Dynamic Trot-Walking with the Hydraulic Quadruped Robot - HyQ: Analytical Trajectory Generation and Active Compliance Control

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Abstract—This paper presents a trajectory generator and an active compliance control scheme, unified in a framework to synthesize dynamic, feasible and compliant trot-walking locomotion cycles for a stiff-by-nature hydraulically actuated quadruped robot. At the outset, a CoP-based trajectory generator that is constructed using an analytical solution is implemented to obtain feasible and dynamically balanced motion references in a systematic manner. Initial conditions are uniquely determined for symmetrical motion patterns, enforcing that trajectories are seamlessly connected both in position, velocity and acceleration levels, regardless of the given support phase. The active compliance controller, used simultaneously, is responsible for sufficient joint position/force regulation. An admittance block is utilized to compute joint displacements that correspond to joint force errors. In addition to position feedback, these joint displacements are inserted to the position control loop as a secondary feedback term. In doing so, active compliance control is achieved, while the position/force trade-off is modulated via the virtual admittance parameters. Various trot-walking experiments are conducted with the proposed framework using HyQ, a $\sim 75kg$ hydraulically actuated quadruped robot. We present results of repetitive, continuous, and dynamically equilibrated trot-walking locomotion cycles, both on level surface and uneven surface walking experiments.

I. INTRODUCTION

Decentralized dynamic legged locomotion control is often decomposed into two sub-phases: i) Online referential trajectory generation to obtain feasible motion inputs, ii) real-time sensory feedback control to regulate unmodelled dynamics and handle unexpected irregularities. The robotics literature includes a sizable amount of research work, where this approach is experimentally proved to be efficient [1]– [10].

When it comes to quadrupedal trajectory generation, CPG (Central Pattern Generator) networks appear to be a popular choice. Researchers utilize nonlinear oscillators to synthesize trajectories with various shapes; such as, sinusoidal or elliptical [10]–[12]. CPGs are also observed in biological creatures; and therefore, their application to multi-legged locomotion is somewhat naturally insightful.

Despite their impressive performance, CPG-based motion generation has limitations. For example, often CPGs require non-intuitive hand-tuning while it is also difficult to incorporate online feedback, sometimes crucial for the

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Fig. 1. The hydraulically actuated quadruped robot - HyQ [6]. It has 12 degrees of freedom and its size is comparable to a goat. HyQ is designed for highly dynamic behaviors, e.g. trotting and jumping.

success of the controller. Keeping these in mind, a group of researchers directed their attention to alternative approaches. For instance, Moro and his associates use motion capture data from a horse and utilized these as kinematic motion primitives [13]. Kalakrishnan and his teammates proposed a *Center of Pressure* (CoP)-based trajectory generation to achieve rough terrain locomotion [4].

Among these approaches, Zero Moment Point (ZMP)based methods are proven to be reliable in generating physically viable quadrupedal locomotion trajectories [4], [8], [9]. The basic idea is to solve ZMP differential equations for a given feasible ZMP input to obtain the corresponding CoM trajectory (so-called inverse ZMP problem [8]). As noted by Byl et al. in [8], this approach cannot be implemented in a straightforward fashion, due to the nature of the mathematical equations that govern the ZMP model. To overcome this issue, researchers implemented polynomials [4], pre-defined sinusoidals [14], and numerical integration [9]. In an alternative solution, Kajita implemented preview control, which interpreted the issue as ZMP servo tracking control [7]. Byl et al. particularly applied this approach to quadrupedal locomotion as well [8].

While impressively useful in its own right, we believe that the ZMP-based feasible CoM motion generation can be solved by considering symmetry conditions, rather than interpreting the issue as a ZMP servo tracking problem or utilizing certain type of predetermined function-based solutions. In doing so, this task can be realized in a simpler and more viable way without any necessity of ZMP feedback loop. One can generate ZMP-based feasible CoM trajectories

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purely in an open-loop strategy, the choice of feedback control can then be freely designated.

Considering real-time sensory feedback control. impedance control seems to be the general approach. By inserting floating-base inverse dynamics terms as feedforward torques, it is possible to achieve sufficient joint position tracking with relatively lower gains, so that the locomotion becomes more compliant [4] [5]. On the contrary, this method may not create a link between force control and active compliance; the stiffness could remain the same regardless of the force error. As an alternative to this approach, we propose to run the system via PD servo controllers. In parallel to these servo loops, we have an additional admittance controller that decreases the joint stiffness when force error appears. The admittance block evaluates the force error and generates the corresponding displacement which is used as a secondary position feedback term to perturb position reference, in a way to comply with the force constraint. As soon as the external force/disturbance causing the force error vanishes, the joint turns back to its initial stiffness for position tracking. This trade-off is modulated by a set of admittance coefficients. Note that feed-forward inverse dynamics terms may still be included in our method in a way to refine PD servo controllers, e.g., to decrease PD gains.

In the light of the above discussion, the contributions of this paper can be grouped in two directions: a) We propose a CoP-based CoM trajectory generator, in which initial conditions are uniquely set for physically-viable motion characteristics. The trajectory generator is purely computational and enforces no feedback loop requirements, easy-to-apply and analytical. Thus, the choice of feedback control can be freely designated. b) An admittance control scheme is adopted to achieve active compliance control for quadrupedal locomotion, in which environmental interactions are compliantly handled. The controller normally prioritizes position tracking. It decreases the stiffness only within the presence of joint force error. Therefore, it is relatively more reactive comparing to off-the-shelf methods in terms of stiffness-force control connection.

The paper is organized as follows. We briefly introduce our experimental platform in section II. Section III is devoted to explain the derivation of trajectory generator. The controller algorithm is explained in detail in section IV. Experimental results are thoroughly evaluated in section V. Finally, the paper is concluded in section VI by stating final discussions.

II. HYQ QUADRUPED

Our platform, HyQ (see Fig. 1), is a fully torque-controlled hydraulically and electrically actuated quadruped robot comparable in size to a goat (\sim 75kg), e.g. an *Alpine ibex*. It has been designed and built at the *Istituto Italiano di Tecnologia* and it uses a combination of hydraulic cylinders and electric motors for the actuation of its 12 joints [6]. HyQ is capable of highly dynamic locomotion as hydraulic actuation allows the handling of large impact forces, high bandwidth control, high power-to-weight ratio and superior robustness.



Fig. 2. Corresponding feet positions of quadruped trot-walking, in equivalent planar biped model. Rectangular shapes are used to indicate EPB feet, solely for the illustration. They do not indicate any support region.

Each leg has three degrees of freedom (*DoFs*), two in the hip (abduction/adduction (hip_{aa}) and flexion/extension (hip_{fe})) and one in the knee (flexion/extension ($knee_{fe}$)). The hip_{aa} joints are actuated by electric motors while all the hip_{fe} and the $knee_{fe}$ joints are hydraulically actuated. All of the quadruped's joints are equipped with high resolution encoders and load cells, which allow a smooth control of both position and torque. Overall, the robot weighs ~75kg, it is 1m long and 0.5m wide and stands 1m high with the legs fully stretched. The system is controlled by a Pentium PC104 running real-time patched Linux (*Xenomai*) and is capable of reaching a 1kHz control frequency.

III. TRAJECTORY GENERATION

In quadrupedal trot-walking, robot feet are diagonally paired as shown in Fig. 2. While the robot is in motion, these paired legs move simultaneously. In a continuous trotwalking, there are three phases: i) Left front, right hind stance phase; ii) 4 legs stance phase, iii) Right front, left hind stance phase. Since there is no 3 legs stance phase, we can create an analogy for an equivalent planar biped (EPB) model, considering the particular trot-walking motion (see Fig. 2). That being said, left foot of biped is the middle point of left front - right hind couple. In a similar manner, right foot of biped is the middle point of right front - left hind couple. Aforementioned phases then can be interpreted as i) left foot single support phase, ii) double support phase, iii) right foot single support phase. To simplify the concept, we will use this model in generating quadrupedal trot-walking trajectories.

In addition, our experimental experiences indicate that quadruped trot-walking can be achieved without any lateral motion, i.e., the robot does not have to sway towards left or right since it is equally balanced on the diagonally paired legs. Keeping this in mind, we only focus on sagittal plane motion generation in this study.





Fig. 4. EPB model during single support phase. Rectangular shapes are used to indicate EPB feet, solely for the illustration. They do not indicate any support region.

Fig. 3. Feasible CoM motion during a single (0.0-0.8 secs.) and a double (0.8-0.9 secs.) support periods. x: poisition, dx: velocity, ddx: acceleration.

A. CoM Trajectory

As previously stated, we make use of CoP criterion to generate dynamically balanced CoM trajectories. When considering point mass model, ZMP and CoP (Center of Pressure) coincides; therefore, we use the term CoP instead of ZMP. Let us begin with analyzing CoP equations for a trot-walking scenario with constant CoM height [7].

$$X_{cop} = x - z\frac{\ddot{x}}{g} \tag{1}$$

In (1), (x, z) are horizontal and vertical CoM position, g is gravitational acceleration, and X_{cop} is x-axis CoP. Depending on the X_{cop} input, we may solve (1) analytically. In order to obtain an analytical solution, X_{cop} can be selected either a step or a ramp input.

In our trajectory generator, X_{cop} is constant during single support phases ($X_{cop} = p_x$), and linearly increasing during double support phases ($X_{cop} = K_x t + p_x$).

1) CoM Trajectory During Single Support Phase: During single support phases, we consider a constant X_{cop} input; $(X_{cop} = p_x)$. In this case, (1) can be analytically solved as follows;

$$x = (x_0 - p_x) \cosh \omega \tau + \frac{x_0}{\omega} \sinh \omega \tau + p_x \qquad (2)$$

$$\omega = \sqrt{\frac{g}{z}}, \quad \tau = t - t_0, \tag{3}$$

in which x_0 , \dot{x}_0 , ω , t, t_0 are initial CoM position, initial CoM velocity, equivalent pendulum natural frequency, time variable and initial time, respectively. CoM velocity and acceleration functions can also be obtained via differentiation, as in the following.

$$\dot{x} = \omega (x_0 - p_x) \sinh \omega \tau + \dot{x}_0 \cosh \omega \tau \tag{4}$$

$$\ddot{x} = \omega^2 (x_0 - p_x) \cosh \omega \tau + \omega \dot{x}_0 \sinh \omega \tau.$$
 (5)

In order to obtain a physically viable CoM trajectory, a single support phase should be composed of two equal deceleration and acceleration phases. A numeric example is illustrated in Fig. 3, in sequence with a double support period. As a crucial feature of a viable CoP-based CoM trajectory, initial CoM velocity should be equal to terminal velocity. It also makes initial acceleration and terminal acceleration equal in amplitude with opposite signs. This property can be guaranteed by setting initial conditions in accordance with desired motion parameters. Since the solution of CoP equations are hyperbolic functions, any single support phase with unbalanced deceleration/acceleration periods will accumulate exponential increases in CoM position and produce physically unrealizable trajectories.

Using the above-mentioned symmetry property, we may realize that velocity position has a minimum at the middle point of a single support period, i.e., when $t = t_m = t_0 + T_s/2$, where T_s is single support time period.

$$\ddot{x}|_{t=t_m} = \omega^2(x_0 - p_x)\cosh(\frac{wT_s}{2}) + \omega \dot{x}_0\sinh(\frac{wT_s}{2}) = 0 \quad (6)$$

Utilizing (6), one can yield \dot{x}_0 as below.



Fig. 5. EPB model during a double support phase. Rectangular shapes are used to indicate EPB feet, solely for the illustration. They do not indicate any support region.

$$\dot{x}_0 = \omega(p_x - x_0) \coth(\frac{wT_s}{2}) \tag{7}$$

During a single support phase, we may substitute an mean forward velocity, v_{mean} . Considering this parameter, the terminal position, x_d , can be computed (see Fig. 4).

$$x_d = v_{mean} T_s + x_0. \tag{8}$$

Terminal position x_d can also be computed by using (2), when $t = t_e = t_0 + T_s$:

$$x|_{t=t_e} = x_d = (x_0 - p_x)\cosh(\omega T_s) + \frac{\dot{x}_0}{\omega}\sinh(\omega T_s) + p_x.$$
 (9)

Inserting (7) into (9), hyperbolic terms cancel each other out $(\cosh \omega T_s - \sinh \omega T_s \coth 0.5\omega T_s) = -1$), and following equation is yielded.

$$x_d + x_0 = 2p_x \tag{10}$$

Combining (8) and (10), x_0 and x_d terms are calculated in the following manner.

$$x_0 = p_x - \frac{v_{mean}T_s}{2}; \quad x_d = 2p_x - x_0$$
 (11)

For a given set of single support period (T_s) , target mean velocity (v_{mean}) , and constant X_{cop} input (p_x) , we may sequentially calculate initial conditions (x_0, \dot{x}_0) via (11) and (7). x_d can also be calculated beforehand for prior verification.

2) CoM Trajectory During Double Support Phase: The main task during double support phase is to carry CoP from the preceding support foot to the proceeding support foot, without any discontinuity as displayed in Fig. 5. Furthermore, at the end of a double support phase, CoM velocity and acceleration values must be coincided with initial CoM

velocity and acceleration values for the next single support phase; so that we can connect the sequential phases seamlessly. Referring to Fig. 5, we may solve differential equation (1) for a linearly increasing X_{cop} input ($X_{cop} = K_x t + p_x$). Its first time derivative also provides us velocity function as well.

$$x = (x'_0 - p_x) \cosh \omega \tau' + \frac{\dot{x}'_0 - K_x}{\omega} \sinh \omega \tau' + K_x \tau' + p_x \quad (12)$$
$$\dot{x} = \omega (x'_0 - p_x) \sinh \omega \tau' + (\dot{x}'_0 - K_x) \cosh \omega \tau' + K_x \quad (13)$$

In (12) and (13), (x'_0, \dot{x}'_0) are initial position and velocity terms for a double support phase. They are equal to terminal position and velocity of the preceding single support phase, as indicated in (14). K_x is a slope value for X_{cop} . $\tau' = t'_0 + t$ stands for shifted time variable with initial time for double support period, namely t'_0 . For a seamless connection, terminal velocity of a double support phase should be equal to initial velocity of the following single support phase when $t = t_{ed} = t'_0 + T_d$.

$$\begin{aligned}
x'_{0} &= x_{d}; \quad \dot{x}'_{0} = \dot{x}_{0}; \quad (14) \\
\dot{x}|_{t=t_{ed}} &= \dot{x}_{0} = \omega(x_{d} - p_{x}) \sinh \omega T_{d} \\
&+ (\dot{x}_{0} - K_{x}) \cosh \omega T_{d} + K_{x}. \quad (15)
\end{aligned}$$

Assessing (15), K_x and stride lenght, Str, may be obtained as follows.

$$K_x = \dot{x}_0 + \omega (x_d - p_x) \coth \frac{\omega T_d}{2}; \qquad (16)$$

$$Str = 2T_d K_x \tag{17}$$

3) *Trajectory Generation Algorithm:* One can easily generate CoM trajectories via the following algorithm.

- 1) Assign single/double support periods (T_s, T_d) , constant CoM height (z), mean target velocity (v_{mean}) and constant ZMP input for a single support period (p_x) .
- 2) Sequentially compute ω , x_0 , x_d , \dot{x}_0 , K_x and *Str* via (3), (11), (7), (16), and (17).
- For single support phases, use (2) to generate CoM trajectory. For double support phases, use (12) to generate CoM trajectory.

This algorithm makes sure that sequential single and support phases are tied seamlessly, both for X_{cop} and corresponding x, \dot{x} , \ddot{x} trajectories, through the exploitation of symmetry properties as explained above. Please refer to sample code for MATLAB¹ for further examination.

B. Swing Leg Trajectories

Swing leg trajectories are constructed using polynomials by considering the Stride length (Str) and maximum vertical swing foot clearance. In generating swing leg trajectories, both initial and terminal velocity and acceleration terms are set to zero to make sure that swing foot does arrive to the floor in a motionless state, so that impact forces may be reduced.

¹https://dl.dropbox.com/u/21136797/UgurluIROS13SampleCode.zip



Fig. 6. Vectorial quantities on the quadruped [9]. Legs are also numbered.



Fig. 7. Ground reaction force at a foot tip.

C. Joint Motion Computation

In order to realize CoM and swing leg trajectories, we are in need of computing the position vector that is defined between the respective hip and foot position for each leg. If we refer to Fig. 6, the associated vectorial operation for the 2^{nd} leg can be expressed as below.

$$\mathbf{r_{hf}} = R_b^T (\mathbf{r_f} - \mathbf{r_c}) - \mathbf{r_{ch}}$$
(18)

In (18), $\mathbf{r_f}$ is a foot position vector with respect to world frame, $\mathbf{r_c}$ is the CoM position vector with respect to world frame, R_b is upper torso orientation that is composed of three possible rotations about pitch (θ) and (ψ) roll and yaw (γ) axes, $\mathbf{r_{ch}}$ is a position vector between CoM and the respective hip. After calculating $\mathbf{r_{hf}}$ vector for each leg, joint angles can be analytically computed, via the utilization of a 3-DoF inverse kinematics scheme.

In summary, we define 18 inputs for the joint motion generation task; CoM position (3 elements), each foot positions (12 elements), and torso orientation (3 elements). In

total, we define 18 inputs, whereas the robot has only 12-DoF. This may seem to be an underactuation issue; however, diagonal pairs move simultaneously during trotting motion. That being said, 6 inputs are not imposed to system, making our calculation to have a unique solution.

IV. ACTIVE COMPLIANCE CONTROL

A. Referential Force Calculation

In the proposed active compliance controller, we simultaneously process position and force references. Therefore, one needs to define joint force references in accordance with the target trajectory. To attain this goal, we primarily define 3 equations using vertical forces.

$$Mg = \sum_{i=1}^{4} F_{zrefi}; \tag{19}$$

$$X_{copref} = \frac{\sum_{i=1}^{2} (F_{zrefi} r_{cfxrefi})}{\sum_{i=1}^{4} F_{zrefi}}; \quad (20)$$

$$Y_{copref} = \frac{\sum_{i=1}^{4} (F_{zrefi} \ r_{cfyrefi})}{\sum_{i=1}^{4} F_{zrefi}}; \quad (21)$$

In (19)-(21), M is total mass, g is gravitational acceleration, F_{zrefi} is i^{th} foot vertical force reference, X_{copref} and Y_{copref} are CoP references, $r_{cfxrefi}$ and $r_{cfyrefi}$ refer to referential displacement between CoM and i^{th} foot, through x-axis and y-axis. In (19), we equalized total force to the robot weight, since there is no vertical acceleration during trot-walking. Eqs. (20) and (21) allow us to utilize force distribution; usually both CoP references are kept at zero.

In addition to (19)-(21), we need to define one more condition, since we have 4 legs. This can be obtained from zero-yawing motion. However, this condition is related to horizontal (F_{xrefi}) and lateral (F_{yrefi}) forces. Even though the robot has point contact feet, the total ground reaction force is decomposed depending on the foot landing angle (see Fig. 7). That being said, (F_{xrefi}) and (F_{yrefi}) can be expressed in terms of F_{zrefi} , so that we may obtain the 4th condition.

$$F_{xrefi} = F_{zrefi} \tan(q_1 + q_2) \sec q_0; \tag{22}$$

$$F_{yrefi} = -F_{zrefi} \tan q_0; \tag{23}$$

$$F_{yref1}r_{cfxref1} - F_{xref1}r_{cfyref1} + F_{yref2}r_{cfxref2}$$

$$- F_{xref2}r_{cfuref2} + F_{uref3}r_{cfxref3} - F_{xref3}r_{cfuref3}$$

$$= \frac{1}{2} \frac{$$

$$+ Tyref4Tcfxref4 - Txref4Tcfyref4 - 0.$$
(24)

Referring to Fig. 7, q_0 , q_1 , and q_2 respectively denote roll axis hip (hip_{aa}) , pitch axis hip (hip_{fe}) , and pitch axis knee $(knee_{fe})$ joints. Combining (22)-(24) would give us the 4th equation. In addition to (19)-(21), all these equations enable us to compute vertical force references for each foot,



Fig. 8. Active compliance control in the servo loop.

during double support phase where all 4 feet are on the ground. During single support phases, we have only 2 feet on the ground; thus, we only utilize (20) and (21) to compute vertical force references. Swing foot force references are naturally set to zero. Once we have vertical force reference for the i^{th} foot (F_{zrefi}), we can compute horizontal and lateral components (F_{xrefi} , F_{yrefi}) using (22) and (23). Having computed all the 3-D referential force vector for the i^{th} leg, we make use of Jacobi transpose to obtain referential joint forces.

B. Joint Force Feedback: An Antagonistic Approach

Fig. 8 depicts the controller that is implemented in the proposed method. In this figure, q_{ref} , q and q_c stand for referential joint angles, actual joint angles, and output of admittance block. T_{ref} , T_{sv} , T_{fr} , T_{cm} , T, and T_{err} respectively denote referential, PD output, friction compensation, command, actual (measured) and error torques. K_p and K_v refer to PD gains, k and b show admittance block coefficients.

Primarily, trajectory generator provides referential joint angles which are inserted to PD servo controllers. On top of this scheme, we added a force control loop in which joint force errors are processed via an admittance block to compute corresponding joint displacements, namely. By perturbing joint reference for about q_c degrees, joint force feedback is provided. In this scheme, basically PD controller makes sure that position tracking is achieved. However, within the presence of force errors, q_{ref} is updated via the secondary feedback $(q_{ref} : q_{ref} - q_c)$ to comply with force constraints, by decreasing the joint stiffness. Once, the external effect that causes force error (disturbances, ground impact, etc.) q_c term vanishes and joint turns back to its initial stiffness. The trade-off between position and force tracking is adjusted via admittance block parameters. In other words, force control loop and position control loop works in an antagonistic configuration; the joint becomes compliant when necessary to handle force errors. If there is no force error, it prioritizes joint tracking. Moreover, friction compensation is added to enhance control performance [15].

Comparing to off-the-shelf active impedance control approaches, the proposed scheme associates compliance with



Fig. 9. A snapshot from level surface trot-walking experiments, conducted on a treadmill.



Fig. 10. A snapshot from uneven surface trot-walking experiments, conducted outdoor. Three wooden plates with 3 [cm] thicknesses are placed on the floor, in a way that the robot gradually steps over.

force feedback. In impedance-based methods, the joint always keeps the preset stiffness/softness regardless of the force error. Our proposed controller, on the other hand, creates a link between force feedback and active compliance modulation strategy. It can also be used with inverse dynamics to further improve the performance [9]. The earliest reference to this approach can be found in [16], in which NASA researchers achieved compliant tele-operation tasks.

V. EXPERIMENT RESULTS

In order to validate the proposed trajectory generator and controller, we conducted two different experiments. i) Trot-walking on a level surface (treadmill), ii) Trot-walking on uneven surface (outdoor). In both experiments, trot-walking parameters are set as the same. Single and double support time periods are 0.28 [s] and 0.14 [s], constant CoM height is 0.68 [m], constant ZMP input is 0 [m], maximum vertical swing foot clearance is 10 [cm]. Target mean velocity is set as 1.26 [km/h] for level surface experiments and 0.36 [km/h] for uneven surface experiments. Fig. 9 and Fig. 10 display a couple of snapshots from the experiments, which can be viewed in the multimedia attachment of this paper.

A. Level Surface Trot-Walking Experiments

To begin with, we conducted level surface experiments on a treadmill (see Fig. 9). Fig. 11 displays the results of this



Fig. 11. Level surface experiment results.

experiment.

Referential feet displacement and CoM trajectory with respect to world frame is shown in Fig. 11(a). Feet positions are plotted with EPB model in mind (see Fig. 2) to provide a clearer view. Judging by this figure, we may claim that the proposed trajectory generator is able to synthesize smooth and continuous motion patterns, which are seamlessly connected through single and double support phases. Trajectories are also observed to be smooth and continuous in velocity and acceleration levels, but not plotted due to page restrictions. Note that the plot displays only 8 steps; however, real experiments include much longer experimentation periods.

Vertical ground reaction forces (GRFs) are estimated using joint torque and position sensors and depicted for each leg in Fig. 11(b). We may see that diagonally paired legs move simultaneously as their swing and stance phases seem to be overlapped. In this figure, it is possible to observe two benefits that are gained through the utilization of active compliance controller: i) Reaction forces are equally distributed to each leg, so that the robot can exhibit dynamically balanced locomotion characteristics. ii) Touch-down impacts are relatively low for a $\sim 75[kg]$ quadruped robot with stiff-by-nature actuation configuration, resulting in a more



Fig. 12. Uneven surface experiment results.

compliant and efficient trot-walking locomotion.

x-axis CoP response variation with respect to local body frame is displayed in Fig. 11(c). Scrutinizing this figure, X_{cop} varies between ± 1.5 [cm]. Even though the support polygon is a diagonal line for trot-walking locomotion, the actual support polygon can be stretched ± 3 [cm] due to non-zero foot tip surface. Therefore, any local CoP variation between ± 3 [cm] margins are considered to point out dynamically balanced locomotion. This result does vary within this range, indicating that the level surface trot-walking experiments are conducted in a dynamically equilibrated manner.

Torso angle variations are also collected via an IMU module and plotted in Fig. 11(d). In this figure, we may see that pitch and roll torso angle variations are respectively kept within ± 4.8 [Deg] and ± 2.4 [Deg] ranges. This result gives us a clue about the trot-walking performance; thanks to active compliance controller, the robot is not prone to undesired torso angle fluctuations which may be caused by inequal reaction force distribution to legs or large ground reaction force impacts. Based on this result, it may be claimed that the controller potentially escalates dynamic trot-walking performance.

B. Uneven Surface Trot-Walking Experiments

Upon the successful completion of level surface experiments, HyQ is moved outside of the laboratory and trotwalking experiments are conducted on an uneven terrain (see Fig. 10). For this purpose, 3 wooden plates with 3 [cm] thickness are gradually placed on top of each other, both creating unevenness and moderate slope. Trajectory generator is not modified; however, only target forward velocity is reduced to eliminate the risk of any possible damage to the robot. Fig. 12 points out the results from this experiment. Due to page restrictions, only CoP and torso angle variations are included.

x-axis CoP variations with respect to local body frame is illustrated in Fig. 12(a). This measurement primarily follows

a variation trend between ± 0.7 [cm]. As the robot starts walking on the uneven terrain, it starts varying within a larger amplitude band which is observed to be $+1.7 \sim -2.5$ [cm]. Even though the variation amplitude band enlarges, it is still within the feasible support polygon range which is ± 3 [cm]. Observing this outcome, we may conclude that the robot is able to walk on the specified uneven terrain with dynamically balanced trot-walking locomotion cycles.

Torso angle variations are included in Fig. 12(b). Initially, our measurements show a variation trend around ± 4 [Deg]. Once the robot starts trot-walking on the uneven terrain, pitch angle variation amplitude gets bigger and becomes ± 8 [Deg]. Roll angle variation also show a slight increase. Increases in torso angle variations are expected, this is a price to be paid while the robot is performing outdoor trotwalking on an irregular surface. Nevertheless, this result did not influence the overall dynamic balance and the robot successfully completed its task.

VI. FINAL DISCUSSIONS

In this paper, we proposed an analytical trajectory generation algorithm and an active compliance controller, which are combined in dynamic trot-walking task for an hydraulically actuated, stiff-by-nature ($\sim 75kg$) quadruped robot. To validate the proposed schemes, two types of dynamic trotwalking experiments are conducted: i) Level surface trotwalking on a treadmill, ii) uneven surface trot-walking. In both experiments, the robot is able to complete the tasks with dynamic, repetitive, continuous, and dynamically balanced trot-walking locomotion characteristics.

The trajectory generator is confirmed to be able to synthesize reliable trot-walking locomotion cycles, which are smooth, continuous and correspond to feasible CoP inputs. The algorithm is easy-to-implement and only requires a couple of parameters to be tuned. Comparing to other trajectory generators, the number of free parameters are relatively low and it does not dictate any obligatory feedback loop. The choice of controller can be freely designated.

The active compliance controller is also observed to be efficient in handling environmental interaction while the robot is trot-walking. It enabled us to obtain equally distributed reaction forces and relatively lower touch-down impacts. These properties directly related to overall trotwalking performance, and thus, allow us to escalate the locomotion efficiency.

As future directions, one may seek ways to include CPGs into CoP (or, in other words, ZMP)-based trajectory generation algorithm to synthesize a method which possess advantages of both approaches. In addition, our team is implementing an overall state estimation based on sensor fusion. Together with these improvements, it could be possible to conduct highly rough terrain locomotion experiments on HyQ.

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