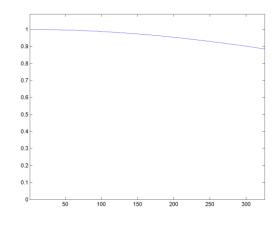
Ground truth V



Radial bright channel VRB



Our result  $V_E$  estimated from Z

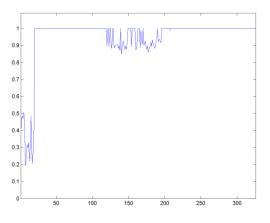


Radial bright channel  $V_E^{\ \ \mathrm{RB}}$ 

## Synthetic Example 4 (f=1300)



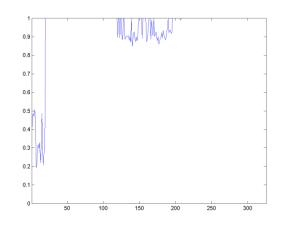
Ground truth *I* 



Radial bright channel IRB



Our result  $I_E$  (PSNR: 77.89)



Radial bright channel  $I_E^{RB}$ 

Thank you!