

Simplified Human Hand Models based on Grasping Analysis

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Abstract—The purpose of this paper is to analyze in some depth the kinematic behaviour of the human hand, in order to obtain simplified human hand models with the minimum and optimal number of Degrees of Freedom (DoF), and thus achieving an efficient manipulation task. The statistical analysis is carried out using Principal Components Analysis (PCA). Power and precision grasps are obtained with the use of a Cyberglove and a human hand model with 24 DoF. Finally, these experiments are used to evaluate the best DoF for an appropriate manipulation.

I. INTRODUCTION

THE main objective of this work is to use simplified human hand models for cooperative manipulation tasks through human interfaces and teleoperated systems in virtual scenarios.

One difficulty in understanding human hand control is the large number of degrees of freedom (DoF) involved. The high dimensionality of the control space also explains the difficulty on creating effective control algorithms for all human hand models or robotic hands with more than 20 DoF. The purpose of this paper is to determine what DoFs are the most important for controlling a hand model or robotic hand based on grasping analysis. The best simplified hand model depends on the requirements of the task, in this case, the degree of realism, the maximum error produced on the reconstruction and the number of controlled inputs in the hand control performance would have to be considered for a particular task.

The base of all simplified human hand models is a kinematic model with 24 DoF that reasonably satisfies realism in simulation [1], [2]. This kinematic model is used for reconstructing simplified hand models with less DoF. The kinematic analysis of the human hand is focused in the role played by the behaviour of the grip in order to decide the more adequate simplified hand model for a particular manipulation.

Principal Component Analysis (PCA) has been used previously on hand poses such as [3], [4], and [5]. By means

of PCA [6], an experiment was done with 200 samples in order to obtain five principal components. These samples were obtained using a Cyberglove® [7] and a model of the human hand with 24 DoF with objects of different sizes. Therefore, a significant simplification is thus made to the original hand description, as the 24 components are reduced to 5 components.

Cyberglove is also used to read the most important degrees of freedom for reconstructing simplified hand models using inter-finger and intra-finger constraints [8].

Also, this paper is focus in evaluate simplified hand models within a dimensionality reduction [9], [10], [11], [12]. The simplified hand models are evaluated, with regard the hand model of 24 DoF using multi-body dynamics engine.

This paper is organized in the following way: Section II describes briefly the kinematic model of the human hand, Section III describes the statistical study to analyze the kinematic grasp behaviour, Section IV describes simplified human hand models, and Section V experiments and results. Finally, conclusions are presented in section VI.

II. KINEMATIC MODEL OF THE HUMAN HAND

The hand model used for this work is based on the human skeleton. The kinematic model is comprised of 19 links that imitate the corresponding human bones, and 24 degrees of freedom (DoF) that represent the joints. Links and joints are defined by L_{ij} and θ_{ij} , where i represents a finger ($i =$ Thumb, Index, Middle, Ring or Little) and j its corresponding link or joint respectively. Two kinematic configurations are considered in this hand model, one for the thumb and another for the rest of the fingers. Therefore, the same kinematic configuration is used for the index, middle, ring and little fingers. This configuration is defined by 5 joints and 4 links: metacarpal ($L_{i,Me}$), proximal ($L_{i,P}$), middle ($L_{i,Mi}$) and distal ($L_{i,D}$) links. The joints are defined as: carpometacarpal ($\theta_{i,CMC}$), proximal interphalangeal ($\theta_{i,PIP}$) distal interphalangeal ($\theta_{i,DIP}$) and metacarpophalangeal, which is modelled by a universal joint (2 DoF) that defines the abduction/adduction (θ_{i,MCP_aa}) and flexion/extension (θ_{i,MCP_fe}) rotations. The thumb is modelled by 4 DoF and 3 links: metacarpal ($L_{T,M}$), proximal ($L_{T,P}$), and distal ($L_{T,D}$). The thumb joints are defined as: metacarpophalangeal (θ_{T,MCP_fe}), interphalangeal ($\theta_{T,IP}$) and trapeziometacarpal, which is also defined by a universal joint that defines the abduction/adduction (θ_{T,TMC_aa}) and flexion/extension (θ_{T,TMC_fe}) respectively. The rest of the joints are modelled by revolute joints. Forward kinematics and inverse kinematics are described in more detail in S. Cobos et al. [3].

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III. PCA ANALYSIS

The PCA analysis was carried out using a data base from 200 samples. These samples were obtained through Cyberglove and hand model with 24 DoF, thus having a collection of virtual gestures by means of handling real objects. The type of grasps produced are: prismatic precision, prismatic power, circular power and circular precision (figures 1.a to 1.e), with objects of different sizes. This procedure performs a principal components analysis using the covariance matrix. The purpose of the analysis is to obtain a small number of linear combinations of the 24 variables which account for most of the variability in the data. In this case, 5 components are extracted as requested. Together, the 3 Principal Components account for $\sim 88.4\%$ of the variability in the original data. Therefore, these functions represent a new compressed 5-dimension of the 24 DoF that have been used to model the hand gesture.

The purpose of this analysis is to identify if it is feasible reducing the degrees of freedom and to identify the most important degrees of freedom for the reconstruction of a specific grasp (power or precision). In other words, how many fingers and DoF are required for the reconstruction of the gestures according to Cutkosky classification [13]?

By means of PCA, it is possible to identify how many variables are required to represent the information of the 24 DoF. Therefore, PCA was used to identify the effective degrees of freedom more precisely.

TABLE I
DEGREES OF FREEDOM MOST IMPORTANT FOR POWER AND PRECISION GRASP FROM THE PRINCIPAL COMPONENT ANALYSIS

Finger	Joint	Symbol
Thumb	Trapeziometacarpal abduction/adduction	θ_{T,TMC_aa}
Thumb	Trapeziometacarpal flexion/extension	θ_{T,TMC_fe}
Index	Metacarpophalangeal abduction/adduction	θ_{I,MCP_aa}
Index	Proximal Interphalangeal	$\theta_{I,PIP}$
Middle	Metacarpophalangeal flexion/extension	θ_{M,MCP_fe}
Middle	Proximal Interphalangeal	$\theta_{M,PIP}$
Ring	Metacarpophalangeal flexion/extension	θ_{R,MCP_fe}
Ring	Proximal Interphalangeal	$\theta_{R,PIP}$
Little	Metacarpophalangeal flexion/extension	θ_{L,MCP_fe}
Little	Proximal Interphalangeal	$\theta_{L,PIP}$

The kinematic analysis of hand postures for grasping objects showed that a considerable reduction of the degrees of freedom is permissible. In particular, the 5 principal components demonstrate that 88.4% of the variance can describe the five principal gestures considered in this analysis. In order to obtain the most relevant degrees of freedom, the weight component, and standard components (rescaled components) of each component are used. The 10 degrees of freedom most important are obtained by applying a weighted standardization over the weight component, and standard components. Table I and figure 2 show the degrees of freedom most important. Therefore, one interpretation of these findings in terms of gesture reconstruction is that one flexion of all fingers and the abduction/adduction for thumb and index fingers must be considered important variables. Figure 2 shows in red colour the most important degrees of freedom and the less important degrees of freedom in blue colour.

On the other hand, the least significant degrees of freedom are the carpometacarpal (CMC) joints. Comparing the weights between the four CMC, the most important CMC joint is the CMC of the Little finger ($\theta_{L,CMC}$).

Flexion is strongly related in all fingers. Therefore, the chosen flexion could be θ_{I,MCP_fe} , $\theta_{I,PIP}$, or $\theta_{I,DIP}$ joints for index, middle, ring and little fingers and θ_{T,TMC_fe} , θ_{T,MCP_fe} , or $\theta_{T,IP}$ for the thumb. The results of the analysis show that the middle finger, the ring finger and the little finger have 2 very relevant flexions. The possibility to choose among any of the 2 flexions for these fingers is given by the strong relation that exists among the 3 flexions. Any of these flexions can be represented as a lineal combination of the other 2 flexions. Finally, the analysis shows that the 3 most important abductions are: θ_{T,TMC_aa} , θ_{I,MCP_aa} and θ_{L,MCP_aa} .

IV. SIMPLIFIED HUMAN HAND MODELS

This section describes simplified human hand models that properly represent the kinematic behaviour of the human hand in accordance with the precision and application required. The human hand model of 24 DoF is used as a basis for comparison among simplified hand models with fewer degrees of freedom than the 24 DoF of the hand model described in section 2.

Kinematic constraints are used in order to obtain simplified hand models (SHM), which allow reducing the number of independent variables or joints in the original model. In other words, with few independent variables it is possible to reconstruct a gesture of 24 degrees of freedom with an acceptable error with respect to the original gesture of 24 degrees of freedom not reconstructed. Simplified human hand models are obtained using dependent and independent variables; these dependent variables or dependent joints are calculated using kinematic constraints.

The reduction of elements from 13 to 1 DoF leads to increasingly rely on interpolations and constraints associated with an increased error in the grip trajectory when the dependent variables are obtained.

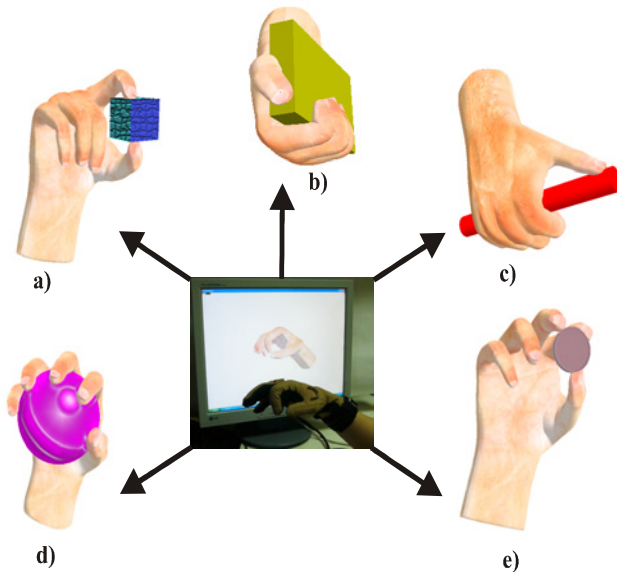


Fig. 1. Grasp rendering of various objects using a Cyberglove and a hand model with 24 DoF. a) Prismatic Precision, b) Heavy Power, c) Prismatic Power, d) Circular Power and e) Circular Precision.

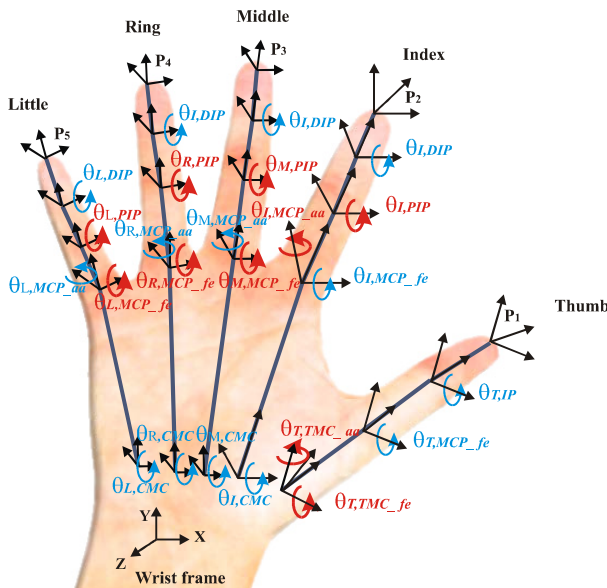


Fig. 2. Degrees of freedom most important obtained with principal component analysis.

Somehow, this technique depends on optimizing the functionality of a particular inter-finger or intra-finger constraint.

Many manipulations involve similar movements among fingers, e.g., a gesture done with the information of five fingers can be simplified by using only the information provided for three fingers. In this case, these three fingers can be thumb, index and ring, creating the same movement for the middle finger through the information of the index and the little finger through the information of the ring finger.

The simplified hand models should be used depending on the relation between the number of degrees of freedom and the allowed error in the application.

The degree of dexterity that can be achieved depends mainly on the largest number of independent variables having thumb and index finger inside the SHM. The abduction/adduction of the thumb and index finger is very important because at least one degree of freedom from these fingers is considered as an independent variable in all the simplified hand models, thus the flexion of the proximal interphalangeal (PIP) joint of the index finger is included in all the simplified hand models.

The abduction/adduction of the thumb Trapeziometacarpal (TMC) joint is important because with a flexion of the interphalangeal (IP) joint can produce the opposition of the thumb with the other fingers. In summary the universal joints of the thumb and index fingers are very important for obtaining simplified hand models because of the information they provide.

Finally, SHM have been used for manipulated power and precision grasps in a virtual environment. The scenario has been performed integrated a collision and dynamics libraries.

A. Simplified hand models from 1 to 6 degrees of freedom

To control a gesture with one degree of freedom has been demonstrated previously in a robotic hand e.g. The Tuat/Karlsruhe Hand [14]. This hand is designed with 24 joints and 1 DoF controlled, and it is able to do circular power grasps.

In general, models from 1 to 6 DoF are appropriate for power grasps with security and stability in the grip without achieving a great precision and skill in handling for precision grasps. In this category the models from 1 to 3 are capable of performing circular power grasps and models from 4 to 6 are capable of performing circular and prismatic power grasps.

The most important flexion was the PIP joint, as resulted in the PCA analysis. The reading or extraction of the information provided from this joint is only possible with a Cyberglove. For a haptic application this is not feasible, because in order to read some degree of freedom of a human hand, it can be done with the fingertips. For this reason, for a haptic application [15], [16] the distal interphalangeal (DIP) joints and the IP joint are ideal for independent joints.

Table II shows the degrees of freedom used to perform a manipulation for circular power grasps. Figures 3a) and 3b) show two examples of SHM with 3 and 6 DoF respectively for a Cyberglove interface.

The Barret Hand [17] is a good example to compare SHM with 4 DoF from the thumb finger, index finger and little finger. The barret hand is composed by three fingers, four servomotors and 7 joints. Both hands are used to do power handling tasks.

TABLE II
DEGREES OF FREEDOM FOR SHM FROM 1 TO 6 DoF

DoF	Independent Joints
1	$\theta_{I,PIP}$
2	$\theta_{I,PIP}, \theta_{T,TMC_aa}$
3	$\theta_{I,PIP}, \theta_{T,TMC_aa}, \theta_{T,TMC_fe}$
4	$\theta_{I,PIP}, \theta_{T,TMC_aa}, \theta_{T,TMC_fe}, \theta_{I,MCP_aa}$
5	$\theta_{I,PIP}, \theta_{T,TMC_aa}, \theta_{T,TMC_fe}, \theta_{I,MCP_aa}, \theta_{M,PIP}$
6	$\theta_{I,PIP}, \theta_{T,TMC_aa}, \theta_{T,TMC_fe}, \theta_{I,MCP_aa}, \theta_{M,PIP}, \theta_{L,PIP}$

B. Simplified hand models from 9 to 14 degrees of freedom
Greater precision and dexterity is derived from 9 degrees of freedom, thus it is possible to carry out precision grasps. Simplified hand models of 9 to 14 DoF are more precise for both types of grasp: precision and power grasps.

These SHM models are capable of performing the four types of grasps: circular power, prismatic power, circular precision and prismatic precision. Table III shows the degrees of freedom for reconstructing models from 9 to 14 DoF. Figures 4a) and 4b) show two examples of SHM with 9 and 14 DoF respectively for a Cyberglove interface.

In this classification, four robotic hands can be compared with SHM of 9 DoF, 11 DoF, 13 DoF and 14 DoF. The Stanford/JPL Hand [18] is composed by three fingers, and 9 DoF controlled. The Okada hand [19] has 11 DoF controlled. The DLR hand [20], [21] is composed by four fingers, and 13 DoF controlled. The Robonaut hand [22] is composed by five fingers, and 14 DoF controlled. These hands are used to do precision handling tasks.

TABLE III
DEGREES OF FREEDOM FOR SHM FROM 9 TO 14 DoF

DoF	Independent Joints
9	$\theta_{I,PIP}, \theta_{T,TMC_aa}, \theta_{T,TMC_fe}, \theta_{I,MCP_aa}, \theta_{M,PIP}, \theta_{L,PIP}, \theta_{R,PIP}, \theta_{L,MCP_aa}, \theta_{L,CMC}$
10	<i>SHM 9 DoF</i> + θ_{I,MCP_fe}
11	<i>SHM 10 DoF</i> + θ_{T,MCP_fe}
12	<i>SHM 11 DoF</i> + θ_{M,MCP_fe}
13	<i>SHM 12 DoF</i> + θ_{R,MCP_fe}
14	<i>SHM 13 DoF</i> + θ_{L,MCP_fe}

C. Simplified hand models from 15 to 24 degrees of freedom

A higher level of realism and sensitivity is achieved with models from 15 to 24 DoF. Only the model with 24 DoF is capable of performing simulation with arc palm deformation.

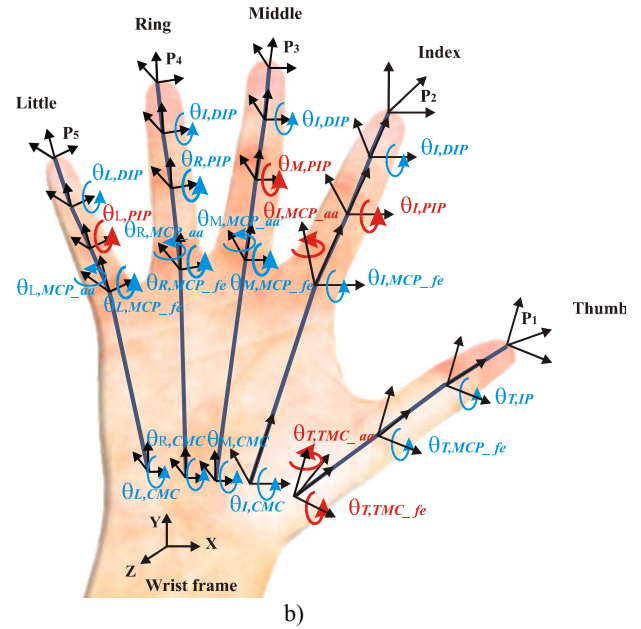
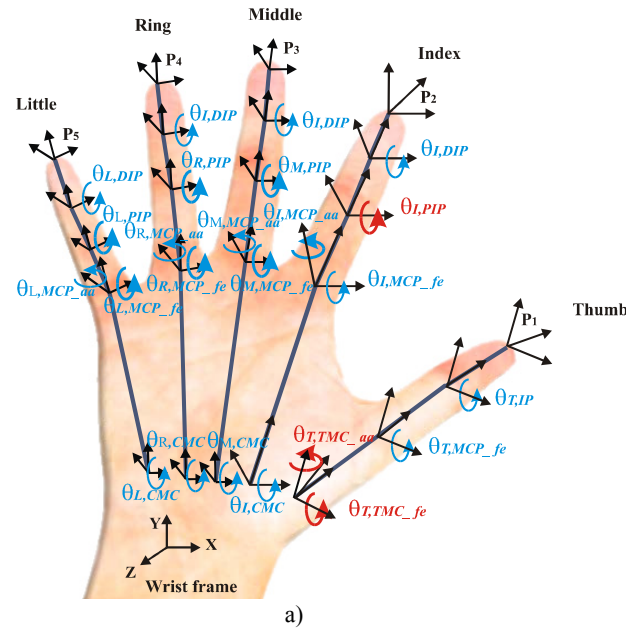


Fig. 3. Simplified hand model for power grasps a) Simplified hand model with 3 DoF b) Simplified hand model with 6 DoF.

With 15, 16 and 17 DoF is possible to have the 3 important flexions for index, thumb and middle fingers. All this information helps carrying out precision grasps with great realism. Table IV shows the degrees of freedom for reconstructing models from 15 to 24 DoF.

These models serve for applications that require a greater realism, sensitivity in handling or description of a human hand gesture. The integration of these models in a haptic application should be computationally expensive, depending on the task that it is required to manipulate and the amount of data for calculating in real time.

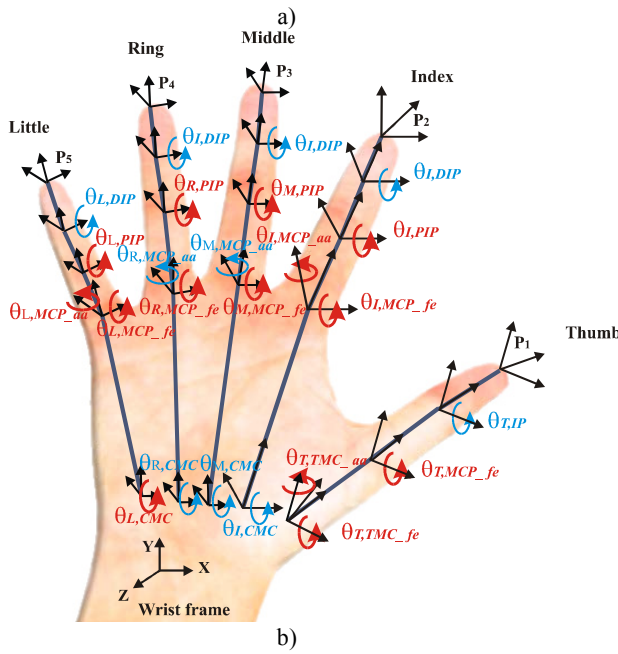
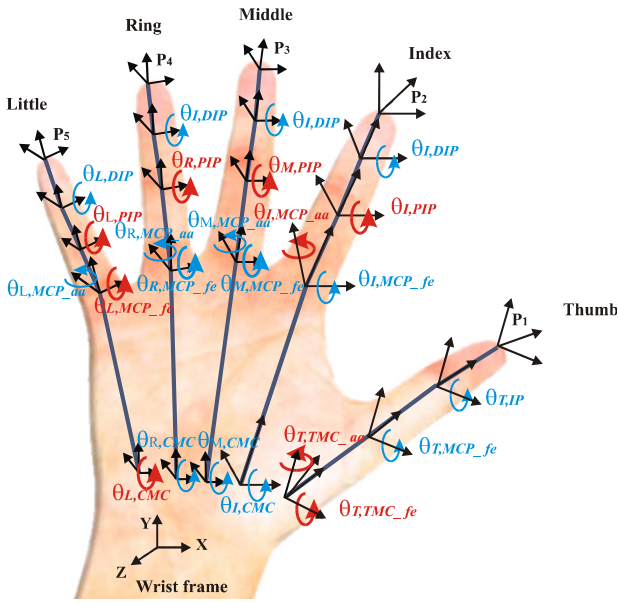


Fig.4. Simplified hand models for Power and Precision grasps. a) Simplified hand model with 9 DoF b) Simplified hand model with 14 DoF.

Finally, in this classification the SHM of 16 DoF and 24 DoF can be compared with two robotic hands. The Gifu Hand [23] is composed by five fingers, and 16 DoF controlled. The Shadow Dexterous Hand [24] is driven by 40 Air Muscles mounted on the forearm with 22 DOF for the fingers and 2 DoF for the wrist. These hands are used to do dexterous handling tasks.

V. EXPERIMENTS WITH SIMPLIFIED HAND MODELS

Simplified hand models are developed with regards to the type of manipulation task, this manipulation characteristic depends on the trajectory carried out by the joints inside of

two movement spaces: circular and prismatic. Therefore, the SHM are evaluated in these two types of trajectories.

This section presents some experiments carried out with simplified hand models. SHM are evaluated by using multi-body dynamics software in order to manipulate virtual objects for force grasp and dexterity grasp, it involves grasping a circular or prismatic object, and retain a stable handling. The collision detection and computation times are measured for: 24 DoF hand model, SHM with 9 DoF and SHM with 6 DoF. The multi-body dynamics software used for this evaluation is: Chrono Engine Library [25]. All experiments were executing in an Intel Core 2 Quad CPU at 2.40 GHz under windows XP operative system.

Figures 5 and 6 contain a comparative graph among the computation times of each SHM. The data collection is obtained through 250 samples for circular and prismatic grasps. Each scenario was replicated 50 times so as to get a representative measurement of time. The following figures contain a comparative graph among the computation times of each SHM. A significant reduction on time calculation for collision detection between SHM with 24 DoF and SHM with 9 DoF such as shown in figure 5 can be observed.

Figure 6 shows the time used for collision detection in 24 DoF hand model, SHM with 9 DoF and SHM with 6 DoF for handling circular grasps. The SHM with 6 DoF was used for evaluating circular grasp handling. In figure 6, the difference in time that exists among 3 hand models can be seen. In this evaluation, prismatic grasp handling was evaluated between 24 DoF hand model and 9 DoF SHM because the 6 DoF SHM is develop just for circular grasp.

TABLE IV
DEGREES OF FREEDOM FOR SHM FROM 15 TO 24 DoF

DoF	Independent Joints
15	SHM 14 DoF + $\theta_{L,DIP}$
16	SHM 15 DoF + $\theta_{T,IP}$
17	SHM 16 DoF + $\theta_{M,DIP}$
18	SHM 17 DoF + $\theta_{R,DIP}$
19	SHM 18 DoF + $\theta_{L,DIP}$
20	SHM 19 DoF + θ_{R,MCP_aa}
24	SHM 20 DoF + $(\theta_{R,CMC}, \theta_{M,CMC}, \theta_{I,CMC}, \theta_{M,MCP_aa})$

VI. CONCLUSION

This paper presented simplified human hand models based on an important statistical analysis such as principal components. This study serves to determine what variables are the most important to take into account for two big spaces of grasping: power and precision grasps. The human role on grasping is considering by means of the abstraction of the human hand joints using a Cyberglove. These models with Number of DoF < 24 DoF are useful for diverse applications that require achieving an efficient handling

depending on the level of dexterity, stability, computational cost and realism required in handling tasks.

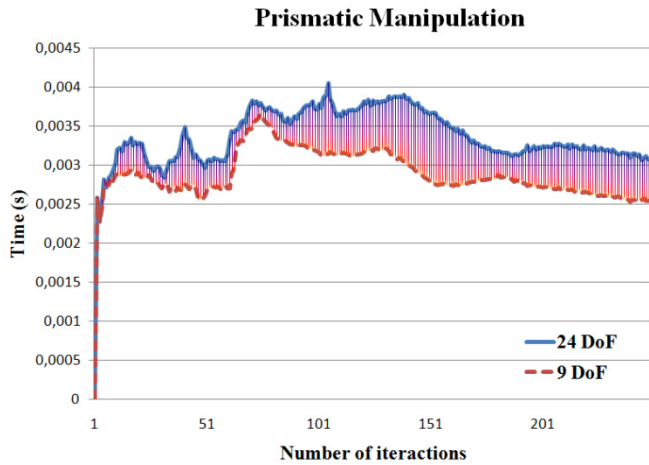


Fig. 5. Time used for collision detection in 24 DoF hand model and SHM with 9 DoF for a prismatic grasp handling

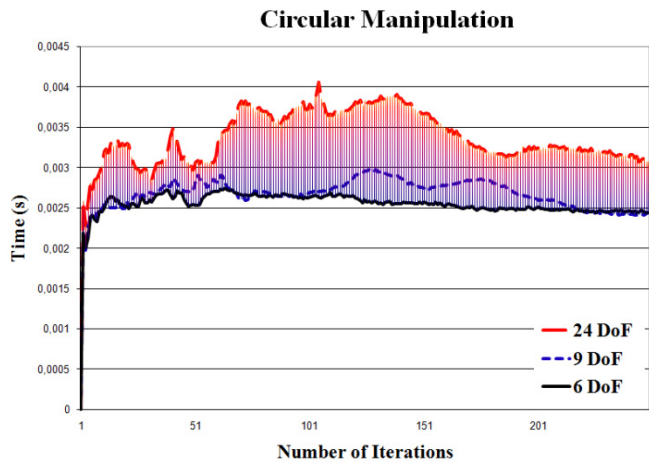


Fig. 6. Time used for collision detection among 24 DoF hand model, SHM with 9 DoF and SHM with 6 DoF for circular grasp handling.

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