Compensating Device Inertia for 6-DOF Haptic Rendering

Jilin Zhou†, François Malric‡, Emil M. Petriu∗, and Nicolas D. Georganas∗†
Distributed and Collaborative Virtual Environments Research Laboratory (DISCOVER)
School of Information Technology and Engineering (SITE), University of Ottawa
Ottawa, Canada
∗jzhou/mlaric/georganas@discover.uottawa.ca, †petriu@site.uottawa.ca

Abstract—In this paper, the importance of the user’s primary holding pivot point on the end effector of a haptic interface is discussed. Both theoretical analysis and experimental results demonstrate that this holding pivot point is critical for the correct perception of the haptic properties assigned to the virtual objects. We also study the physical inertia effects of the end effector on the non-uniform stiffness perception of simulated virtual objects. To the best of our knowledge, no such combined consideration of holding pivot point and device structure related inertia has so far been made for works in 6-DOF haptic rendering.

We have instrumented the end effector of a haptic interface with a membrane potentiometer to measure the user’s primary holding pivot point in real-time. Accordingly, a preliminary adaptive feedback method is developed to render the appropriate forces/torques to compensate for the effects of the end effector’s inertia on the haptic stiffness perception.

Index Terms—6-DOF haptic rendering, tip inertia, holding pivot point, collision point.

I. INTRODUCTION AND MOTIVATION

Haptics, originally from the Greek verb “haptesthai” (to touch), pertains to the sense of tactile and kinesthetic touch. Since the emergence of the Phantom series of haptic interfaces in the middle 1990s, haptics has been a fast-growing interdisciplinary research field in the areas of psychophysics, haptic interface design, and particularly the replication of real-world interacting forces in virtual reality (VR) applications. Haptic rendering refers to the process of computing and exhibiting interaction forces between a virtual tool, which directly follows the prismatic holding postures for precision grip as shown in Fig. 1, haptic rendering includes two main modules: collision detection and contact determination for complex objects with multiple point interaction.

For haptic interfaces generating only translational force, the tool is usually modeled by a zero-mass point or sphere with a small radius for the collision detection [2], [3]. This point-based method is adequate for applications where tool-object interactions can be sufficiently described as a point-surface contact. But many of our real-world tasks do not fall into this contact paradigm. For instance, when we tighten a bolt using a wrench, the contacts between the bolt and the wrench may be a point-surface contact, a line-surface contact, a surface-surface contact, or a combination of them. There are two primary distinctions in these general tool-object operations. The first one is that the contact point can be anywhere on the tool. The second one is that the torque generated by the contact force passes important information to the user about the interaction and is essential for the completion of the task. Therefore, to simulate these general operations, the tool should be modeled as its real geometric shape in the process of haptic rendering. This 6-DOF haptic rendering not only increases the computational complexity of the collision detection but also requires the devices with the capability of providing both translational force and rotational torque. Current research on 6-DOF haptic rendering mainly focuses on the real-time collision detection and contact determination for complex objects with multiple point interaction.

In this paper, we will discuss the effects of the user’s holding points on the end effector for the perception of the force/torque feedback from the VE. In the real-world, the objectives of the task usually determine how the tool is held, the number of fingers involved, and the forces exerted by the different fingers. The force exerted on the tool from each finger is also generally time-varying. In addition, the force/torque felt by the user while using a tool is also related to the hand holding posture and its relative configuration on the tool. For instance, the prismatic holding postures for precision grip as shown in

Fig. 1: Typical haptic rendering process
DOF haptic rendering is also described. The maximum linear stiffness of the collision point in 6-DOF haptic simulation is discussed from two perspectives: the virtual holding point on the virtual tool and the real holding point in real-time and by modifying the rendered force/torque for these multi-points and time-varying holding postures is challenging. Currently, the user holding points on the end effector is either not considered or just assumed to be fixed. This may not be important for general virtual touching applications, but for some applications such as medical simulations to train students on how to make a cut with a scalpel or tele-operated surgery, the realistic haptic rendering of the interaction is extremely important because the decision for future steps is heavily relied on the current haptic feedback.

We will also discuss the effects of physical inertia of the end effector (device inertia) on the rendering of haptic feedback. In any haptic simulations, we always hope that the requested force/torque can be faithfully transmitted to the user through the equipped joint motors. However, some factors which may affect this include motor dynamics, current amplifier characteristics, and arm structure [7]. Through experiments, we have found that the device inertia affects the perceived stiffness of the simulated objects non-uniformly. We propose an adaptive method to compensate for it by measuring the primary holding point in real-time and by modifying the rendered force/torque based on the relative configuration between the virtual collision point and the primary holding point. Our preliminary results show the effectiveness of the method.

The rest of this paper is organized as follows. Section II discusses the role of the holding point in current 6-DOF haptic rendering algorithms. The maximum linear stiffness at the collision point is also discussed. Section III describes the problems and the proposed method for the device inertia compensation. Section IV describes the experiment procedure and the results. Section V concludes the paper and describes some future work.

II. HOLDING POINT IN 6-DOF HAPTIC RENDERING

In this section, the role of the user’s holding point for 6-DOF haptic simulation is discussed from two perspectives: the virtual holding point on the virtual tool and the real holding point (control point) on the end effector of the device. The maximum allowed linear stiffness of the collision point in 6-DOF haptic rendering is also described.

A. Virtual holding point

For 6-DOF haptic rendering, there are two main ways to compute the force/torque feedback: direct rendering and simulation-based rendering [8]. Let us take the stick-on-ball application shown in Fig. 3 as an example in which the stick is the virtual tool held by the user and the ball is the interacting virtual object. With direct rendering, when the stick is penetrating the ball, the point on the surface of the stick (collision point) with the deepest penetration depth and correspondent contact point on the surface of the ball (proxy point) are first determined. A spring force $f$ is then calculated between these two correspondent points as the translational force feedback component. At the same time, force $f$ will generate a torque/moment component around the holding point. This feedback force/torque pair will push the stick out of the ball so that the user feels the collision and the stiffness of the ball. Other haptic properties such as frictions can be simulated by the perturbation of the force $f$ according to some physical laws.

![Fig. 2: Prismatic handling posture adapted from [4]](image)

![Fig. 3: Direct haptic rendering](image)
B. Real holding point

After a feedback force/torque pair $F_t = [f_t \tau_t]^T$ from the simulation is determined, a correspondent motor torque $\tau$ to render on the end effector has to be calculated. In this section, we discuss the effects of the user’s real holding point on the end effector for the perception of the requested $F_t$. A 6-DOF haptic interface, the MPB Freedom6S hand controller, is taken as an example. The Freedom 6S is equipped with 6 joint motors for the rendering of both translational force and rotational torque. Fig. 5 provides a conceptual view of the linkage of the last three joints which renders most of the rotational torque component to the users. During the device initialization stage, the programmer specifies a spatial frame on the end effector as the control point to represent the location of the user’s primary holding point. The following access of the forward kinematics describes the configuration of the moving tool frame relative to this spatial frame. The holding point is sometimes called the control point since the motor torque is computed with respect to it.

To generate $F_t$ around the control point, the required motor torque is given by

$$\tau = (J_{st}^b(\theta))^T F_t,$$  \hspace{1cm} (1)

where $J_{st}^b(\theta)$ is the body Jacobian of the device in its current configuration. Expanding $J_{st}^b(\theta)$ in (1) for the MPB Freedom6S hand controller, it gives

$$J_{st}^b(\theta) = \begin{bmatrix} 0 & 0 & 0 \\ -a \cos(\theta_4) \sin(\theta_5) & a \cos(\theta_4) & 0 \\ \sin(\theta_5) & 0 & 1 \\ \cos(\theta_2) \cos(\theta_4) & 0 & \sin(\theta_4) \\ \cos(\theta_2) \sin(\theta_4) & 0 & \cos(\theta_4) \end{bmatrix},$$

where $a$ denotes the distance from the tip of the end effector to the control point. Each column of $J_{st}^b(\theta)$ corresponds to a joint twist written with respect to the tool frame in the current configuration [9]. $\xi_0^b$, $\xi_1^b$, and $\xi_2^b$ are not shown here because of their lengthy expressions. It is obvious that $J_{st}^b(\theta)$ depends on the location of the control point which represents the user’s primary holding point. If an unmatched Jacobian matrix $J_{st}^b(\theta)$ is applied, the user will perceive a distorted feedback $F_t = ((J_{st}^b)^{-1})^T F_t$ at the holding point instead of the desired $F_t$. One direct implication is that the user will not perceive the correct mechanical properties such as the stiffness assigned to the virtual objects. In many haptic-enabled virtual environments, e.g., surgical simulations, accurate perception of mechanical properties such as tissue stiffness is indeed very important to task performance. Therefore, the selection of the correct control point on the end effector is important for the simulation.

C. Maximum linear stiffness of collision point

In haptic simulation, translational force feedback is usually calculated with linear Hook’s law: $f = K \cdot d$, where $K$ is spring constant (linear stiffness) describing the stiffness of the simulated object and $d$ is the penetration depth between the virtual tool and object. During the experiments, we notice that the vibration increases with the point of force application (collision point) far from the center of the distal stage (tip of end effector) as shown in Fig. 5. To understand the nature of the problem, let us take a look at a 1-DOF example. In Fig. 6, a collision happens at the end of the lever with a penetration depth $d$ of $1 \text{ mm}$. If linear stiffness $K = 1 \text{ N/mm}$ is simulated, a $1 \text{ N}$ feedback force $f$ is required. Since the motor joint (rotation axis) is $1 \text{ mm}$ away from the collision point, the angular motion $\theta$ around the joint is $d/l$ and the joint torque $\tau$ to generate $f$ is $l \times f$. Accordingly, the required angular stiffness $K_\theta$ for the joint is

$$K_\theta = \tau/\theta = l^2 \cdot K.$$  \hspace{1cm} (3)

For haptic interfaces, this angular stiffness for each joint is a function of the motors’ capability and the integrity of the linkage structure. For the MPB Freedom6S hand controller, the maximum linear stiffness at the center of the distal stage is between $1 \sim 2 \text{N/mm}$, which depends on the first three joint’s angular stiffness and its current configuration in the workspace. However, the angular stiffness for pitch, roll, and
yaw around the center of distal stage is only 4.0, 0.2, and 2.5 N·m/rad respectively. As the collision point is moving away from the tip of the end effector, the scaling factor \( l^2 \) in (3) makes the maximum achievable linear stiffness decrease quickly. For example, if the collision point is at (100, 0.0, 0.0) mm relative to the tip, the maximum linear stiffness becomes 0.4 N/mm only. In [10], Tan et al. experimentally obtained that the minimum stiffness required to simulate a hard wall is 24.2 N/mm. Therefore, the application designer has to pay special attention to the maximum achievable linear stiffness for a full tool-object haptic simulation. In fact, this is a generic problem for all 6-DOF haptic interfaces.

III. PROBLEM STATEMENTS

A. Control Point for Multi-finger Handling Posture

As discussed, the feedback force/torque \( F_t \) is computed relative to a holding point on the virtual tool while the real holding point (control point) on the end effector is needed for the rendering of \( F_t \). Ideally, the two holding points should be directly coupled together. Any changes of primary holding point should be reflected onto the virtual holding point inside the simulation and the control point for the update of motor Jacobian. As aforementioned, to derive a primary holding point from user’s handling posture on the tool in real-time is challenging, particularly for those involving multi-fingers and time-varying finger forces. From an application’s point of view, the spatial and force/torque trajectories from experts may be recorded for the guiding or the comparison of student’s trajectories in a surgical simulator. If the student’s handling of the tool is different from the expert, he/she will not get the same haptic perception from the VE as the expert does. To identify the resolution requirements for the control point, we need to know human sensing resolution in force and torque. In terms of kinesthetic force sensing, the differential threshold averages 7-10% over a force range of 0.5-200 N, and for force smaller than 0.5 N, the threshold increases to 15-27% [4]. Jandura and Srinivasan experimentally measured human performance in torque discrimination and control in [11]. They concluded that the just noticeable different (JND) for torque is around 12.7% when the reference torque was in the range of 60-90 mN·m for a pinch grasp. This is roughly to say that for a contact force of 1 N, humans can discriminate the torque magnitude around every 10 mN away from the pivot point.

However, in this paper, we only work with handling postures where the primary holding pivot point can be easily identified. We have fixed the control point at the center of the distal stage. For the direct haptic rendering method discussed in Section II, the feedback torque is always computed with this fixed control point. The user perceived force/torque feedback around the holding point will be naturally induced from the force/torque delivered to the center of the distal stage.

B. Device Inertia Effects on Force/torque Rendering

In any haptic simulations, we always hope that the requested force/torque can be faithfully transmitted to the user through the equipped joint motors. However, some factors which may affect this include motor dynamics, current amplifier characteristics, and arm structure [7]. Through experiments, we have found that the device inertia affects the perceived stiffness of the simulated objects non-uniformly. In this section, we discuss the inertia effects of the tip onto the rendering of the feedback. In Fig. 7a, a collision force \( f \) is acting on the stick. The equivalent wrench for \( F_c \) at the center of the distal stage and the holding point is

\[
F_c = [f_c \tau_c]^T = [f \ l \times f]^T, \tag{4}
\]

\[
F_h = [f_h \tau_h]^T = [f \ h \times f]^T. \tag{5}
\]

Let us assume wrench \( F_c \) is faithfully rendered around the center of the distal stage. If the end effector is at rest or moving at constant velocity, the user will feel the desired \( F_h \). However, this is not a usual case, particularly during the contact transition period. If the user holds the stick and moves towards the ball with an incoming acceleration \( a \), due to the inertia at the center of the distal stage, the actual force/torque generated at the user holding point is

\[
F_h' = [f_h' \tau_h']^T
= [f - ma \ \tau_c - (l - h) \times (f - ma)]^T \tag{6}
= [f - ma \ h \times f + (l - h) \times ma]^T
\]

Comparing (5) with (6), we can see that the translational force generated at the holding point \( f_h' \) is smaller than the desired translational force \( f_h \) by \( ma \), while the torque generated around the holding point \( \tau_h' \) is larger than the desired torque \( \tau_h \) by \((l - h) \times ma\). This unbalance force/torque pair will generate a fast and large clockwise rotation around the holding point and give the user a perception of a stiffer virtual ball than it should be.

On the other hand, if the collision point is between the holding point and the center of distal stage as shown in Fig. 7b, the situation is different. Now, the equivalent wrenches for

\[
\begin{align*}
\text{Fig. 6: Angular stiffness vs. linear stiffness} \\
\text{Fig. 7: Illustration of device inertia effects on the rendering of force/torque feedback around holding point}
\end{align*}
\]
The center of the distal stage is around 250 g. The translational inertia of the Freedom6S hand controller at the holding point is also important. According to the factory specification sheet, the primary holding point also plays a role here. It is interesting that the primary holding point is the one where the user feels a perception of a softer virtual ball than it should be. This is because the primary holding pivot point, which is the location where the potentiometer is mounted, is 0.5-1.8 N, so it can be easily actuated with human fingers without much distraction from the application itself. The holding point is visually displayed as three-orthogonal axes on the stick. With the visual display of the holding point inside the VE, the subject is able to know the relative position of the collision point and the primary holding point. A total of 5 subjects, with no known sensorimotor impairments with their hand or arm, took part in the experiments. Altogether, 6 levels of linear stiffness from 0.1 N/mm to 0.6 N/mm at a spacing of 0.1 N/mm are randomly assigned to the virtual ball during the experiments for each subject. As described above, the maximum achievable linear stiffness without vibration depends on the position of the collision point. Vibrations can occur for this 6-level stiffness, particularly when the collision point is far from the center of the distal stage. To protect the motors, the subjects were asked to leave the collision state once they feel abnormal vibrations. For the experiment, each subject is asked to hold the end effector using the thumb and the index finger, forming a pinch grasp. For each stiffness level assigned, the subject is asked to touch the virtual ball with different parts of the stick by holding the end effector at different locations. The experimental results are consistent with the above mathematical analysis. All subjects report softer stiffness when touching the ball with the collision point in between the holding point and the center of the distal stage. There were no detected motor vibrations for collision points on the top half of the stick for all the 6 levels. When the collision point was on the other side of the primary holding point, all subjects reported that it felt stiffer. For assigned stiffness over 0.3 N/mm, subjects felt vibrations when touching the ball with the lower part of the stick. It is possible that this stiffer stiffness sensation comes from these short duration vibrations. But the difference of the perceived stiffness is quite evident for all other cases. From the psychophysics point of view, studies in human stiffness perception show that the differential thresholds range from 8-22% [5] [12]. This is also to say that the inertia effects on the perceived stiffness cannot be ignored and needs compensation.

IV. PROPOSED METHODS AND RESULTS

Two methods are proposed to compensate for the device inertia effects. Both methods utilize the real-time measurements of the primary holding point on the end effector. This enables uniform stiffness perception of the virtual object instead of generating the fully desired feedback force/torque around the holding point. As discussed in the last section, when the virtual collision point is between the primary holding point and the center of the distal stage, the perceived stiffness of the virtual object is smaller than it should be because of the additional

\[ f = \begin{bmatrix} f_c \\ \tau_c \end{bmatrix}^T = \begin{bmatrix} f - l \times f \end{bmatrix}^T \]

But the actual induced force/torque around the holding point is

\[ F_h = \begin{bmatrix} f_h \\ \tau_h \end{bmatrix}^T = \begin{bmatrix} f - h \times f \end{bmatrix}^T. \]

Comparing (8) and (9), we can see that the translational force generated at the holding point \( f_h \) is still smaller than the desired translational force \( f_h \), but an additional term \( l \times \tau_h \) in \( \tau_h \) counterbalances the desired torque \( \tau \). If the incoming acceleration \( a \) is large enough, the user will even feel a clockwise rotation around the holding point as opposed to the expected counterclockwise rotation. Therefore, in this case, it gives the user a perception of a softer virtual ball than it should be. It is interesting that the primary holding point also plays a role here. According to the factory specification sheet, the translational inertia of the Freedom6S hand controller at the center of the distal stage is around 250 g and the rotational tensor is 0.17 gm\(^2\) for pitch and yaw, and 0.005 gm\(^2\) for roll. For an incoming acceleration of 1 m/s\(^2\), the inertia may generate a 0.25 N force which is definitely not negligible in haptic rendering. This problem also applies to other 6-DOF haptic interfaces.

C. Experiment Validation

To experimentally validate the effects of the device inertia, the example stick-on-ball application is chosen as a testbed. The experimental setup consists of a MPB Freedom6S hand controller interfaced with a PC running MS Windows XP. The PC is equipped with an Intel(R) Xeon 1700 MHz processor and 2 GB of RAM. A regular 19 inch flat CRT monitor is used for the graphic rendering without stereo support. Through the application’s user interface (UI) as shown in Fig. 8a, the user is able to modify the simulation’s parameters such as to manually set the holding point, and the stiffness of the virtual object, to enable/disable the real-time measurement of the primary holding point, etc.
term \(-ma\) in the force component and the additional term \((l + h) \times ma\) in the torque component. To compensate for the inertia in this case, we directly set the desired force/torque \(F_h\) at the center of the distal stage and it gives \(f'_c = f\) and \(\tau'_h = -(2h + l) \times f + (h + l) \times ma\). With some algebra manipulations, the induced force/torque around the holding point now becomes

\[
\begin{align*}
\dot{f}_h &= f - ma \\
\dot{\tau}_h &= -(2h + l) \times f + (h + l) \times ma 
\end{align*}
\]  

(10)

Referring to Fig. 7b, this is equivalent to moving the collision point away from the center of the distal stage by \(h\). This movement of the contact force \(f\) helps to balance out the inertia effects. If the collision point is not between the center of the distal stage and the holding point, we do not modify force/torque \(F_c\). Now in both cases, the user gets a stiffer stiffness perception of the virtual object than it should normally be. Since the human stiffness perception \(\text{JND}\) is in the range of 8-22\%, we expect that this artificial modification of the control force/torque will improve the uniform stiffness perception. The experimental results from 3 subjects show that the part where the users perceive a soft sensation due to the inertia indeed improved. One noticeable artifact is that there is a glitch due to the jump in the requested torque when the collision point is passing from one side of the holding point to the other.

In the second method, we will directly compensate for the inertia effects by estimating the acceleration of the control point. Referring to Fig. 7a, to transmit the desired force/torque \(F_h\) given in (5) around the holding pivot point, the modified \(F'_c = [f'_c \quad \tau'_h]\) with respect to the control point is given by

\[
\begin{align*}
f'_c &= f_c + ma \\
\tau'_h &= \tau_h - l \times ma 
\end{align*}
\]  

(11)

It can be easily verified that (11) also applies to the situation described in Fig. 7b. However in this case, the estimation accuracy of the translational inertia on the end tip, the rotational inertia around the holding point, and the acceleration information becomes very important. Since the device is not equipped with an accelerometer, the acceleration information has to be derived from the position measurements. An adaptive 4-state Kalman filter to estimate the acceleration of the end effector was proposed in [13] considering the human arm/hand trajectory behavior. This is left as the future work.

V. CONCLUSION AND FUTURE WORK

In this paper, we introduced the role of a user’s holding point in the current 6-DOF haptic rendering methods. We propose that the control point should be fixed for 6-DOF haptic rendering using direct rendering method. This ensures that regardless of how the tool is held by the user, correct and realistic force/torque feedback will be provided. However, this fixed control point does not directly work for the simulation based rendering method directly. We also briefly discussed the usefulness of the visual display of the primary holding point inside VE. We also studied the effects of the device inertia on the perception of stiffness properties assigned to virtual objects. A stick-on-ball simulation is used for the experimental verification. Both theoretical analysis and experimental results show that the perceived stiffness is related to the location of the collision point, the primary holding point, and the center of the distal stage. Due to device inertia, distinct stiffness levels of the same virtual object are sensed when the user touches it using different part of the tool. We have instrumented the end effector of a haptic interface with a membrane potentiometer to measure the user’s primary holding point in real-time. Two methods are proposed for inertia compensation. The first method targets the perception of uniform stiffness of the virtual object. The experimental results show the effectiveness of the method. But when the collision point is passing from one side of the holding point to the other side, there is a clear glitch because of the non-continuity of the requested torque sent to the control point. In the second method, we directly target the compensation of the device inertia by estimating the acceleration of the control point and the inertia of the end effector in real-time. A more thorough investigation of this method is left for future work.

ACKNOWLEDGMENT

The authors would like to thank Dr. Ian Sinclair for his assistance with the MPB Freedom 6S hand controller.

REFERENCES