

Investigating Evaluation Measures in Ant Colony Algorithms for Learning Decision Tree Classifiers

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Abstract—Ant-Tree-Miner is a decision tree induction algorithm that is based on the Ant Colony Optimization (ACO) meta-heuristic. Ant-Tree-Miner_M is a recently introduced extension of Ant-Tree-Miner that learns multi-tree classification models. A multi-tree model consists of multiple decision trees, one for each class value, where each class-based decision tree is responsible for discriminating between its class value and all other values present in the class domain (one vs. all). In this paper, we investigate the use of 10 different classification quality evaluation measures in Ant-Tree-Miner_M, which are used for both candidate model evaluation and model pruning. Our experimental results, using 40 popular benchmark datasets, identify several quality functions that substantially improve on the simple Accuracy quality function that was previously used in Ant-Tree-Miner_M.

I. INTRODUCTION

Decision trees [1], [2] are widely used in data mining as a comprehensible knowledge representation. They can be easily represented in a graphical form and also be represented as a set of classification rules, which generally can be expressed in the form of IF-THEN rules. In a decision tree, the internal nodes correspond to attribute tests (decision nodes) and the leaf nodes correspond to predicted class labels. In order to classify a case, the tree is traversed from the root node towards a leaf node by selecting branches according to internal nodes' tests, until a leaf node (class prediction) is reached.

Top-Down Induction of Decision Trees (TDIDT) is the most common approach in the literature for learning decision trees, and employs a *divide-and-conquer* approach: 1) select the best attribute to use as an internal node of the tree at a certain level; 2) divide the dataset into several subsets according to the branches (values) of the selected node (attribute); and 3) recursively apply the previous steps on each subset until all cases from the subset have the same class label or when another stopping criterion is satisfied, creating a leaf node to represent a class label to be predicted. The well-known ID3, C4.5 [3] and CART [4] algorithms follow such an approach for learning decision trees. Nonetheless, the divide-and-conquer approach represents a deterministic, greedy search strategy to create a decision tree; the selection of the best attribute is made locally at each iteration, without taking into consideration its influence over the subsequent iterations. This makes the algorithm vulnerable to local optima traps.

Ant Colony Optimization (ACO) [5] is a meta-heuristic for solving combinatorial optimization problems, inspired by the behaviour of biological ant colonies. Ant-Tree-Miner [6] is an ACO-based algorithm for inducing decision trees. Ant-Tree-Miner_M [7] is a recently introduced extension of Ant-Tree-Miner that learns multi-tree classification models. In essence, a multi-tree model consists of several class-based decision trees, where each tree is responsible for discriminating between a specific class value and all other values in the class domain. Besides its predictive effectiveness [7], the multi-tree model can provide the user with a potentially useful representation of the knowledge discovered from the dataset, by focusing on the specific patterns describing each class value and differentiating it from the other ones.

One of the most important aspects of the ACO algorithm is the choice of the quality measure used to evaluate a candidate solution to update pheromone. In this paper, we explore the use of various classification quality measures for evaluating the candidate multi-tree models constructed by the ants during the execution of the Ant-Tree-Miner_M algorithm. In addition, the same selected evaluation measure is also used as a criterion for model (tree) pruning. The aim of this investigation is to discover how the use of different evaluation measures affects the quality of the final output classifier in terms of predictive accuracy. In our experiments, we explore the use of 10 different classification measures, including Accuracy that was originally used by the Ant-Tree-Miner_M algorithm in [7], on 40 UCI repository [8] benchmark datasets.

II. REVIEW OF THE ANT-TREE-MINER ALGORITHM

ACO has been applied to classification [9], [10], [11] using a variety of different types of classification models, including classification rules [12], [13], [14], [15], [16], [17], neural networks [18], [19], [20], and various types of Bayesian network classifiers [21], [22], [23], [24].

Ant-Tree-Miner [6] is an ACO algorithm for learning decision trees. The Ant-Tree-Miner algorithm follows the traditional divide-and-conquer approach, except that an ACO procedure is used during the tree construction to select the nodes (attributes) of the tree. Instead of applying a greedy deterministic selection, Ant-Tree-Miner uses a stochastic process based on heuristic information and pheromone values. To create a candidate decision tree *DT*, an ant starts by selecting

an attribute from the construction graph. The probability of selecting an attribute is based on both the heuristic function value η and the pheromone amount τ .

Each entry in the pheromone matrix is represented by a triple $[E_{ij}, L, x_k]$, where E_{ij} is the edge representing the j -th attribute-condition of the attribute x_i in the construction graph, L is the level of the decision tree where E_{ij} appears and x_k is its destination attribute vertex. The level information of the edge is associated with an entry to discriminate between multiple occurrences of the same type of edge (i.e., the same attribute-condition) at different levels of the tree, either for occurrences in the same tree path—possible in the case of edges of continuous attribute vertices—or in different tree paths.

Once an attribute is selected to represent a decision node, branches corresponding to each attribute-condition are created. At this point, the training set is divided into one subset for each branch, where each subset contains the training cases satisfying the attribute-condition represented by the branch. When an ant follows a branch, it checks whether a leaf node should be added or if it should recursively add a sub-tree below its current branch. An ant chooses to add a leaf node if one of the following conditions occur:

- 1) the branch's subset is empty—i.e., no training case satisfies the branch's condition;
- 2) all cases in the subset have the same class label;
- 3) the subset size is smaller than or equal to the `min_cases_per_branch` user-defined value;
- 4) there are no more (unused) attributes to be selected.

If none of the above conditions is observed, the construction procedure is applied recursively to create a sub-tree given the subset of training cases.

When all ants have created a decision tree, the created decision trees are evaluated and the iteration-best tree (DT^{tbest}) is used to update pheromone values. The creation process is repeated until a user-defined maximum number of iterations is reached or the algorithm has converged (i.e., the pheromone values lead the algorithm to create the same solution). The pheromone update procedure is given by:

$$\tau_{(E,L,x_k)} = \begin{cases} \rho \cdot \tau_{(E,L,x_k)}, & \text{if } (E, L, x_k) \notin DT^{tbest} \\ \rho \cdot \tau_{(E,L,x_k)} + Q(DT^{tbest}), & \text{if } (E, L, x_k) \in DT^{tbest} \end{cases} \quad (1)$$

where ρ is the `evaporation_factor` parameter, $\tau_{(E,L,x_k)}$ is the pheromone entry associated with the triple (E, L, x_k) —where E is the attribute condition of the edge that this pheromone entry corresponds to, L is the tree level in which the edge occurs and x_k is the edge's destination attribute vertex—and $Q(DT)$ is the quality of the candidate constructed decision tree DT .

III. LEARNING MULTI-TREES WITH ACO ALGORITHM

A. Multi-tree Models

Unlike a decision tree classification model, which represents the induced knowledge from a given dataset as a tree model,

the multi-tree model represents the induced knowledge in several decision trees, one from each class value's perspective. More precisely, a multi-tree model MT consists of a set of separate local decision trees $\{DT_1, DT_2, \dots, DT_{|C|}\}$, where $|C|$ is the number of the available class values. DT_l is responsible for discriminating between class value l and all the other values in the class domain. In other words, each tree in the multi-tree model treats its related class value as the positive class, and all the other class values as one negative class. Hence, DT_l is concerned with classifying a case to one of two class values: one natural positive class value ($C = l$), and another artificial negative class value ($C \neq l$). Thus, the knowledge captured in each tree of a multi-tree model only describes the attribute-value relationships that are relevant to a specific class value, regardless of the other relationships that might be relevant to the other classes.

Therefore, for each DT_l , an induction algorithm will only focus on discovering the specific patterns that describe class value l , and will not get distracted by patterns related to other classes. This should make the induction process of DT_l more effective in terms of discriminating l from other class values. This is in contrast to the conventional decision tree induction algorithms that try to discriminate between all the class values in a single model.

In essence, in order to predict the label of a new test case x using a multi-tree classification model, x is classified using each tree DT_l in the model. Each DT_l produces a classification output: $P(C = l|x)$, which is the probability that x belongs to local positive class l . The outputs of the different trees in a multi-tree can take of the following forms:

- $P(C = l|x) > 0.5$ in only one tree in the set, then x is assigned to class l ;
- $P(C = l|x) > 0.5$ in multiple trees in the set, then x is assigned to the class value l of the tree that has the highest probability;
- $P(C = l|x) \leq 0.5$ for all the trees in the set, then x is also assigned to the class value l of the tree that has the highest probability.

B. Ant-Tree-Miner_M Variations

The ACO algorithm for learning multi-tree classifier has two variations: Ant-Tree-Miner_{ML} and Ant-Tree-Miner_{MI}. Ant-Tree-Miner_{ML} employs a local approach to build a multi-tree, in which each tree in the model is learned in a one-at-a-time fashion. In other words, there is no dependency between the processes of learning different trees in the model—each tree induction process is considered as a separate optimization problem, carried out by a separate ACO procedure.

The second algorithm, Ant-Tree-Miner_{MI}, follows an integrated approach, which is different from its local counterpart. A single run of ACO is used to build the whole solution; each ant builds a *complete* multi-tree classification model as a candidate solution at once. This is accomplished by building a candidate local DT_l for each class value l in each single ant trial, appending them to the current candidate multi-tree model. Unlike Ant-Tree-Miner_{MI}, which has to

completely finish building the local tree DT_i before starting to build DT_{i+1} , in Ant-Tree-Miner_{MI} the whole multi-tree model is constructed before performing the quality evaluation and pheromone update. In this case, the integrated approach is not concerned with the quality of each individual decision tree DT_i —in classifying the artificial training dataset D_i —per se, rather it is concerned with the quality of the complete multi-tree model when used to classify the original training set D .

In our previous work [7], we empirically evaluated these two algorithms against the results of the well-known CART and C4.5 decision trees induction algorithms, as well as the Ant-Tree-Miner algorithm. In addition, we compared our results to C4.5-MT, a greedy implementation for learning multi-tree models. The results showed that the two proposed ACO algorithms are statistically significantly better than the three greedy algorithms. Ant-Tree-Miner_{MI} produced overall better predictive accuracy results to its local counterpart and to the original Ant-Tree-Miner algorithm [7]. Moreover, predictions made by the multi-tree model involve a smaller number of terms in the produced rules, which contributes to the comprehensibility of the model. Therefore, the user needs to analyse a smaller number of attribute-value conditions in order to understand a prediction.

IV. INVESTIGATING DIFFERENT QUALITY MEASURES

We investigate several measures to evaluate the quality of the candidate solutions (i.e., multi-tree classification models) that are constructed by the ants during the ACO algorithm's execution. In addition, the same measure is used as a criterion to perform tree pruning in each of the two Ant-Tree-Miner_M algorithms. Note that the effectiveness of the final produced solution is tightly coupled with the choice of the “fitness” measure used to evaluate the candidate solution constructed during the ACO search. This is because the evaluation measure reflects the amount of the pheromone to be deposited on the construction graph to guide the ACO search towards the optimum solution. Specifically, the amount of pheromone deposited is proportional to $Q(\mathcal{M})$, as follows:

$$\tau(sc_i) = \tau(sc_i) + [\tau(sc_i) \times Q(\mathcal{M})] \quad \forall sc_i \in |\mathcal{M}| \quad (2)$$

where \mathcal{M} is a candidate (iteration-best) solution, which is a local decision tree DT as in Ant-Tree-Miner_{ML} or a complete multi-tree model MT as in Ant-Tree-Miner_{MI}. sc_i is the i -th solution component in the construction graph belonging to the constructed solution \mathcal{M} .

Measuring the predictive performance of a classifier is mainly based on the counts of the cases (learning cases in the training phase and test cases in the test phase) correctly and incorrectly predicted by the classifier. These counts are organized in a tabular structure known as a *confusion matrix*, as represented in Table I. The entries of the confusion matrix are defined as follows:

TP The count of cases that belong to the positive class and are predicted as positive (true positives).

FP The count of cases that belong to the negative class and are predicted as positive (false positives).

TABLE I
CONFUSION MATRIX.

		Predicted Class	
		Positive	Negative
Actual Class	Positive	TP	FN
	Negative	FP	TN

TN The count of cases that belong to the negative class and are predicted as negative (true negatives).

FN The count of cases that belong to the positive class and are predicted as negative (false negatives).

SM The total count of cases (TP + FP + TN + FN).

The confusion matrix is computed for classification model \mathcal{M} using the training set D . Various classification quality evaluation measures can be formulated using the elements of the confusion matrix. The following presents the 7 confusion matrix-based measures investigated in our work.

- 1) **Accuracy** (Equation 3) - The baseline measure which is used in the original Ant-Tree-Miner_M [7] to evaluate the candidate constructed multi-tree models. Accuracy measures the ratio of the count of correctly classified cases (TP + TN) over the sum of counts of all the cases.

$$Accuracy = \frac{TP + TN}{SM} \quad (3)$$

- 2) **F-measure** (Equation 5) - Widely used in the context of information retrieval and text classification systems. It calculates a harmonic mean between precision and recall:

$$Precision = \frac{TP}{TP + FP} \quad Recall = \frac{TP}{TP + FN} \quad (4)$$

and

$$F - measure = \frac{2 \cdot Precision \cdot Recall}{Precision + Recall} \quad (5)$$

- 3) **Sensitivity × Specificity** (Equation 6) - Sensitivity measures the ratio of the count of true positives to the count of all the positive cases, and specificity measures the ratio of the count of true negatives to the count of all the negative cases.

$$Sensitivity \times Specificity = \frac{TP}{TP + FN} \cdot \frac{TN}{TN + FP} \quad (6)$$

- 4) **Jaccard Coefficient** (Equation 7) - It calculates the similarity between sample sets. In the classification context, it measures the accuracy only with respect to the true positive count, neglecting the true negatives.

$$Jaccard = \frac{TP}{TP + FP + FN} \quad (7)$$

- 5) **M-estimate** (Equation 8) - a parametric function with parameter m :

$$M - estimate = \frac{TP + m \cdot \frac{TP}{SM}}{TP + FP + m} \quad (8)$$

We set m to 22.4 as recommended by Janssen and Fürnkranz in [25].

- 6) Kappa (Equation 9) - Kappa Statistic, a well-known predictive effectiveness measure, compares the accuracy of the system to the accuracy of a random system. Total accuracy is an observational probability of agreement and random accuracy is a hypothetical expected probability of agreement under an appropriate set of baseline constraints.

$$Kappa = \frac{Accuracy - RandomAccuracy}{1 - RandomAccuracy} \quad (9)$$

where

$$RandomAccuracy = \frac{(TN+FP) \cdot (TN+FN) + (FN+TP) \cdot (FP+TP)}{(SM)^2} \quad (10)$$

- 7) Klösigen (Equation 11) - A parameteric function with parameter ω . When $\omega = 0$, the measure acts as precision (Equation 4). As ω increases the measure acts in a manner similar to recall (Equation 4). The transition from one to the other is not linear, and as ω increases further it starts acting as coverage.

$$Klosigen = \left(\frac{TP + FP}{SM} \right)^\omega \cdot \left(\frac{TP}{TP + FP} - \frac{TP + FN}{SM} \right) \quad (11)$$

We used an ω value of 0.43 in our experiments, as recommended by Janssen and Fürnkranz in [25].

In addition to the confusion matrix-based measures, we used three more classification quality measures that are based on the probability of the classified class. In more details, let m denote the number of classes, \hat{c} denote the true (correct) class for a given case x , and c denote the class that is predicted by the classification model \mathcal{M} . The output of the classifier is an m -dimensional probability vector p_1, p_2, \dots, p_m . Hence, the predicted class c will be the label k of the output of the model \mathcal{M} with the highest probability score p_k . We will use the notation $f(\mathcal{M}|x)$ to refer to the value of the classification measure f on \mathcal{M} given case x .

- 8) Class Probability Error (CPE), also known as Probabilistic Accuracy (Equation 12) - This is a probabilistic alternative to the accuracy measure. For a given case x ,

$$CPE(\mathcal{M}|x) = 1 - p_{\hat{c}} \quad (12)$$

CPE computes the difference between the actual (ideal) probability value (1.0) and the predicted probability $p_{\hat{c}}$ of the correct class \hat{c} . Hence, CPE favours models that correctly classify the cases with higher probability. This is unlike Accuracy, which counts any classified case with probability of 0.5 or higher for the true class as a true positive.

The pheromone amount to be deposited is based on the evaluation of the entire training set:

$$Q_{CPE}(\mathcal{M}|D) = 1 - \frac{1}{|D|} \sum_{x \in D} CPE(\mathcal{M}|x) \quad (13)$$

- 9) Mean Squared Error (Equation 14) - MSE is another widely used error measure. For a given pattern x :

$$MSE(\mathcal{M}|x) = (1 - p_{\hat{c}})^2 + \sum_{k:k \neq \hat{c}}^m (p_k)^2 \quad (14)$$

MSE computes the mean squared difference between the predicted probability of each class and its actual (ideal) probability value. For the correct class $p_{\hat{c}}$, the ideal probability value is 1.0, while it is 0.0 for the other classes. Note that not only does MSE favour the models that produce a higher probability for the true class, but it also favours the models that produce the lowest probabilities for the other classes.

The pheromone amount to be deposited is based on the evaluation of the entire training set, as follows:

$$Q_{MSE}(\mathcal{M}|D) = 1 - \frac{1}{|D|} \sum_{x \in D} MSE(\mathcal{M}|x) \quad (15)$$

- 10) Bayesian Information Reward (Equation 16) - For a given pattern x , we use a variation of Bayesian Information Reward BIR , defined as:

$$BIR(\mathcal{M}|x) = \frac{1}{m} \sum_{c=1}^m IR_c(\mathcal{M}|x) \quad (16)$$

where

$$IR_c(\mathcal{M}|x) = \begin{cases} 1 - \frac{\log(p_c)}{\log(p'_c)} & \text{if } c = \hat{c} \text{ (reward)} \\ \frac{\log(1-p_c)}{\log(1-p'_c)} & \text{if } c \neq \hat{c} \text{ (penalty)} \end{cases} \quad (17)$$

where p'_c represents the prior probability of class c , which is the ratio of the number of cases in the learning set with class label c to the total number of cases in the learning set, and m is the total number of the classes. Note that the first branch in the conditional Equation (17) is the reward value, where the predicted class c is the same as the true (correct) class \hat{c} , while the second branch is the penalty value, where the predicted c is not the same as the true class \hat{c} .

Not only does the Bayesian Information Reward measure take into account the true class $p_{\hat{c}}$, it also accounts for the prior probability p'_c of the predicted class in the dataset. This makes BIR more robust to class imbalance situations, where one (or more) class values have high occurrence in a given dataset compared to the other values. That is, the lower the frequency of the correctly predicted class in the dataset, the higher the reward. Similarly, the higher the frequency of the misclassified class in the dataset, the higher the penalty.

The pheromone amount to be deposited is based on the evaluation of the entire training set,

$$Q_{BIR}(\mathcal{M}|D) = \frac{1}{|D|} \sum_{x \in D} [\phi_1 + BIR(\mathcal{M}|x) / \phi_2] \quad (18)$$

where the parameters ϕ_1 and ϕ_2 are used to adjust the actual amount of pheromone to be deposited. The first

parameter makes sure that the Q_{BIR} value is greater than 0, while the second parameter scales the Q_{BIR} value. In our experiments, we set $\phi_1 = \phi_2 = 50/m$.

It is crucial to emphasize that there are two different quality evaluation operations. The first is the one used in the testing phase to evaluate the classification quality of the final output classifier on a test set *unseen* during training, which is fixed and used to evaluate several algorithms or several variations of an algorithm. The second is the one used during the training phase for evaluating each candidate classifier constructed by an ant on a validation set.

Candidate solutions are evaluated during the training phase to perform pheromone update for guiding the search to build a high quality classifier as a final output. In the experiments, the former is fixed to *Accuracy* in the testing phase, while the latter used the various aforementioned measures in the training phase to examine their effectiveness with respect to maximizing the *Accuracy* test measure. The next section describes the experimental methodology in detail.

V. EXPERIMENTAL RESULTS

In our experiments, we modify Ant-Tree-Miner_M in two ways. First, We remove the heuristic component from the probabilistic state transition formula. The reason behind this is to isolate the effect of the quality measure and to make sure that only the evaluation measure will affect the ants' decisions and guide the search through the pheromone amounts deposited. Second, we only perform the pruning operation on the final converged-on solution, rather than on each candidate solution, in order to reduce the algorithm's computational time and again to amplify the effect of the quality measures being compared.

The performance of classification quality measures was evaluated using 40 public-domain datasets from the well-known UCI (University of California at Irvine) dataset repository [8]. The parameter settings used in our experiments are the default values used in [6].

The experiments were carried out using a well-known *stratified* 10-fold cross-validation procedure [1]. This means that each dataset is divided into ten mutually exclusive partitions (folds), with roughly the same class distribution in each partition. Then, the algorithm is run ten times, where each time a different partition is used as the test set and the other nine partitions are collectively used as the training set. The predictive performance reported for each evaluation measure is computed as the average value of the *Accuracy* on the test set across the runs of the 10 folds.

Table II reports the test set predictive accuracy results for Ant-Tree-Miner_{ML} for the 10 quality evaluation measures described in Section IV: *Accuracy* (ACC), *Probabilistic Accuracy* (PR-A), *Mean Squared Error* (MSE), *Bayesian Information Reward* (BIR), *Jaccard* (JAC), *F-measure* (F-M), *Kappa* (KAP), *M-estimate* (M-ES), *Sensitivity-Specificity* (S-S), and *Klösgen* (KLO). For each dataset, the average test set accuracy, aggregated over the 10 cross-validation folds,

is reported for each measure; the highest-accuracy achieved for each dataset is shown in boldface. The penultimate row of the table reports a count of the number of datasets for which each measure achieved the highest accuracy, and the last row reports the average rank of each measure. To obtain the average rank, the ten measures are first ranked for each dataset individually, with the best measure being given a rank of 1, and the worst a rank of 10. In the case of ties, the tied measures are given the average of the spanned ranks. Finally, the ranks are averaged over the datasets to obtain the overall average ranks.

As the table indicates, the best average rank was obtained by *Mean Squared Error*, with an average rank of 4.49 and the best accuracy in 7 datasets, followed in second-place by *Kappa* with a rank of 4.55 and the best accuracy in 6 datasets, then in third-place by *M-estimate* with a rank of 4.80 and the best accuracy in 4 datasets. In fourth-place was *Jaccard* with an average rank of 4.89 and the best accuracy in 9 datasets, followed by *F-measure* in fifth-place with a rank of 4.99 and the best accuracy in 10 datasets. In sixth-place was *Accuracy* (the original quality evaluation measure of Ant-Tree-Miner_{ML}) with a rank of 5.09 and the best accuracy in 5 datasets, followed in seventh-place by *Probabilistic Accuracy* with a rank of 5.26 and the best accuracy in 3 datasets, then in eighth-place by *Sensitivity-Specificity* with a rank of 5.59 and the best accuracy in 10 datasets. In the last two places were *Klösgen* with an average rank of 6.42 and the best accuracy in a single dataset, and *Bayesian Information Reward* with a rank of 8.93 and the best accuracy in 3 datasets.

Table IV reports the results of applying a Friedman test with the Holm *post hoc* test at the conventional 0.05 threshold to the results of Table II, using *Mean Squared Error* (the measure with the best average rank) as the control measure. The Friedman statistic χ_F^2 is determined to be 69.28 with 9 degrees of freedom, corresponding to a p value of 7.0E-11. Thus, we can reject the null hypothesis and proceed with the *post hoc* tests. For each measure, the second column of the table reports the average rank, the third column reports the p value of the statistical test when the measure is compared to the control measure, and the last column reports the Holm critical value. Statistically significant p values are shown in boldface. The table indicates that *Mean Squared Error* is significantly better than two of the other measures: *Klösgen*, and *Bayesian Information Reward*.

Table III reports the test set predictive accuracy results for Ant-Tree-Miner_{MI} for the same 10 quality evaluation measures, and follows the format of Table II. We can see that there are many similarities, but also a few differences between the pattern of results for Ant-Tree-Miner_{MI} and Ant-Tree-Miner_{ML}. For Ant-Tree-Miner_{MI}, the highest average rank was again obtained by *Mean Squared Error*, with an average rank of 4.41 and the best accuracy on 8 datasets. The second-best average rank was a tie between *Probabilistic Accuracy*, which had a rank of 4.57 and the best accuracy

TABLE II
TEST SET PREDICTIVE ACCURACY (%) FOR EACH OF THE QUALITY MEASURES FOR ANT-TREE-MINER_{ML}.

dataset	ACC	PR-A	MSE	BIR	JAC	F-M	KAP	M-ES	S-S	KLO
annealing	92.93	94.05	92.79	76.26	91.21	80.73	90.29	91.67	81.15	81.63
audiology	78.33	77.50	77.50	33.33	74.17	80.83	80.83	79.17	70.00	70.00
automobile	70.76	69.36	72.79	32.74	74.07	69.29	69.31	69.79	56.74	52.29
balance	71.83	67.83	70.17	46.67	69.00	67.00	69.17	71.50	73.67	70.00
breast-l	75.29	76.60	74.47	70.13	75.09	76.95	75.60	76.45	76.06	75.91
breast-p	72.08	71.71	67.21	76.29	67.11	72.68	68.63	70.11	75.24	74.79
breast-tissue	58.73	59.82	58.55	28.36	60.64	58.64	61.73	55.64	56.73	60.36
breast-w	92.80	93.86	92.79	62.74	92.28	94.56	93.51	92.80	92.98	94.20
car	92.81	92.51	93.45	70.76	91.70	93.22	92.87	91.17	89.12	88.71
credit-a	81.16	85.07	84.06	55.51	83.62	83.19	84.35	84.78	86.67	84.06
credit-g	71.00	72.30	72.80	70.00	70.80	71.40	71.50	72.10	70.70	69.60
cylinder	71.91	72.69	73.23	58.00	74.88	71.17	69.12	74.53	65.05	68.03
dermatology	94.81	94.79	92.88	30.60	92.33	93.15	94.81	92.04	90.16	87.38
ecoli	81.27	78.92	81.00	42.57	77.73	65.53	78.91	80.39	71.47	69.33
glass	70.85	62.41	67.43	38.29	65.64	67.93	69.84	67.97	51.84	50.15
hay	61.54	60.77	62.31	38.46	63.85	60.77	62.31	57.69	62.31	61.54
heart-c	52.82	54.18	52.49	54.15	54.76	52.82	53.16	54.55	55.80	52.83
heart-h	60.97	64.01	63.34	63.70	61.22	62.30	64.41	63.00	64.42	63.34
hepatitis	78.71	80.62	76.75	79.33	80.62	76.75	75.50	80.00	82.54	78.63
horse	83.26	82.37	83.33	66.67	83.54	85.00	82.62	83.26	82.72	80.96
ionosphere	87.62	87.92	89.36	64.48	89.04	90.53	92.54	89.09	87.39	88.78
iris	94.00	92.67	93.33	45.33	95.33	94.00	93.33	92.67	91.33	93.33
liver-disorders	65.75	63.13	62.87	57.98	63.21	66.04	64.62	61.98	67.51	62.34
lymphography	78.48	77.86	79.24	54.76	73.76	79.24	79.14	80.43	70.90	64.90
monks	63.64	62.91	63.64	63.64	63.64	63.64	63.09	63.09	63.64	62.91
parkinsons	86.24	84.05	89.21	75.39	89.26	89.79	87.16	86.63	87.21	87.21
pima	70.43	71.08	72.53	65.11	70.17	73.82	70.03	72.53	71.35	72.65
pop	75.00	75.00	75.00	75.00	75.00	75.00	75.00	75.00	75.00	75.00
segmentation	94.72	94.31	93.61	13.99	95.30	88.82	94.72	94.76	60.15	57.01
s-heart	71.85	71.11	72.96	55.56	74.44	72.22	76.30	74.44	77.41	75.19
soybean	77.24	78.97	81.72	13.79	77.59	82.76	77.24	73.79	53.45	52.76
thyroid	89.33	92.10	94.39	69.81	93.46	90.69	93.53	93.46	91.62	92.60
transfusion	69.38	71.46	73.14	71.74	70.81	70.40	71.09	72.43	71.17	72.23
ttt	88.42	87.47	88.21	65.26	86.63	87.79	88.95	87.16	88.32	85.16
vehicle	68.20	67.02	68.45	25.77	70.56	67.61	69.27	70.69	56.85	64.17
vertebral-column-2c	79.68	79.35	77.42	67.74	82.26	82.26	80.65	78.39	80.00	80.32
vertebral-column-3c	79.68	83.55	79.35	48.39	78.39	78.06	78.06	81.29	77.74	80.00
voting	95.22	94.60	94.88	85.88	95.56	93.89	94.57	93.95	94.15	94.29
wine	93.86	90.52	94.97	39.93	91.60	92.12	93.79	91.60	87.12	86.60
zoo	96.25	96.25	97.50	55.00	93.75	97.50	97.50	98.75	98.75	97.50
#wins	5	3	7	3	9	10	6	4	10	1
rank (avg)	5.09	5.26	4.49	8.93	4.89	4.99	4.55	4.80	5.59	6.42

on 6 datasets, and Kappa which had the same rank and the best accuracy on 4 datasets. It is interesting that Kappa also had the second-best ranking for Ant-Tree-Miner_{ML}.

In fourth-place was Accuracy with a rank of 4.77 and the best accuracy on 8 datasets, followed in fifth-place by Jaccard with a rank of 4.96 and the best accuracy on 7 datasets. In sixth-place was Sensitivity-Specificity with a rank of 5.73 and the best accuracy on 7 datasets, followed in seventh-place by F-measure with a rank of

5.83 and the best accuracy on 3 datasets. In eighth-place was M-estimate with a rank of 6.04 and the best accuracy on 3 datasets, followed in ninth-place by Klösgen with a rank of 6.15 and the best accuracy on 5 datasets. Finally, in last place was Bayesian Information Reward with a rank of 7.96 and the best accuracy on 5 datasets. Interestingly, the two worst-ranked measures are the same for the two algorithms.

Table V reports the results of applying a Friedman test with the Holm *post hoc* test at the conventional 0.05 threshold to the

TABLE III
TEST SET PREDICTIVE ACCURACY (%) FOR EACH OF THE QUALITY MEASURES FOR ANT-TREE-MINER_{MI}.

dataset	ACC	PR-A	MSE	BIR	JAC	F-M	KAP	M-ES	S-S	KLO
annealing	95.44	94.63	94.75	76.72	78.19	77.41	78.09	77.51	78.21	77.06
audiology	85.00	85.83	86.67	65.00	65.00	71.67	68.33	66.67	70.83	70.00
automobile	79.48	77.00	77.00	57.67	55.24	57.14	60.98	59.64	56.21	54.64
balance	79.00	68.00	66.17	58.00	73.00	73.00	75.50	74.50	76.67	74.00
breast-l	80.02	79.12	78.50	70.13	79.86	79.94	79.59	78.81	79.28	78.58
breast-p	66.66	73.26	71.74	76.29	69.26	66.13	72.79	70.68	65.08	71.16
breast-tissue	64.45	60.55	59.45	59.73	65.55	56.73	60.55	62.27	56.91	48.55
breast-w	91.22	93.51	93.15	62.74	92.97	92.80	92.80	92.27	92.80	91.39
car	94.80	93.68	93.68	71.52	91.99	92.51	91.87	92.16	91.52	90.99
credit-a	81.88	82.61	81.30	84.06	80.87	80.72	80.87	82.17	83.62	84.06
credit-g	69.30	69.40	70.10	70.00	71.30	70.30	70.10	66.90	68.00	70.10
cylinder	73.98	73.95	73.41	58.00	74.86	68.80	71.91	73.79	64.85	67.45
dermatology	95.08	94.55	94.02	30.60	81.70	84.72	86.34	80.86	81.69	76.44
ecoli	78.57	78.59	79.48	65.21	69.35	69.08	70.25	63.72	60.73	67.58
glass	67.56	69.90	70.85	65.57	63.69	69.34	70.29	62.85	63.82	60.69
hay	63.08	60.77	60.77	38.46	63.85	61.54	64.62	63.85	65.38	65.38
heart-c	47.20	50.49	46.28	54.15	52.15	47.84	53.53	50.83	52.17	52.49
heart-h	61.67	62.02	63.05	63.70	59.63	62.36	64.75	61.62	61.69	63.72
hepatitis	78.17	80.04	80.58	79.38	81.42	80.00	80.79	79.38	83.83	80.08
horse	83.59	82.10	82.74	69.58	83.61	81.86	82.71	83.51	81.52	83.80
ionosphere	89.10	89.70	87.35	64.48	87.93	90.25	88.53	90.49	85.29	82.61
iris	92.67	94.67	94.67	33.33	92.67	92.67	94.67	92.67	92.67	74.67
liver-disorders	59.93	60.32	61.17	57.98	61.72	62.55	61.71	63.72	63.76	63.66
lymphography	77.00	71.76	73.24	54.76	73.67	75.76	78.52	58.76	71.67	74.52
monks	61.45	62.73	63.64	63.64	62.91	63.27	62.91	63.64	63.09	62.36
parkinsons	86.63	89.76	86.58	75.39	84.50	84.66	86.71	82.58	81.47	88.11
pima	69.12	70.18	68.62	65.11	69.67	67.57	67.70	70.17	70.29	71.34
pop	73.75	75.00	75.00	75.00	75.00	75.00	75.00	75.00	75.00	73.75
segmentation	94.93	95.43	94.91	13.99	79.71	84.37	85.32	72.20	76.56	63.91
s-heart	75.19	76.30	75.19	67.04	74.44	70.74	76.67	67.41	78.52	73.70
soybean	86.21	85.17	86.55	49.66	57.24	55.17	50.69	46.21	44.48	63.45
thyroid	93.05	91.65	92.55	69.81	93.01	91.65	93.01	92.08	92.51	93.01
transfusion	70.53	70.48	70.73	71.49	69.95	69.99	70.01	70.76	71.84	71.71
ttt	89.05	89.37	88.42	65.26	91.05	91.16	90.00	89.37	89.89	91.16
vehicle	68.31	66.79	67.60	25.77	69.86	65.38	67.49	67.48	54.49	49.41
vertebral-column-2c	79.35	78.06	79.68	67.74	81.29	80.00	80.32	80.00	80.97	78.06
vertebral-column-3c	78.39	77.74	81.61	48.39	82.90	80.32	76.45	73.87	77.42	68.06
voting	93.23	94.24	94.53	88.73	93.30	94.88	94.26	94.29	92.97	94.23
wine	89.90	91.57	92.12	39.93	91.63	88.27	89.38	91.08	92.22	80.82
zoo	97.50	97.50	97.50	95.00	95.00	91.25	93.75	93.75	93.75	91.25
#wins	8	6	8	5	7	3	4	3	7	5
rank (avg)	4.77	4.57	4.41	7.96	4.96	5.83	4.57	6.04	5.73	6.15

results of Table III, again using Mean Squared Error (the measure with the best average rank) as the control measure. The Friedman statistic χ_F^2 is determined to be 46.43 with 9 degrees of freedom, corresponding to a p value of 5.0E-7. Thus, we can reject the null hypothesis and proceed with the *post hoc* tests. Table V follows the same format as Table IV and indicates that MSE is significantly better than a single measure: Bayesian Information Reward.

VI. CONCLUDING REMARKS

Ant-Tree-Miner_M is a recently introduced algorithm that employs the ACO meta-heuristic to induce multi-tree classification models. This paper has explored the effect of using 10 different classification quality measures for evaluating the candidate models constructed by the ants and updating pheromone during the training phase of the ACO algorithm. The effect of using these quality measures in the training phase was assessed according to their effectiveness in producing

TABLE IV

RESULTS OF THE FRIEDMAN TEST WITH THE HOLM *post hoc* TEST, AT THE 0.05 SIGNIFICANCE LEVEL, FOR THE PREDICTIVE ACCURACY RESULTS REPORTED IN TABLE II.

measure	rank	<i>p</i>	Holm
Mean Squared Error (control)	4.49	–	–
Kappa	4.55	0.926	0.05
M-estimate	4.80	0.644	0.025
Jaccard	4.89	0.555	0.01666
F-measure	4.99	0.460	0.0125
Accuracy	5.09	0.375	0.01
Probabilistic Accuracy	5.26	0.252	0.00833
Sens.-Spec.	5.59	0.104	0.00714
Klösigen	6.42	0.004	0.00625
BIR	8.93	5.6E-11	0.00555

TABLE V

RESULTS OF THE FRIEDMAN TEST WITH THE HOLM *post hoc* TEST, AT THE 0.05 SIGNIFICANCE LEVEL, FOR THE PREDICTIVE ACCURACY RESULTS REPORTED IN TABLE III.

measure	rank	<i>p</i>	Holm
MSE (control)	4.41	–	–
Kappa	4.57	0.810	0.05
Probabilistic Accuracy	4.57	0.810	0.025
Accuracy	4.77	0.592	0.01666
Jaccard	4.96	0.417	0.0125
Sens.-Spec.	5.73	0.053	0.01
F-measure	5.83	0.037	0.00833
M-estimate	6.04	0.016	0.00714
Klösigen	6.15	0.010	0.00625
BIR	7.96	1.6E-7	0.00555

classifiers with a high predictive performance in the testing phase, using Accuracy as a fixed predictive performance evaluator.

Empirical evaluation on 40 UCI datasets has shown that the performance of different quality measures varies substantially across different datasets. However, the Mean Squared Error and Kappa measures obtained the best overall average predictive performance, while Bayesian Information Reward and Klösigen obtained the worst overall average predictive performance. One possible research direction is to use an ensemble of several quality measures in the same learning procedure, which is left for future work.

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