# Microparticle Manipulation using Multiple Untethered Magnetic Micro-Robots on an Electrostatic Surface

Steven Floyd\*, Chytra Pawashe\*, and Metin Sitti

Abstract—This work presents the control of multiple untethered rectilinear magnetic micro-robots (Mag- $\mu$ Bots) with dimensions  $250 \times 130 \times 100 \ \mu m^3$  actuated by pulsed external magnetic fields, which translate by induced stick-slip motion at speeds of up to 4 mm/s immersed in silicone oil. Multiple Mag- $\mu$ Bot control is enabled by employing an array of individually addressable electrostatic surfaces to selectively anchor individual Mag- $\mu$ Bots. Coupled parallel and uncoupled serial motion of multiple robots is demonstrated, and they can combine to form an assembly that is also capable of motion. Manipulation of 230  $\mu$ m diameter microspheres is also demonstrated cooperatively by two Mag- $\mu$ Bots in a fluid environment, and is enhanced when the two Mag- $\mu$ Bots are combined. An analysis of the electrostatic anchoring forces and the forces relevant to manipulation is discussed.

## I. INTRODUCTION

The recent emergence of sub-millimeter sized mobile micro-robots has introduced new approaches to power delivery and control at the micron-scale. The current designs in literature, including electrostatic [1], [2], electromagnetic [3]-[7], laser driven thermal impact [8], and bacteria propelled systems [9], [10], have resulted in successful wireless control of individual micro-robots. These micro-robots are also capable of manipulating micron-scale objects in their respective workspaces. For example, Zhang et al. [4] demonstrate 6  $\mu$ m spheres being manipulated by a microswimming flagellar device, and Frutiger et al. [5] show that 150  $\mu$ m gold discs can be moved by a mobile micro-magnetic actuator. These approaches offer a valuable alternative to conventional micro-grippers controlled by a multi-degreeof-freedom macro-scale positioning system, which can be complex, difficult to control, and expensive [11]. In addition, such a system does not share the advantages of untethered micro-robots where the micron-scale end-effector is entirely contained within the workspace.

For any contact-based micro-manipulation method, stiction between the end-effector and micro-object becomes relevant at the micron-scale, making the release of grasped micro-objects difficult. Methods to combat this problem can include using ice to form and break connections between end-effectors and micro-objects, vibrating the end-effector to release a grasped object, employing vacuum to selectively capture and release micro-objects, and using electrostatic attraction and repulsion to manipulate micro-objects [12], [13]. Alternatively, the micro-object can be immersed in fluid, where micro-manipulation can be easier because stiction effects dramatically reduce. However, this limits applications to situations where the micro-object can be immersed, which is not always desired.

A new challenge in micro-robotics is the control of multiple untethered agents, where the power delivery and control mechanisms may not be conducive to this task. Donald et al. [1] demonstrate the control of four electrostatically actuated MEMS micro-robots, which are all designed to be physically different to respond differently to the global driving electric field. Motion among these micro-robots is coupled, and requires sophisticated algorithms to create paths for each micro-robot. Using magnetic-resonant micro-robots, Kratochvil et al. [6] demonstrate that decoupled motion is possible. Like in [1], these individual micro-robots must be physically different, so that their response to the global driving fields are unique.

To enable the control of multiple magnetic micro-robots (Mag- $\mu$ Bots) in our electromagnetically actuated system, we introduce a structured surface where electrostatic forces can be applied in order to selectively anchor Mag- $\mu$ Bots to the surface, which we demonstrate in [14]. This allows for any unanchored Mag- $\mu$ Bot to be driven by the encompassing magnetic fields, while keeping anchored Mag- $\mu$ Bots immobile. This approach allows for both the uncoupled serial actuation and coupled parallel actuation of multiple Mag- $\mu$ Bots. In this scheme, Mag- $\mu$ Bots do not need to be specially designed, reducing complexity of micro-robot fabrication.

Using Mag- $\mu$ Bots, the manipulation of microparticles can be performed within a fluid environment, which reduces the effects of stiction. In addition to forces exerted by the Mag- $\mu$ Bot by contact manipulation, fluid forces can also affect microparticles, caused by the displacement of fluid by the Mag- $\mu$ Bot while moving. This effect is explored in [15], where a single Mag- $\mu$ Bot can manipulate microparticles as small as 50  $\mu$ m, limited by the imaging resolution of the system. The combination of multiple Mag- $\mu$ Bots and microparticle manipulation can lead to the vision of teams of micro-robots playing soccer, which is a goal for the RoboCup Nanogram league [16].

# II. TOOLS AND CONCEPT

A rectilinear Mag- $\mu$ Bot with dimensions  $250 \times 130 \times 100 \ \mu m^3$  is actuated by six independent electromagnetic coils, aligned to the faces of a cube approximately 11 cm on a

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side, with horizontal and vertical coils capable of producing maximum field strengths at the position of the Mag- $\mu$ Bot of 3.0 mT and 2.3 mT, respectively (see Fig. 1). Imaging of the Mag- $\mu$ Bot and the workspace is accomplished by a camera (Sony XC-75) connected to a variable magnification microscope lens, providing an 8.6 mm × 7.2 mm field of view. Control of the electromagnetic coils is performed by a PC with a data acquisition system at a control bandwidth of 1 kHz, and the coils are powered by custom-made electronic amplifiers. The Mag- $\mu$ Bot is made of neodymium-iron-boron (NdFeB, N42 grade), a hard magnetic material. To create the robot, a magnetized piece of NdFeB was cut using a laser machining system (NewWave LaserMill).

Actuation of each Mag-µBot is accomplished by using two or three electromagnetic coils. One or more horizontal coils are first enabled (coil D in Fig. 1), causing the Mag- $\mu$ Bot to orient in the direction of the net magnetic field. The magnetic force exerted by the coils on the Mag- $\mu$ Bot is insufficient to translate it, due to friction and adhesion to the surface. Vertical clamping coils (coils C and F in Fig. 1) are enabled and pulsed using a sawtooth waveform, resulting in a nonuniform rocking motion of the Mag- $\mu$ Bot, which induces stick-slip motion across the surface. In general, the Mag- $\mu$ Bot's velocity increases with pulsing frequency, typically from 1-100 Hz, and can exceed velocities of 16 mm/s in air, and 4 mm/s in silicone oil, as used in this study. The Mag- $\mu$ Bot is also capable of operating in fluids of viscosities less than about 50 cSt, and can operate on a variety of smooth and rough magnetically inactive surfaces, provided that the adhesion between the Mag- $\mu$ Bot and surface is low. With an appropriate driving waveform, the Mag- $\mu$ Bot can be moved in steps down to about 5  $\mu$ m.

Further details on this system are explained in [3], where modeling of the stick-slip dynamics is performed, and experimental analyses of robot motion is presented. Videos of operation can be found at [17], [18].

#### A. Multi-Robot Control

In Fig. 2, a schematic displaying the concept of multirobot motion control is shown with four Mag- $\mu$ Bots. The Mag- $\mu$ Bots move on a grid surface, where each cell contains a set of interdigitated electrodes that provide electrostatic anchoring, and each cell is independently addressable [14]. To fabricate the surface, a silicon wafer is first coated with a 25  $\mu$ m layer of SU-8. 100 nm of aluminum is then sputtered onto it, and patterned into the electrodes. A final layer of SU-8, approximately 1.5  $\mu$ m thick, is coated onto the aluminum, and is in direct contact with the Mag- $\mu$ Bots. SU-8 is used for its high dielectric strength (112 V/ $\mu$ m), which supports the generation of the electric fields necessary to anchor a Mag- $\mu$ Bot without damaging the substrate. For experiments, a surface with 16 independent electrostatic pads in a  $4 \times 4$  grid configuration was fabricated. Figure 3 displays a free body diagram of an anchored Mag- $\mu$ Bot with external electrostatic and magnetic forces, and a cross-section of the surface.

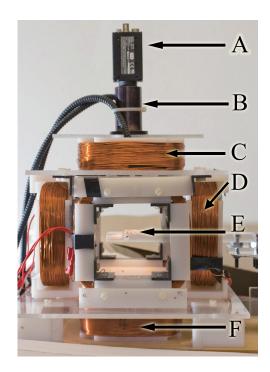


Fig. 1. Photograph of the electromagnetic coil setup, where A is the camera for visual feedback, B is the microscope lens, C is the top coil, D is one of four upright coils that orients the Mag- $\mu$ Bot within the plane on the surface, E is the surface on which the Mag- $\mu$ Bot locomotes, and F is the bottom coil. The top and bottom coils are clamping coils, which provide a clamping force and a torque that pushes and orients the Mag- $\mu$ Bot towards the surface, respectively.

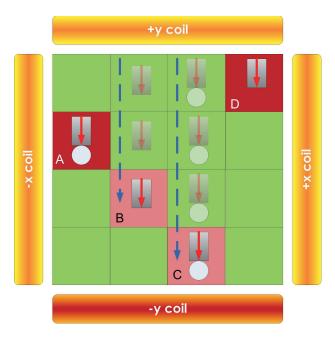


Fig. 2. Top-down schematic of four Mag- $\mu$ Bots, A, B, C, and D, demonstrating coupled and decoupled motion. The -y coil is enabled, causing robots to orient in the -y-direction. Robots A and D are anchored to the surface and do not translate. Robots B and C translate in the -y-direction; robot B is anchored after having traversed one pad. Robot C pushes a microsphere during its travel.

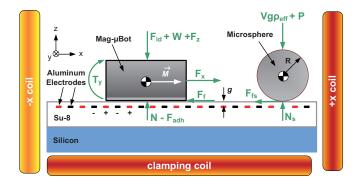


Fig. 3. Schematic of the Mag- $\mu$ Bot and a microsphere with magnetic, electrostatic, and gravitational forces and torques displayed. The Mag- $\mu$ Bot experiences an electrostatic anchoring force  $(F_{id})$ , its weight (W), magnetic forces  $(F_z \text{ and } F_x)$ , a magnetic torque  $(T_y)$ , a static friction force  $(F_f)$ , a reactive normal force (N), and an adhesive force  $(F_{adh})$  due to surface effects.  $\vec{M}$  denotes the magnetization vector of the Mag- $\mu$ Bot. When translating, forces on the microsphere include its effective weight  $(Vg\rho_{eff})$ , an adhesion force  $(F_{fs})$ . The clamping and +x coils are active. The composition of the electrostatic surface is also displayed.

## III. MODELING

The Mag- $\mu$ Bot experiences electromagnetic, electrostatic, adhesive, and fluid forces from the environment. The effects of the electromagnetic forces are explained in detail in [3]. When a robot is anchored, the electrostatic force must prevent motion of the robot. To do this, it must prevent the robot from pivoting, which in turn prevents the stick-slip motion from occurring.

Microspheres in the workspace also experience these forces; magnetically inactive spheres, as used in this paper, will not respond to the magnetic fields. When each Mag- $\mu$ Bot is manipulating a microsphere, two interactions are of importance: the effects of adhesion and friction between the microsphere and the substrate, and the induced drag force on the microsphere from the fluid. The robot must be able to overcome both of these to successfully push microspheres. The effects of an electric field in the workspace can exert electrophoretic and dielectrophoretic forces on the microspheres. For the purposes of this paper, we ignore electrophoresis by assuming particles do not become charged while in the fluid, and assume that dielectrophoretic forces, due to the relatively large microsphere sizes used.

This section provides the derivations of the relevant forces, and examines the conditions necessary for successful selective manipulation. The detailed effects of the fluid forces on limiting micro-robot velocity and allowing non-contact manipulation of micro-objects is covered in detail in [15].

## A. Adhesion at the Micron-scale

When trying to pull two objects apart from one another, a non-zero pull-off force arises. This force is due to a combination of van der Waals interactions, capillary effects, and electrostatic charging [19]. Capillary forces can be neglected if the humidity is kept below 10%. Electrostatic effects are usually small compared to van der Waals effects due to the low dielectric strength of air [20]. To determine what the pull-off force for separating two materials 1 and 2 is, the work of adhesion,  $W_{12}$ , must be determined for the pair utilizing their intrinsic surface energies  $\gamma_1$  and  $\gamma_2$  [21], [22]:

$$W_{12} = \gamma_1 + \gamma_2 - \gamma_{12} \approx 2\sqrt{\gamma_1 \gamma_2}.$$
 (1)

Adhesion modeling for micro and nanoparticle manipulation is discussed in [23], where the Johnson-Kendall-Roberts (JKR), Deraguin-Muller-Toporov (DMT), and Maugis-Dugdale (MD) models are explained. The range of possible pull-off forces, P, is curtailed and will fall within the range of:

$$\frac{3}{2}\pi R_e W_{12} \le P \le 2\pi R_e W_{12} \tag{2}$$

where the exact value of P can be determined based upon a variable called the elasticity parameter [22]. Hence, with only information on the surface energy of the material, an upper limit on P can be determined.

Values of several of these properties for different materials used in this work are given in Table I; the microspheres used are 230  $\mu$ m diameter polystyrene divinylbenzene (PS-DVB, Duke Scientific Inc, properties assumed to be similar to polystyrene), and the fluid used is silicone oil (Dow Corning 200 fluid, 20 cSt).

	Surface	Density	Dielectric
Material	Energy $(\gamma)$	$(\rho)$	<b>Constant</b> $(\epsilon_r)$
	$[mJ \cdot m^{-2}]$	$[kg/m^{-3}]$	-
SU-8	30-40 [24]	-	4.1
Polystyrene	33-40 [21], [25]	1060	-
Silicone oil	19.8-21 [26], [27]	935	2.3

## TABLE I PROPERTIES OF MATERIALS

Due to the range of possible surface energies for the materials in Table I, there is a large range of pull-off forces that can potentially exist for a polystyrene sphere of a given diameter on SU-8.

For irregularly shaped particles, the pull-off force will be greatly reduced from its perfectly smooth value, given in Eq. (2). To account for this, the irregularity can be quantified by treating the effective contact as a summation of several smooth spheres of varying radii:

$$P_{eff} = \sum_{i=1}^{N} \frac{3}{2} \pi R_i W_{12} = \frac{3}{2} \pi W_{12} \sum_{i=1}^{N} R_i.$$
 (3)

If we assume that the number of contact points scales with the particle radius, and that the distribution of contact point radii is independent of the particle radius, then the summation term can be treated as an effective radius,  $\sum_{i=1}^{N} R_i =$  $R_{eff} = hR$ , where  $h \leq 1$ . For highly irregular particles,  $h \approx 0.1$  [28]. Using experimental data obtained from earlier work [29], the roughness of the polystyrene particles used in this work results in  $h \approx 0.12$ .

#### B. Adhesion in Fluid

When operating completely within a fluid, the capillary and electrostatic contributions to the pull-off force can be neglected. The van der Waals adhesion can be determined by taking into account the interactions with the fluid medium [22]:

$$W_{132} = W_{12} + W_{33} - W_{13} - W_{23} \tag{4}$$

where the subscripts 1 and 2 correspond to the solid materials, and 3 corresponds to the fluid medium.

In such a case, the resulting work of adhesion can be either positive or negative. Negative values imply the two surfaces repel each other, and the surfaces minimize their energy by contacting the fluid, not each other. For the range of values presented in Table I, the range for the immersed work of adhesion is  $2.1 \text{ mJ} \cdot \text{m}^{-2} < W_{132} < 6.9 \text{ mJ} \cdot \text{m}^{-2}$ . Taking into account particle irregularity, this translates into a range of pull-off forces of 180 nN  $< P_{eff} < 595$  nN.

#### C. Electrostatic Force

For the case of a conductive Mag- $\mu$ Bot above an SU-8 insulation layer covering a set of interdigitated electrodes at an applied voltage difference of  $V_{id}$ , the conductor will assume the mean potential if it overlaps equal areas of electrodes at both voltages [2]. With this assumption, the voltage difference between the Mag- $\mu$ Bot and each electrode will be  $\frac{1}{2}V_{id}$ . Assuming negligible fringing, an estimate of the anchoring force  $(F_{id})$  exerted by the interdigitated electrodes onto the Mag- $\mu$ Bot is:

$$F_{id} = \frac{\epsilon_0 \epsilon_r}{8g^2} V_{id}^2 A_{id} \tag{5}$$

where  $A_{id}$  is the area of the Mag-µBot overlapping the electrodes, g is the insulator thickness,  $\epsilon_0$  is the permittivity of free space, and  $\epsilon_r$  is the relative static permittivity of the insulating material (SU-8).

To anchor a Mag- $\mu$ Bot to the surface, the electrostatic force must suppress any Mag- $\mu$ Bot rotation about its contact point with the surface, caused by the magnetic torque,  $T_y$ . The effect of this torque significantly dominates all the other interactions experienced by the Mag- $\mu$ Bot, shown in Fig. 3. The maximum magnetic torque ( $T_{max}$ ) that can be applied to a robot with a magnetization  $\vec{M}$  at the maximum field strength  $\vec{B}_{max}$  within this system is [3]:

$$T_{max} = \vec{M} \times \vec{B}_{max} \approx 2.88 \times 10^{-9} [\text{N} \cdot \text{m}] \qquad (6)$$

Treating the magnetic torque as a pair of forces acting in opposite directions on the ends of the Mag- $\mu$ Bot, each of these forces is approximately 11.6  $\mu$ N. To counteract this, the anchoring force must be approximately twice this value, as it is evenly distributed across the bottom of the robot, and the torque about the pivot point will act at the center of the robot. Using Eq. (5) and noting that for electrodes that are 10  $\mu$ m wide with 10  $\mu$ m spacing, making  $A_{id}$  approximately half the apparent robot area of  $A_{id} = 0.5 \cdot (250 \times 130 \ \mu\text{m}^2)$ ,

the required voltage is approximately  $V_{id} = 26$  V with g = 1.5  $\mu$ m.

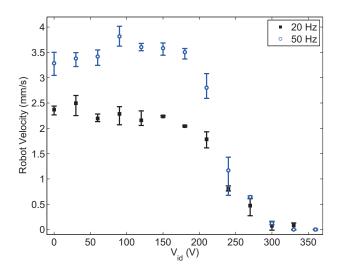


Fig. 4. Mag- $\mu$ Bot velocity vs. electrostatic anchoring voltage,  $V_{id}$ , at two pulsing frequencies on an SU-8 substrate with  $g = 1.5 \ \mu m$  in silicone oil. Each data point represents three experiments.

In Fig. 4 an experimental plot of Mag- $\mu$ Bot velocity vs.  $V_{id}$  is shown for two actuation frequencies. Velocity is measured by analyzing frames from a video of an experiment. As  $V_{id}$  increases from 0 V, the Mag-µBot's velocity slightly increases, particularly in the 50 Hz case; this can be due to an increased downward force causing the Mag- $\mu$ Bot to travel more during its slip phase (effectively adding to the magnetic clamping force). The Mag-µBot's velocity begins to decrease at  $V_{id} = 180$  V, which is when the electrostatic anchoring force begins to dominate and detriments the slipping motion. The Mag- $\mu$ Bot completely stops at about  $V_{id} = 360$  V; this high voltage requirement is likely caused by roughness on the Mag- $\mu$ Bot's surface, which can trap fluid beneath it and increase the separation from the electrodes. An additional fluid layer with thickness comparable to the robot's maximum asperity height of about  $a = 10 \ \mu m$ , causes the total capacitance  $C_{tot}$  between the robot and the electrodes to be:

$$C_{tot} = \left(C_1^{-1} + C_2^{-1}\right)^{-1} \tag{7}$$

where  $C_1$  is the capacitance associated with the SU-8 ( $C_1 = \epsilon_0 \epsilon_{r1} g^{-1} A_{id}$ ) and  $C_2$  is associated with the fluid gap ( $C_2 = \epsilon_0 \epsilon_{r2} a^{-1} A_{id}$ ). Using the principal of virtual work and successive application of the chain rule for differentiation, the electrostatic anchoring force with a fluid gap ( $F_{id,fg}$ ) will be:

$$F_{id,fg} = \frac{1}{16} V_{id}^2 C_{tot}^2 \left[ \frac{1}{C_1 g} k + \frac{1}{C_2 a} (1-k) \right] A_{id} \quad (8)$$

where k is a constant (0 < k < 1) relating the amount of virtual SU-8 displacement that occurs per unit of total virtual displacement. Taking the limit when k = 0 and all the contraction is in the fluid gap, 257 V is required to anchor the robot. When k = 1 and all the contraction is in the SU-8, 343 V is required. This range is slightly lower than the experimentally determined voltage of 360 V. Minor fabrication defects such as poorly formed electrodes, variations in insulation thickness, resistive losses in the electrodes, and variations in the roughness of the robots can cause the required voltage to increase.

## D. Manipulation Capabilities

Using the information in the previous sections, logical limits can be determined on the Mag- $\mu$ Bot's ability to push a microsphere based upon the forces that must be overcome. Within a fluid medium, there exists a minimum lateral force,  $F_{min}$ , to move an object:

$$F_{min} \approx \mu_f \left[ 2\pi R W_{132} + (\rho_p - \rho) V g \right] \tag{9}$$

where  $\mu_f$  is the immersed friction coefficient between the surface and the object. For the case of a 230  $\mu$ m sphere, 18 nN <  $F_{min}$  < 59 nN if it is assumed  $\mu_f = 0.1$ .

The maximum possible forces exerted by the Mag- $\mu$ Bot can be roughly estimated as the maximum lateral magnetic force that can be applied to the Mag- $\mu$ Bot, approximately 52 nN [3]. Hence, if the immersed friction coefficient is much larger than 0.1, or if the surface energies of SU-8 and polystyrene are near the high end of their ranges, pushing with a single robot will be difficult, if not impossible.

## IV. RESULTS AND DISCUSSION

To demonstrate the control of multiple Mag- $\mu$ Bots with the electrostatic anchoring surface, three Mag- $\mu$ Bots were placed on the surface within silicone oil, which supports the generation of the electric anchoring fields and enables microsphere manipulation due to reduced stiction effects. An electrostatic potential of  $V_{id} = 400$  V was used to anchor the Mag- $\mu$ Bots.

In Fig. 5, three Mag- $\mu$ Bots are displayed, where uncoupled serial motion and coupled parallel motion are both demonstrated. In addition the Mag- $\mu$ Bots assemble and are able to translate while assembled; qualitatively, this Mag- $\mu$ Bot structure translates at higher velocities than each individual Mag- $\mu$ Bot.

In Fig. 6, two Mag- $\mu$ Bots are displayed with four 230  $\mu$ m diameter PS-DVB microspheres. Each of the Mag- $\mu$ Bots takes turns pushing the spheres in a serial fashion. The two Mag- $\mu$ Bots then assemble and the combined structure is capable of pushing spheres as well.

From these experiments, the electrostatic anchoring surface is capable of preventing Mag- $\mu$ Bot motion. In most cases however, anchored Mag- $\mu$ Bots will change in orientation due to the encompassing magnetic field. This occurs because the relatively strong magnetic torque exerted on the Mag- $\mu$ Bot overcomes any additional friction to the surface caused by anchoring. This friction is derated due to the fact that the Mag- $\mu$ Bot's surfaces are rough, causing adhesion to the surface to decrease. In some cases the Mag- $\mu$ Bot remains fixed in orientation, e.g.  $R_b$  in Fig. 5c-d, possibly due to a relatively smooth surface on this particular Mag- $\mu$ Bot. When two Mag- $\mu$ Bots become sufficiently close to each other, they jump-into contact due to the high magnetic field gradients caused by their magnetization. This jumpinto distance implies that there is a minimum distance two Mag- $\mu$ Bots must maintain between each other to ensure successful individual motion, and is experimentally about 2-3 body lengths (500-750  $\mu$ m) within fluid. This distance can be reduced by designing robots with lower magnetizations. Assembled Mag- $\mu$ Bots are still capable of translating, as the fundamental stick-slip dynamics have not changed. Translational speeds observed are higher with this structure because the magnetic forces and torque scale with volume, while the viscous drag and surface adhesion scale only with area.

Microsphere manipulation is performed by the Mag- $\mu$ Bots; however some microspheres tend to stick to the substrate more than others, and as a result, individual Mag- $\mu$ Bots are sometimes incapable of moving them (as in Fig. 6b). When the Mag- $\mu$ Bots combine into larger assemblies, the total pushing force also increases, which allows previously stuck microspheres to be pushed (see Fig. 6d).

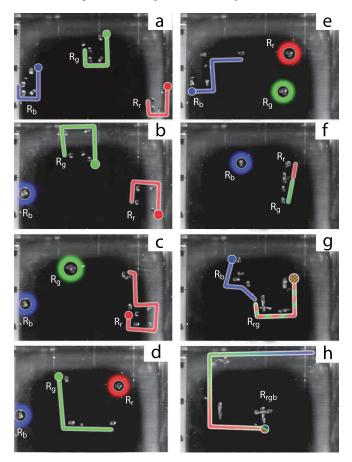


Fig. 5. (Color online) Frames from a movie with three Mag- $\mu$ Bots,  $R_r$  (red),  $R_g$  (green), and  $R_b$  (blue), traversing individually and in parallel under silicone oil. In (a) all three robots move identically, in (b)  $R_b$  is anchored and  $R_g$  and  $R_r$  move, in (c)  $R_g$  becomes anchored and  $R_r$  moves, in (d) only  $R_g$  is free to move, in (e) only  $R_b$  is free to move, in (f),  $R_r$  and  $R_g$  combine into  $R_{rg}$ , in (g)  $R_{rg}$  moves to combine with  $R_b$ , and in (h) all robots combine into  $R_{rgb}$  and move. Circles indicate Mag- $\mu$ Bot starting position. Total experiment time is 43 sec. Noise and dust were digitally removed from frames for clarity. Videos are available at [18].

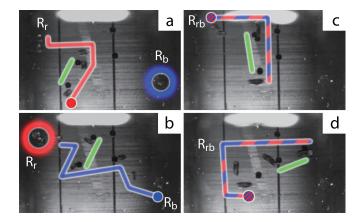


Fig. 6. (Color online) Frames from a movie with two Mag- $\mu$ Bots,  $R_r$  (red) and  $R_b$  (blue), manipulating 230  $\mu$ m PS-DVB microspheres (green) under silicone oil. In (a)  $R_b$  is anchored and  $R_r$  pushes a microsphere upwards, in (b)  $R_r$  is anchored and  $R_b$  pushes a microsphere upwards after failing to push a stuck microsphere, in (c) the two Mag- $\mu$ Bots assemble to form  $R_{rb}$  and push a microsphere downwards, and in (d)  $R_rb$  pushes the previously stuck microsphere to the right. Circles indicate Mag- $\mu$ Bot starting position. Total experiment time is 50 sec. Videos are available at [18].

## V. CONCLUSIONS

In this study, we demonstrate that multiple untethered magnetic micro-robots with dimensions  $230 \times 130 \times 100 \ \mu m^3$  can move both in parallel, and individually with decoupled motion. This capability was enabled by an array of 16 independent electrostatic anchoring pads on the substrate. Pushing of microspheres was also demonstrated within a fluid with two Mag- $\mu$ Bots, and is a step towards team-based micron-scale soccer for the RoboCup Nanogram League.

Models describing the electrostatic forces were given to quantify the anchoring behavior of the electrostatic pads on a Mag- $\mu$ Bot, and experimental results displayed the required electrostatic voltages. Models for estimating the required force to push microspheres are also presented.

Future works will include incorporating vision and path planning algorithms to autonomously control multiple Mag- $\mu$ Bots to perform tasks such as microparticle assembly. Mag- $\mu$ Bots with lower magnetization will also be investigated to decrease jump-into contact distances and allow disassembly.

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