COLORIZATION IN YCBCR SPACE AND ITS APPLICATION TO IMPROVE QUALITY OF JPEG COLOR IMAGES

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ABSTRACT
This paper presents a colorization method in YCbCr color space, which is based on the maximum a posteriori estimation of a color image given a monochrome image as is our previous method in RGB color space. The presented method in YCbCr space is much simpler than that in RGB space and requires much less computation time, while both methods in YCbCr and RGB space produce color images with comparable PSNR values. The proposed colorization in YCbCr is applied to JPEG compressed color images aiming at better recovery of downsampled chrominance planes. Experimental results show that colorization in YCbCr is usually effective for quality improvement of JPEG color images.

Index Terms— Colorization, JPEG, MAP estimation, MRF, YCbCr

1. INTRODUCTION
Colorization is usually a computer-aided process of adding color to monochrome images or movies. Colorization is now generally carried out manually using some drawing software tools. Obviously such manual work is very expensive and time-consuming.

Several colorization methods [1, 2, 3] have already been proposed which do not require intensive manual effort. Welsh et al. proposed a semi-automatic method to colorize a monochrome image by transferring color from a reference color image [1]. This method requires an appropriate reference color image prepared by a user. Levin et al. have proposed an interactive method, where a user needs to give some color scribbles and the colors are automatically propagated to produce a fully colorized image [2]. Horiuchi [3] has proposed a method where a user gives colors for some pixels and the colors are automatically propagated to produce a fully colorized image [2]. Horiuchi [3] has proposed a semi-automatic method to colorize a monochrome image given a monochrome image as is our previous method in RGB space [5].

2. COLOR IMAGE ESTIMATION IN RGB SPACE
In this section, we review our previous colorization method in RGB space [5].

2.1. Estimation Algorithm
Let \( x_L = \{ x_{ij}; (i, j) \in L \} \) and \( y_L = \{ y_{ij}; (i, j) \in L \} \) denote the set \( \{ x_{a1}, \ldots, x_{al} \} \) and the multivariable function \( f(x_{a1}, \ldots, x_{al}) \) respectively, where \( A = \{ a_1, \ldots, a_l \} \).

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Assuming a Markov random field (MRF) for \( x_L \) and then using the mean field approximation, \( p(x_L) \) can be decomposed as
\[
p(x_L) \simeq \prod_{(i,j) \in L} p(x_{ij} \mid (x)_{n_{ij}}), \tag{6}
\]
where \( n_{ij} \) denotes \((i, j)\) pixel’s neighborhood and \((x)_{n_{ij}}\) denotes the mean fields for \( x_{n_{ij}} \). Substituting (4) and (6) into (3) and replacing \( \sum_{x_L} \prod_{(i,j) \in L} p(x_{ij}) \) by \( \prod_{(i,j) \in L} \sum_{x_{ij}} \), we obtain the following decomposition for \( p(x_L \mid y_L) \):
\[
p(x_L \mid y_L) \simeq \prod_{(i,j) \in L} p(x_{ij} \mid y_{ij}, (x)_{n_{ij}}), \tag{7}
\]
where
\[
p(x_{ij} \mid y_{ij}, (x)_{n_{ij}}) = \frac{1}{\sum_{x_{ij}} \exp\left(-\frac{1}{2} \left( x_{ij} - m_{ij}^{(p)} \right)^T \Sigma^{-1} \left( x_{ij} - m_{ij}^{(p)} \right) \right) p(x_{ij} \mid (x)_{n_{ij}})}.	ag{8}
\]

In the following, \( x_{n_{ij}} \) is simply used for \((x)_{n_{ij}}\). Then \( p(x_{ij} \mid y_{ij}, x_{n_{ij}}) \) is considered as local a posteriori probability (LAP). Using these LAPs, the global optimization problem shown by Eq. (2) is approximately decomposed into the local optimization problems
\[
x_{ij} = \arg \max_{x_{ij}} p(x_{ij} \mid y_{ij}, x_{n_{ij}}), \tag{9}
\]
In order to solve (9) for all \((i, j)\) pixels, their neighboring color vectors \( x_{n_{ij}} \) should be given. Since such a problem as shown in (9) can be solved iteratively as is popular in numerical analysis, we rewrite Eq. (9) as
\[
x_{ij}^{(p+1)} = \arg \max_{x_{ij}} p(x_{ij} \mid y_{ij}, x_{n_{ij}}),
\]
where \( p \) represents the \( p \)th iteration.

Regarding \( p(x_{ij} \mid x_{n_{ij}}) \) in (8), a Gaussian MRF is here used whose local conditional probability density function (pdf) is given as
\[
p(x_{ij} \mid x_{n_{ij}}) = \frac{1}{\sqrt{(2\pi)^{N} \Sigma}^{|1/2}} \exp\left(-\frac{1}{2} \left( x_{ij} - m_{ij}^{(p)} \right)^T \Sigma^{-1} \left( x_{ij} - m_{ij}^{(p)} \right) \right),
\]
\[
x_{n_{ij}} = \frac{1}{|N|} \sum_{\tau \in N} x_{ij+r}, \tag{12}
\]

Here \( \bar{x}_{n_{ij}} \) is the mean of neighboring pixels’ color vectors \( x_{n_{ij}} = \{ x_{ij+r}, \tau \in N \} \), where \( N \) denotes the neighborhood of \((0, 0)\) pixel. For example, \( N = \{ (0, 1), (0, -1), (1, 0), (-1, 0) \} \) for the first-order neighborhood, and if \( \tau = (0, 1) \), \( x_{ij+r} = x_{ij+1} \). \( \Sigma \) is the covariance matrix of \( x_{ij} - \bar{x}_{n_{ij}} \). Considering (1), (8), (11) and (12), the local MAP estimation (10) is rewritten as the following constrained quadratic programming problem:
\[
\begin{align*}
\text{minimize} & \quad (x_{ij} - m_{ij}^{(p)})^T \Sigma^{-1} (x_{ij} - m_{ij}^{(p)}) \\
\text{subject to} & \quad \alpha^T x_{ij} = y_{ij}, \quad 0 \leq r_{ij}, g_{ij}, b_{ij} \leq 255.
\end{align*}
\]
where

\[ c_{ij} = \frac{1}{|N|} \sum_{\tau \in N} c_{ij+\tau} \]  \hspace{1cm} (22)

\[ y_{ij} = \frac{1}{|N|} \sum_{\tau \in N} y_{ij+\tau} \]  \hspace{1cm} (23)

In initial color estimation, chrominance components of a selected reference for \((i, j)\) pixel are used as those of \(x_{ij}^{(0)}, i.e., c_{ij}^{(0)}\).

4. EXPERIMENTAL RESULTS

In order to compare colorization performance in YCbCr space with that in RGB space, experiments were carried out using four standard color images (Lena, Milkdrop, Peppers, Mandrill). These images are 256 × 256 pixels in size and 24 bit per pixel (bpp) full color images. Their monochrome images were produced by the transform shown in (1) from the original color images and used for colorization experiments. For initial color estimation, several numbers of reference color vectors were given from each original image, whose positions in the image were randomly selected. It is fair to select reference positions randomly because colorization performance depends on positions of given references.

The local MAP estimation in RGB space, i.e., the constrained quadratic programming problem in (13) and (14), was here directly solved using a quadratic programming solver [7]. In YCbCr space, the solution of (15) is given in (21) with (22) and (23). In the calculation of \(x_{ij}^{(0)}\) in (13) and in (15), the third-order neighborhood\(^2\) was used and \(x_{ij+\tau}^{(0)}\) whose luminance value \(y_{ij+\tau}\) is far from \(y_{ij}\) was excluded from the calculation. In the following experiments, if \(|y_{ij+\tau} - y_{ij}| > 0.5s\), where \(s\) is the standard deviation of luminance values averaged over four images, \(x_{ij+\tau}^{(0)}\) was excluded from the calculation of \(x_{ij}^{(0)}\). For the covariance matrix \(\Sigma\) in (13) and (15), the average of normalized covariance matrices (normalized by their maximum components) for four images was used.

**Table 1.** Colorization performance (PSNR(dB)) using 25 references in YCbCr and RGB space

<table>
<thead>
<tr>
<th>Image</th>
<th>YCbCr</th>
<th>RGB</th>
</tr>
</thead>
<tbody>
<tr>
<td>Lena</td>
<td>initial 25.1 ± 1.0</td>
<td>24.9 ± 0.9</td>
</tr>
<tr>
<td>Milkdrop</td>
<td>initial 23.4 ± 1.1</td>
<td>23.6 ± 1.5</td>
</tr>
<tr>
<td>Peppers</td>
<td>initial 20.8 ± 0.5</td>
<td>20.7 ± 0.5</td>
</tr>
<tr>
<td>Mandrill</td>
<td>initial 17.3 ± 0.7</td>
<td>17.1 ± 0.7</td>
</tr>
</tbody>
</table>

Colorization performance using 25 references measured by PSNR value and CIELAB distance is shown in Table 1 and Table 2, respectively. Experiments were carried out 20 times using randomly selected references and each result is shown as mean value ± standard deviation of 20 experimental values in the tables. For each image, the upper row shows performance of initial color estimation and the lower row shows the final result after the iterative MAP estimation.

**Table 2.** Colorization performance (CIELAB distance) using 25 references in YCbCr and RGB space

<table>
<thead>
<tr>
<th>Image</th>
<th>YCbCr</th>
<th>RGB</th>
</tr>
</thead>
<tbody>
<tr>
<td>Lena</td>
<td>initial 8.5 ± 0.8</td>
<td>11.3 ± 1.7</td>
</tr>
<tr>
<td>Milkdrop</td>
<td>initial 21.2 ± 2.1</td>
<td>22.4 ± 3.2</td>
</tr>
<tr>
<td>Peppers</td>
<td>initial 31.8 ± 2.5</td>
<td>32.2 ± 2.1</td>
</tr>
<tr>
<td>Mandrill</td>
<td>initial 22.7 ± 3.1</td>
<td>25.0 ± 4.0</td>
</tr>
</tbody>
</table>

Iterations were stopped when the difference of estimated color components averaged over all pixels at a current and the previous iteration became less than 0.5. Mean of the number of iterations is also given in Table 1. It is seen that colorization performance in YCbCr measured by PSNR is comparable to that in RGB and that in YCbCr measured by CIELAB distance is a little bit better than that in RGB. Regarding computation time, colorization in YCbCr took approximately only one fourth the computation time in RGB, though even in RGB space it took only 6 seconds at most to colorize one image. This time reduction is due to the aforementioned unconstrained optimization in YCbCr space resulting in the simple computation shown in (21). Note that in RGB space, a certain amount of numerical computation is needed to solve the constrained quadratic programming problem.

5. APPLICATION TO JPEG COLOR IMAGES

In JPEG compression, R, G, B color components are converted to Y, Cb, Cr components and each of the three color planes is processed independently. The chrominance planes, Cb and Cr planes are usually downsampled by a factor of two. At JPEG decompression stage, the downsampled Cb and Cr planes are interpolated by repetition followed by spatial smoothing with a low-pass filter.

The proposed colorization in YCbCr space is applied to JPEG compressed color images, where the interpolated and smoothed chrominance components are used as initial values \(c_{ij}^{(0)}\)’s for the iterative MAP estimation. The iterative MAP estimation shown in (21) has a structure that chrominance components are estimated considering luminance component which is not downsampled, and therefore we can expect a better recovery of them. In the application to JPEG color images, one or two iterations were enough for the MAP estimation and the following experimental results are those by one iteration. The covariance matrix in (15) for each image was computed using each JPEG compressed image.

Experimental results are shown in Fig. 1 and Fig. 2, where PSNR values are plotted for four different quality factor (qf) images: qf=60, 70, 80, and 90, and the leftmost and the rightmost point of each line correspond to qf=60 and qf=90, respectively. Larger quality factor image has higher quality and larger PSNR value with larger bit rate (larger file size). Fig. 1 shows results for Lena of three different pixel sizes: 128 × 128, 256 × 256, and 512 × 512 pixels. It is seen that significant improvement on PSNR value is achieved particularly in small size cases. Fig. 2 shows colorization results applied to JPEG compressed four color images of 256 × 256 pixels in size. It is seen that colorization is effective to improve PSNR value of JPEG compressed images except for Peppers with qf=90 and Mandrill. Fig. 3 shows a closeup result for Milkdrop, where

\(^2\)For the third-order neighborhood, \(N = \{(0, 1), (0, -1), (1, 0), (-1, 0), (1, 1), (-1, -1), (1, -1), (-1, 1), (0, 2), (0, -2), (2, 0), (-2, 0)\}\)
Fig. 1. Experimental results on colorization applied to JPEG compressed color image Lena of 128 × 128, 256 × 256, and 512 × 512 pixels in size.

quality improvement can be visually perceived. From these results, it could be addressed that colorization in YCbCr space is usually effective for quality improvement of JPEG color images except for very complex and/or textured images such as Mandrill.

6. CONCLUSIONS

This paper presented a colorization method in YCbCr space, which is in principle based on the MAP estimation of a color image given a monochrome image as is our previous method in RGB space. The presented method in YCbCr space is much simpler than that in RGB space and requires much less computation time: about one fourth the computation time in RGB space. As for quality of estimated color image, both methods in YCbCr and RGB space produce color images with comparable PSNR values.

The proposed colorization in YCbCr space was applied to JPEG compressed color images aiming at better recovery of downsampled chrominance planes. Experimental results show that colorization in YCbCr space is usually effective for quality improvement of JPEG color images.

7. REFERENCES