6 DoF SLAM using a ToF Camera: The challenge of a continuously growing number of landmarks

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Abstract—Localization and mapping are fundamental problems in service robotics since representations of the environment and knowledge about the own pose significantly simplify the implementation of a series of high-level applications.

ToF (time-of-flight) cameras are a relatively new kind of sensors in robotics. They enable the real-time capture of the distance and the grayscale information of a scene. Due to the increase of the image resolution of ToF cameras, now highlevel computer vision algorithms for visual feature extraction (e.g. SIFT [1] or SURF [2]) can be applied to the captured images. These visual features combined with the corresponding distance information give a full measurement of 3D landmarks.

An obvious problem to be solved is the continuously growing number of landmarks. So far, *all* ever seen landmarks are just accumulated irrespective of their utility and the then required resources. Rather, one should keep only really useful landmarks, e.g. such that localization quality in the whole operational area is kept above a given threshold. In fact a lifelong running SLAM approach is dependent on means to select and discard landmarks. That is even more acute in case of feature-rich sensor data as provided with high update rates by sensors like a ToF camera.

We run our SLAM approach in a real-world experiment within an indoor environment. The experiment was performed on a P3DX-platform equipped with a PMD CamCube 2.0 and a Xsens IMU.

I. INTRODUCTION

Localization and mapping are fundamental problems in service robotics since representations of the environment and knowledge about the own pose are crucial for a series of high-level applications.

Especially in 3D SLAM, the requirements on the sensors are high. ToF cameras provide a good performance on capturing 3D scenes. They are able to simultaneously capture distance and grayscale images with high frame rates. The compact size and low power consumption makes them suitable for use in robotics.

Service robots should be designed for life-long and robust operation in dynamic environments. However, SLAM approaches typically just accumulate landmarks over time and do not discard them anymore. Therefore, each newly recognized landmark is added to the state vector which results in a growth of the state vector size without an upper bound. In case of bounded resources, one thus needs a mechanism to keep only the best landmarks. The SLAM problem thus needs to be extended such that one selects those landmarks that ensure a certain localization quality within the working environment of the service robot. The other landmarks can be marked for deletion.

In this paper we present an approach to fuse ToF camera data and 3D odometry for feature-based 6 DoF SLAM. The focus lies on the validation of landmark measurements in ToF images as well as on the data association part. The problem of ever growing number of landmarks is handled by a landmark rating and selection process. It selects landmarks in such a way that they best cover the working environment for localization purposes.

II. RELATED WORK

Well known sensors for 3D scene recognition are stereovision systems. In weakly textured image regions it is not possible to detect the necessary correspondences in both images for computing the distances. Beder [3] compares stereo vision systems with a ToF camera for surface reconstruction tasks. He shows that the ToF camera outperforms the stereo vision system in case of distance measurements. Because the resolution of the ToF camera is lower, he suggests to fuse both kinds of cameras for surface reconstruction purposes.

Sabeti [4] proposes two Particle Filter based visual object tracker. One is based on time-of-flight range image data and the other one on 2D color camera data. He compares both to identify the advantages and drawbacks of the systems.

The potential of ToF cameras in mobile robotics is described by May [5]. First, he describes the influence of integration time and modulation frequency on the measurement quality and how ToF cameras have to be calibrated. Then a filter to determine inaccurate distance values is presented. In [6] May uses a ToF camera for indoor SLAM based on depth image registration. He discusses the error characteristics of ToF cameras in detail and suggests, methods for camera calibration. Several methods for registering real-world ToF camera data using ICP based algorithms are explained. Experiments in a indoor environment with a diagonal of 19.4m were reported. The trajectory forms a loop where 325 distance images are captured.

Prusak proposes an approach for pose estimation and map building using ToF camera and 2D CCD camera [7]. A combined Structure-from-Motion (SfM) and model-tracking approach is used for selflocalization. The ToF camera image is mapped into the 2D CCD image. The distance can be determined by using the pixel by pixel correspondence for every interest points. A KLT-tracker is used to track interest points in the 2D CCD camera image. This set of interest points is used for pose estimation.

An early approach using SIFT features as visual 3D landmarks for SLAM is presented by Se [8]. The 3D landmarks are extracted from stereo vision. Then the 3D landmark measurements and the 2D odometry data are fused in a Kalman Filter.

Landmark rating needs a measure for determining the benefit of a landmark for localization purposes. In [9], the observation region of a landmark together with the landmark pose uncertainty is used for defining a measure for the benefit of a landmark. DBSCAN clustering is used to identify regions in the environment with a high landmark density.

A quality measure to compute the best landmark out of a set of landmarks is also used by Dissanayake [10]. First, all landmarks are collected whose state changes in the current step from visible to invisible. From this set only the highest quality landmark is kept and all others are discarded. Thus, the selected highest quality landmark is a single representative for the set of previously visible landmarks. However, selection of landmark representatives is based on a local set of landmarks and thus depends on the exploration path and the resulting visibility sequence. There is still no global measure of landmark quality. Nevertheless, this is one of the rare approaches addressing landmark deletion with respect to a landmark's use in terms of observability.

A fundamentally different approach is proposed by Strasdat [11]. The presented approach uses Monte-Carlo Reinforcement Learning to learn landmark selection policies that optimize the navigation task. He demonstrates his approach in two scenarios. The first is a single goal navigation task. The second is a round-trip navigation task where subgoals are visited more than once. Due to the complexity of the learning algorithm and the number of training episodes, it is not feasible to learn these policies during real-world experimentation. Therefore, Strasdat recommends to learn the policies in simulation.

III. METHOD

This section starts with the description of the overall system. Then the used methods for the action and the sensing step of the Extended Kalman Filter (EKF) are explained in detail. Next, the approach used for the data association problem is presented. The data association problem is considered as the major problem in robust feature-based EKF SLAM approaches. Our proposed solution on handling the problem of the ever growing number of landmarks during SLAM is described at the end of this section.

The overall sequence of processing steps is shown in figure 1. Wheel encoder data (2D odometry) together with the inclinometer data are used to predict the relative 3D pose change of the mobile robot. In the sensing step 3D landmark measurements from the ToF camera are used. SURF features extracted from the intensity image of the ToF camera are used as salient and recognizable landmarks. The SURF feature position in the intensity image together with

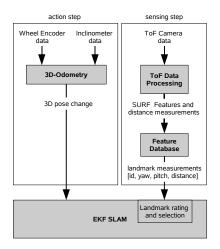


Fig. 1. The overall system for 6 DoF SLAM

the distance measurement describes a full 3D measurement in spherical coordinates. The observed SURF features are compared with those from the previously observed ones in the feature database. A SURF feature of the current scene is considered as not matching an already known landmark, if the comparison of the descriptors by a Chi-square test is above a given threshold. In this case, the SURF feature gets a new and unique identifier. Otherwise, the SURF feature is considered as matching an already known landmark and therefore gets the unique identifier of the recognized landmark. Both, the predicted relative pose change (3D odometry) and the data from the sensing step are then fused in the EKF to estimate the 6 DoF pose of the mobile robot and the 3D landmarks in the map.

A. Full 6 DoF EKF-based Bearing-Range SLAM

A tremendous amount of frameworks for SLAM algorithms have been developed and published in the recent years [12], [13]. Most of them provide basic algorithms to solve the SLAM problem with probabilistic methods, like Kalman Filter, Extended Kalman Filter and Particle Filter. Our approach is based on the Range-Bearing SLAM algorithm of Blanco [14]. This efficient implementation is used in the Mobile Robot Programming Toolkit (MRPT) [13] and has a complexity of $O(N^2)$. The state vector contains the vehicle pose as well as all landmarks.

$$x = [x_v, y_1, y_2, y_3, \dots, y_L]^T$$
(1)

The vehicle pose $x_v = [x_v, y_v, z_v, \phi_v, \chi_v, \psi_v]$ is the position in 3D Cartesian coordinates and the three orientation angles. Every landmark $y_i = [x_i, y_i, z_i]$ is represented by its 3D coordinates in the map.

1) 3D Odometry: Typical wheel encoder based odometry provides pose information in 2D (x, y, ϕ) . The 3D odometry approach presented in [15] and [16] extends the 2D odometry to 3D by using inclinometer data for pitch (χ) and roll (ψ) . In case we use 3D landmarks, even ground vehicles in indoor environments require 3D odometry due to ramps or inclined planes. 3D odometry can be achieved by fusing

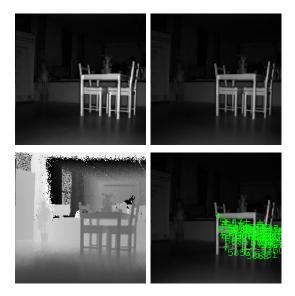


Fig. 2. ToF camera data captured during an experiment. The amplitude image is shown on the upper left and the intensity image on the upper right. On the lower left the distance image is shown. Near measurements are displayed dark and distant measurements are displayed bright. Remaining SURF features after the accuracy determination process are displayed with their identifier on the lower right image.

wheel encoder data (2D odometry) and *pitch* and *roll* angles from the inclinometer. Hence, the control vector u_k is defined as $u_k = [x_u, y_u, z_u, \phi_u, \chi_u, \psi_u]$, where $x_u = \Delta x, y_u = \Delta y, \phi_u = \Delta \phi$ are the relative pose change measured by the 2D odometry. $\Delta \chi_u$ and $\Delta \psi_u$ are determined by the inclinometer. Since we never have a control input in zdirection, we set $z_u = 0$.

With this assumption the relative pose can be computed by incorporating the previous 3D odometry data and the current control vector (relative pose change). Blanco uses in [14] the following motion model:

$$x_{v_k} = f_v(x_{v_{k-1}}, u_k) = x_{v_{k-1}} \oplus u_k \tag{2}$$

with, \oplus denoting the pose composition operator [17]. A detailed derivation and description of the motion model can be found in [14].

2) 3D Landmarks: In our approach we use 3D landmarks extracted from ToF camera data in the sensing step of the EKF. ToF cameras are able to simultaneously capture distance and grayscale images. More precisely the PMD CamCube 2.0 provides two kinds of grayscale images. The intensity image is a 2D grayscale image, as produced by a 2D CCD camera. The second image is the amplitude image which contains the signal strength of the active illumination for every pixel. Figure 2 shows those images captured during an experiment.

Image processing with ToF camera data is challenging, because the active illumination of the scene by the PMD camera results in an inhomogeneously illuminated image. The low amount of reflecting light leads to noisy distance measurements.

SURF features [2] are used as visual landmarks. They are robust against changing lighting conditions. An additional advantage of SURF features is the high discriminability between the features.

In the ToF data processing step, we first extract the SURF features from the intensity image. For every extracted SURF feature the accuracy of the distance measurement is determined. Features with low corresponding distance accuracy are removed. The accuracy of the distance measurements depends on the amount of received light. A method for distance measurement accuracy determination is proposed by May [5]. He mentioned that photonic interference is the main reason for inaccuracy. The relation between the inaccuracy and the photonic interference is defined in [18]. The inaccuracy ΔL is computed by the following equation:

$$\Delta L = \frac{L}{\sqrt{8}} * \frac{\sqrt{I}}{2 * A} \tag{3}$$

L is the maximum measurement distance of the sensor, A the amplitude value and I the intensity value of the corresponding pixel. The distance accuracy threshold for ΔL was set to 0.3. Thus, all measurements with $\Delta L > 0.3$ are removed. After accuracy thresholding, the remaining SURF features are compared with those from the feature database. A SURF feature is considered matching an already known landmark if the descriptors are similar. It is associated with the unique identifier of the recognized landmark. To compare the descriptors, a Chi-square test is applied. A result of $\chi^2 < 0.3$ is considered as match of the SURF features. In this case the new observed feature gets the same identifier as the already known one. In the other case, the new observed feature gets a new identifier. The observation model comprises the robot pose x_v and the landmark measurement $z_k = [r, \alpha, \beta]$ in spherical coordinates. Since, the resolution $(204px \times 204px)$ and the field of view of the sensor is known ($40 deg \times 40 deg$), the angles α and β depend only on the position of the SURF feature in the intensity image. The corresponding distance measurement is stored in the corresponding position in the distance image. A detailed derivation and description of the used observation model can be found in [14].

B. Data Association

A match for an observed feature is based solely on the similarity of the descriptors of the landmarks so far. Until now, there is no validation of the spatial plausibility of the pose of the matched landmark done. However, the EKF provides additional information about expected observation poses. Costa proposes in [19] to use a Chi-square test for data association. The Chi-square test takes into account the measurement uncertainty and the uncertainty of the robot pose. In the following equations the Chi-square test is defined:

$$r_i = z_i - \hat{z}_i \tag{4}$$

$$S_i = \mathbf{H}\mathbf{P}\mathbf{H}^T + R \tag{5}$$

$$\chi^2 \geq r_i^T \mathbf{S}^{-1} r_i \tag{6}$$

In equation 4, r_i is the difference between the estimated measurement \hat{z}_i and the observed measurement z_i of the

landmark at index *i*. S_i in equation 5 is the residual covariance which is calculated by multiplying the system covariance matrix with the Jacobian matrix **H** and the transpose of the Jacobian matrix. After transforming the covariance matrix into the measurement space the sensor noise covariance matrix **R** is added. The Jacobian matrix **H** is defined by the following equation

$$\mathbf{H} = \begin{bmatrix} \mathbf{H}_{\mathbf{R}} & 0 & \dots & 0 & \mathbf{H}_{\mathbf{L}_{\mathbf{i}}} & 0 & \dots & 0 \end{bmatrix}$$
(7)

 $\mathbf{H}_{\mathbf{R}}$ is the Jacobian of the transition model and $\mathbf{H}_{\mathbf{L}}$ is the Jacobian of the observation model.

$$\mathbf{H}_{\mathbf{R}} = \frac{\partial f}{\partial x} \tag{8}$$

$$\mathbf{H}_{\mathbf{L}} = \frac{\partial h}{\partial x} \tag{9}$$

The motion model is denoted by f and the observation model by h. The position of H_L in H corresponds to the index of the landmark in the state vector.

The right part of equation 6 describes the squared Mahalanobis distance [20]. For Gaussian distributions the Mahalanobis distance follows the Chi-square distribution. The threshold for the Chi-Square test can be obtained from a Chi-square table. Our system have three degrees-of-freedom. For a confidence value of 90% to associate a measurement to a landmark, the value for χ^2 obtained from table lookup is 0.5844.

C. Landmark rating and Selection

The basic approach for landmark rating and selection is presented in [9] and is integrated into the SLAM mechanism (see figure 1). It can be used with all kinds of feature-based EKF SLAM approaches. In previouse work the approach is used in 3DoF SLAM here in the 6DoF case we only have to extend the viewpoint location estimation from 2D to 3D. The sensing step keeps track of the set of robot poses from which a landmark has been observed so far. This provides the basis for describing from where in the environment a certain landmark is observable. This information provides then the basis for evaluating the benefit of a landmark for localization purposes. At every time step the approach determines the map quality by calculating the viewpoint location and the information content [10] of every landmark.

Removing a landmark from a region with high localization support results in a small degradation of robot localization quality only. Clustering algorithms are used to identify regions in the environment with a high landmark density. DBSCAN clustering [21] is especially suitable to determine those regions. The algorithm typically constructs clusters around local dense maxima, separated by regions of low density. The algorithm does not need to know the number of clusters in advance. A further advantage is the efficiency (O(n*log(n))) of the algorithm, equal to K-means [21] [22]. Removing landmarks within low density regions is critical. Relocalization in these regions using those landmarks is difficult. All viewpoint locations with a distance greater Epsto the Eps-neighborhood are considered as outliers. Outliers are not part of a cluster and are thus never removed.



Fig. 3. The real world experiment is performed in the whole ZAFH laboratory with a room-size of $15m \times 9m$.



Fig. 4. Pioneer 3DX platform equipped with embedded PC, Xsens IMU and ToF Camera (PMD CamCube 2.0)

IV. RESULTS

A. Experiment Setup

In this section, the results of the experiments are discussed in detail. The performance is demonstrated within a standard indoor environment by means of a real-world experiment. The experiment has been performed in our lab with a size of $15m \times 9m$ (see figure 3) partly with moving people in the scene. We have not taken any precautions to avoid specular reflections and surfaces with low reflectivity.

The experiments are performed on a P3DX-platform (see figure 4) with the above described feature-based 3D SLAM approach.

The resolution of the ToF camera (PMD CamCube 2.0) is $204px \times 204px$ and the field of view $40deg \times 40deg$. Therefore the angular resolution is 0.1961deg. The repeatability of distance measurements defined by the manufacturer is < 3mm at 2m distance and 90% reflectivity. To measure the pitch and roll inclination an Xsens IMU is used. The static accuracy of the pitch and roll measurements is 0.5deg and the dynamic accuracy 2deg RMS.

The parameters of the motion model are $(0.03m)^2/1m$ error for change in position $(\Delta x, \Delta y, \Delta z)$ and $(3deg)^2/360deg$ angular error for $\Delta \phi \ \Delta \chi$ and $\Delta \psi$. The observation model uses $(0.05m)^2$ as distance error (σ_r^2) and $(0.3deg)^2$ as angular errors $(\sigma_{\alpha}^2, \sigma_{\beta}^2)$ of the landmark observation.

The clustering algorithm constructs clusters around local dense maxima, separated by regions of low density. All viewpoint locations with a distance greater Eps = 0.2m to the Eps-neighborhood belong to a cluster. Every cluster needs at least 4 viewpoint locations. Otherwise the viewpoint

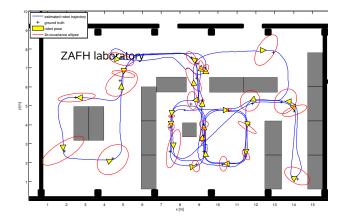


Fig. 5. The estimated trajectory in the environment is plotted with a blue line. For visualization purposes, we project the 3D robot pose onto the 2D plane and place a floor plan in the background. The gray objects are tables. The yellow triangles represent the robot with the 2σ covariance ellipse (red). For these robot poses the corresponding ground truth positions are marked with a black cross.

locations are considered as outliers.

B. Localization Quality

The localization quality directly depends on the quality of the landmarks and their distribution over the operational area. As can be seen from figures 5, 7 and 8 the achieved overall localization quality is still within a range suitable for service robotic tasks. Figure 8 illustrates the localization error against ground truth measurements. The error value plotted there is the Euclidean distance from the ground truth measurement to the mean of the robots state estimation. Due to the lack of GPS/DGPS in indoor environments, it is quite hard to get the ground truth position of the robot. We solve the problem of determining the ground truth position by measuring manually the distance from the robot towards two a priori known coordinates in the environment with a Bosch Digital Laser Rangefinder (DLE 150). The 2σ value of our ground truth poses is $[0.06m^2, 0.04m^2]$.

The trajectory shown in figure 5 contains 1401 time steps and has a length of approximately 124m with an average step width of 0.09m. During the run, the robot closes multiple loops with a length of approximately 6m to 17m each. The result after the experiment is a consistent map and a high positioning accuracy of the robot.

Figure 6 shows all map objects at time step 1401. The landmarks in the state vector are plotted with the corresponding 2σ covariance ellipsoid (blue). The red colored ellipsoid visualizes the robot pose covariance (2σ). The robot coordinate system origin is represented as a X,Y,Z (red, green, blue) 3D corner. This marks the start position of the experiment.

In Figure 7 uncertainty of the robot pose estimation is visualized by plotting the eigenvalues of the robot position covariance matrix during the complete run. The plot in the figure clearly indicates the decrease of uncertainty after every loop closing.

A common method to evaluate the SLAM approach is

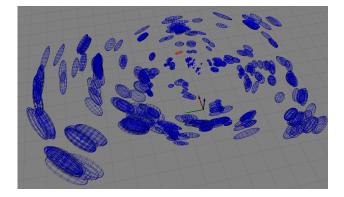


Fig. 6. 3D scene of the estimated map at time step 1401 with robot pose, the corresponding 2σ covariance ellipsoid (red) and the landmarks with their 2σ covariance ellipsoid (blue). The three arrows designate the origin of the robot coordinate system (x,y,z : red, green, blue). Every square on the ground plane is of size $1m \times 1m$.

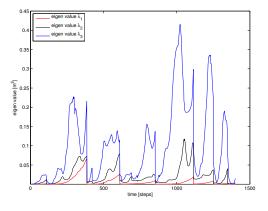


Fig. 7. Eigenvalues of the robot position covariance matrix during the run.

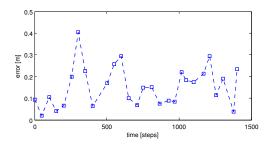


Fig. 8. Localization error against ground truth.

the comparison of the estimated robot pose against ground truth. During the experiment, we made 28 ground truth measurements. The Euclidean distance from the estimated robot pose to the ground truth measurement is shown in figure 8. If we compare the localization error in figure 8 with the estimated pose uncertainty in figure 7, we can see that time steps with a large distance to ground truth correlates with the time steps with a high pose uncertainty. After loop closing, the localization error and the pose uncertainty decrease.

C. Landmark coverage quality

The landmark coverage of the environment is, as previously mentioned, a crucial factor for the relocalization

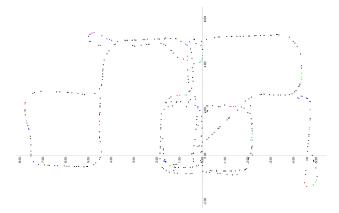


Fig. 9. Landmark clustering using DBSCAN based landmark rating and selection process after 1366 time steps.

capability. If the landmark reduction algorithm removes all landmarks from one area, relocalization within this area will be difficult. The applied landmark rating and selection algorithm leads to a well distributed landmark coverage over the operational area, as illustrated in figure 9. The figure shows the clusters of viewpoint locations of landmark observations. A viewpoint location is the position from where a landmark can be observed. All representatives belonging to a cluster (spatial closeness) are drawn with the same color. Recurrent color labels for different clusters are an illustration artifact. Using the landmark rating and selection process, only 519 landmarks are kept. If the number of landmarks would not have been reduced, the number of landmarks would have grown beyond 20000 in this experiment.

V. CONCLUSIONS AND FUTURE WORK

ToF cameras are appropriate sensors for feature-based 3D SLAM, especially since the image resolution now is high enough to apply, high-level image processing algorithms. In this work, we show that 6 DoF feature-based EKF SLAM performs well with ToF cameras. Whereas a reduced number of landmarks were used, the proposed approach covers the operational area with landmarks in such a way that a certain localization quality is achieved in the whole map. Furthermore our approach allows to distinguish between static and dynamic landmarks, by evaluating the expected landmark observations.

Since, the PMD CamCube can be used for indoor and outdoor (PMD CamCube SBI mode), future work will evaluate the performance of the approach in mixed indoor and outdoor environments. Our landmark rating and selection approach is independent of any special types of landmarks, other types or combinations of landmarks will be evaluated in future work.

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