

# HeMI++: A Genetic Algorithm based Clustering Technique for Sensible Clusters

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**Abstract**—We propose a new clustering technique called HeMI++. It uses cleansing and cloning operations that help to produce sensible clusters. HeMI++ learns necessary properties of a good clustering solution for a dataset from a high-quality initial population, without requiring any user input. It then disqualifies the chromosomes that do not satisfy the properties through its cleansing operation. In the cloning operation, HeMI++ replaces the chromosomes by high-quality chromosomes already found in the initial population. We compare HeMI++ with six (6) existing techniques on twenty (20) publicly available datasets using the Tree Index metric. Our experimental results indicate a clear superiority of HeMI++ over existing methods. We also apply HeMI++ on a brain dataset and demonstrate its ability to produce sensible clusters.

**Keywords**—data mining, clustering, genetic algorithms, artificial intelligence (AI)

## I. INTRODUCTION

### A. Clustering

Clustering is a well-known and an important technique that aims to group the similar records in one cluster and dissimilar records in different clusters [1-6]. Clustering has enhanced data analysis in a wide range of areas such as business [11], machine learning [12] social network analysis [13] and medical imaging [14].

K-means [5] is among the top ten most used clustering techniques [15] for its simplicity and a low complexity of  $O(dn)$  time where  $n$  is the size of the data set and  $d$  is the dimension. Although it is popular for its simplicity, it also has several well-known drawbacks. Fundamentally, K-means is statistically biased (even on data from a mixture of multivariate normal distributions with equal variance and just one dimension, K-means converges to incorrect means). Another issue commonly attributed to K-means is its requirement of a user-defined number ( $k$ ) of clusters [6, 16]. In reality, it can be difficult for a user (data analyst) to estimate the suitable number of clusters in advance.

Because K-means is essentially a hill-climber/gradient descent search method on a least square's loss, K-means has a tendency to converge to poor local optima [10,16,17]. The random selection of the initial cluster centers in K-means is also considered to be a major drawback since it often results in a poor-quality final clustering solution [6,7]. Arthur and

Vassilvitskii [6] proposed a clustering technique called K-means++ that shows a theoretical competitive ratio if initialisation is cleverly used. However, experimental evaluations show that this variant does not alleviate K-means problems in practice [7].

To overcome these limitations in recent years, many evolutionary algorithms such as stochastic search [18], simulated annealing [19] and genetic algorithms [2-4,7] for clustering have been proposed that achieve encouraging results.

Genetic algorithms (GA) use randomised search and optimisation techniques emulating the concepts of natural activity of genes, individual selection, and the evolutionary process [2-4,7]. Typically, in GA for clustering, a chromosome is an encoding of a clustering solution, and a gene within a chromosome corresponds to a vector that encodes the centre of a cluster.

However, there has some limitations on the existing GA-based clustering techniques. Typically, in the initial population, the number of genes of a chromosome are generated randomly. The genes are also selected randomly from a dataset instead of careful consideration [3,4]. Carefully genes selection increases the possibility of getting high-quality chromosome in the initial population (recall the theoretical result of K-means++). Having high-quality chromosomes in the initial population improves speed as it typically reduces the algorithm's number of iterations [2].

Rahman and Islam [2] presented a GA-based clustering technique known as GenClust that produces high-quality chromosomes in the initial population. However, users must provide a set of radius values for the chromosomes in the initial population. It can be difficult for a user to provide a suitable set of radius values.

Our previous technique, HeMI [7] produces high-quality chromosomes in the initial population without requiring any user-defined parameter and produces good-quality clustering results. We recently proposed a genetic algorithm-based clustering technique called GenClust++ [20] where we took a slightly similar approach for the initial population of HeMI. In the initial population, GenClust++ uses K-means [5] or K-means++ [16] multiple times with different values for the number  $k$  of clusters. That is, each value in  $\{2, 3, \dots, 10\}$  is used as the number ( $k$ ) of clusters for K-means or K-

means++. Thus, at least nine different clustering solutions progress in GenClust++ to a first ranking and culling phase. The initial population is probabilistically elected under a regime where chromosomes with higher cluster quality have greater chance to survive.

However, unlike GenClust++, HeMI does not select the initial chromosomes probabilistically, instead, HeMI selects only the best chromosomes based on their fitness values. Moreover, HeMI++ generates 50% of the initial population from a *deterministic phase* and 50% from a *random phase*. In the *deterministic phase*, HeMI picks the initial population from the pool of chromosomes obtained through K-means using the value of  $k$  ranging from 2 to 10. In many data sets, the true number of clusters is more than 10. To handle such situations, in the *random phase* HeMI generates the initial population randomly with the value of  $k$  ranging from 2 to  $\sqrt{n}$  (where  $n$  is the number of records in a dataset).

However, HeMI also has some limitations. Although it produces high-quality chromosomes in the initial population, it does not take full advantage of them since they are not used in any other genetic operations. Through our intelligent use of the high-quality initial population, the genetic operations could be made more effective. It also does not use any data-driven approach to learn the necessary properties of sensible clusters. Sometimes it produces non-sensible clustering solutions. An example, of a non-sensible clustering solution can be two clusters where one cluster has only one record and the other cluster has all other records. We discuss this in the paper as we go.

Earlier, we showed [8] that recent clustering techniques such K-means [5], K-means ++ [6], AGCUK [3], GAGR [4], GenClust [2] and HeMI [7] produces non-sensible cluster: they can obtain a huge number of clusters, and sometimes they derive only two clusters, with one cluster holding one record, and the other cluster contains all remaining records. Interestingly, these clustering solutions often attain high fitness values for existing evaluation criteria. Here, we propose a new clustering technique called HeMI++ that produces sensible clusters with high fitness values.

### B. Main contributions of this study

In this paper we propose a new clustering technique called **HeMI++**. HeMI++ is inspired by our previous techniques called CSCLust [8] and HeMI [7]. However, HeMI++ has significant differences from those methods [7, 8] as follows.

Technical contributions:

- The use of multiple streams in HeMI++:
  - CSCLust did not use multiple streams.
  - HeMI used multiple streams, but it did not learn the good clustering property from a data set and did not apply that knowledge for producing good quality clusters.
  - HeMI++ uses multiple streams; like HeMI and unlike CSCLust. Unlike HeMI, it learns the good clustering property from a data set and applies that to produce clustering solutions.

Learning properties of good clustering solutions:

- HeMI did not learn the properties of good clustering solutions.
- CSCLust learnt some properties of good clustering solutions by applying the DB-Index [26] on the initial population. However, this approach was problematic since the selection was biased by the inductive principle of the DB-Index.
- HeMI++ learns properties of a good clustering solution through a new approach (without using the DB-Index), and then applies the knowledge in producing its clustering solutions.

Experimental contributions:

- Comparison with more techniques and data sets
  - We test HeMI++ against six other existing techniques on twenty (20) natural data sets.
  - CSCLust was compared with five existing techniques on ten (10) data sets.
- Complexity analysis:
  - We also analyze the complexity of HeMI++ and compare it with six other existing techniques, whereas in CSCLust we did not present any complexity analysis.

In that follows, the proposed technique is described in Section II. In Section III, we discuss experimental results and Section IV provides the concluding remarks.

## II. OUR TECHNIQUE

### A. Main Components of HeMI++

We first mention the main steps of HeMI++ as follows and then explain each of them in detail.

**BEGIN**

Step-1: Normalization

**DO:**  $k=1$  to  $m$  /\*  $m$  is the user defined number of streams \*/

Step-2: Population Initialization

**END**

Step-3: Selection of Sensible Properties

**DO:**  $j=1$  to  $G$  /\*  $G$  is the user defined number of intervals\*/

**DO:**  $k=1$  to  $m$  /\*  $m$  is the user defined number of streams \*/

**DO:**  $t=1$  to  $I$  /\*  $I=10$ ;  $I$  is the number of iterations \*/

Step-4: Noise-Based Selection

Step-5: Crossover Operation

Step-6: Twin Removal

Step-7: Three Steps Mutation Operation

Step-8: Health Improvement Operation

Step-9: Cleansing Operation

Step-10: Cloning Operation

Step-11: The Elitist Operation

**END**

**END**

Step-12: Neighbour Information Sharing

**END**

Step-13: Global Best Selection

**END**

a. *Component 1: Normalization*

HeMI++ first takes a data set  $D$  as input and then normalizes each attribute of the data set  $D$  in order to consider each attribute equally regardless of their domain size. This step is the same as HeMI [7].

b. *Component 2: Multiple Stream*

HeMI++ uses the multiple stream approach of HeMI in order to take the advantage of using a big population through multiple streams where each stream contains relatively small number of chromosomes. It can process each stream separately in parallel in order to reduce the time complexity. It generates the chromosomes for each stream separately through the population initialization. Various components such as noise-based selection, crossover and mutation are applied on each stream separately.

c. *Component 3: Population Initialization*

HeMI++ generates the initial population of  $|P|$  chromosomes,  $|P|/2$  from the *deterministic phase* and  $|P|/2$  from the *random phase*. The value of  $|P|$  in HeMI++ is set to 20. This component is same as HeMI [7].

d. *Component 4: Selection of Sensible Properties*

HeMI++ selects  $|P|$  top chromosomes from the generated initial chromosomes based on their fitness (DB value). The Davis Bouldin Index [26] is biased towards a low number of clusters and a low number of records in a cluster [8]. Therefore, HeMI++ finds the necessary properties of a sensible clustering solution. The properties of a sensible clustering solution are then used in each generation in order to ensure that chromosomes in a population do not contradict the properties.

In the initial population, HeMI++ produces  $9 \times 4 = 360$  chromosomes as it has 4 streams. Each stream generates 90 chromosomes. HeMI++ finds the minimum number of records in a cluster for each of the 360 chromosomes. It then sorts these number in descending order and calculates the median of these numbers. The median value is then used as a property (of a sensible clustering solution) relating to the minimum number of records in a cluster. HeMI++ similarly finds the minimum and maximum number of clusters in a clustering solution, based on the 360 chromosomes. These values are then used in the cleansing operation in order to identify a sensible clustering solution.

Note that CSClust [8] uses a similar component. However, there are some significant differences, First, CSClust does not use multiple streams and hence it finds the properties based on 90 chromosomes of its single stream. Second, in order to find the minimum number of records in a cluster CSClust identifies the best 20 chromosomes according to their DB Index values and then picks the minimum number of records in a cluster out of all clusters in these 20 chromosomes. Since the best 20 chromosomes are selected based on their DB Index values, CSClust also suffers

from the drawbacks of DB Index in identifying the properties of a sensible clustering solution.

e. *Component 5: Noise Based Selection*

The chromosomes of two generations are compared in order to select the chromosomes for the consequent genetic operations. HeMI also uses this component.

f. *Component 6: Crossover Operation*

All chromosomes in a population participate in crossover pair by pair. The best chromosome (available in the current population) is selected as the 1<sup>st</sup> chromosome of the pair and the 2<sup>nd</sup> chromosome of the pair is selected probabilistically using the roulette wheel technique [6, 9]. The probability of a chromosome  $P_j$  is computed as  $T_j = (f_j / \sum_{i=1}^{|P|} f_i)$ . Here,  $f_j$  is the fitness of the chromosome  $P_j$  and  $|P|$  is the size of the current population

There are many approaches for crossover such as single-point, multi-point, arithmetic and path-based crossover [2, 4, 6, 20]. However, many existing techniques [2, 6, 7] use a single-point crossover, and it is commonly used in genetic algorithms. Moreover, Peng et al. [21] suggest that a single-point crossover performs better than a multi-point crossover. Therefore, HeMI++ uses a single-point crossover where each chromosome of a pair is randomly divided into two segments, where some genes of the chromosome fall in one segment and other genes fall in the other segment. A segment of the first chromosome is then swapped with a segment of the second chromosome. Thus, two offspring chromosomes are generated from two-parent chromosomes.

g. *Component 7: Twin Removal*

We use the twin removal approach [2] to change/remove the identical genes. If a chromosome has two identical genes and, if the length of the chromosome is more than two, then HeMI++ deletes one of the two identical genes. If the number of genes of a chromosome is two and both genes are identical, HeMI++ then randomly changes an attribute value of a gene to ensure that there are no identical genes.

h. *Component 8: Three Steps Mutation Operation*

The mutation operation of the proposed technique changes each chromosome using three operations: division, absorption and a random change. This component is the same as HeMI [7].

i. *Component 9: Health Improvement Operation*

This component aims to continuously improve the health of chromosomes within a population in order to ensure the presence of healthy (high-quality) chromosomes in each generation. This component is the same as HeMI [7].

j. *Component 10: Cleansing Operation*

The aim of this component is to identify the chromosomes in a population with sensible and non-sensible solutions. This component is the same as CSClust [8].

*k. Component 11: Cloning Operation*

The cloning operation replaces the sick chromosomes found in the cleansing operation. This component is the same as CSClust [8].

*l. Component 12: The Elitist Operation*

The elitist operation carries the best chromosome throughout the generations and pass it to the next generation in order to improve the quality of the population [2-4, 6, 20]. This component is same as HeMI [7].

*m. Component 13: Neighbor Information Sharing*

HeMI++ uses the neighbor information sharing approach of HeMI [7] in order to share/exchange the best chromosome among neighboring streams at a regular interval such as at every 10<sup>th</sup> iteration. This component is the same as HeMI [7].

*n. Component 14: Global Best Selection*

HeMI++ uses this component in order to find the global best chromosome among multiple streams. This component is the same as HeMI [7].

*B. The HeMI++ Algorithm*

We now present the HeMI++ algorithm, whose main steps is shown in Section 2 (A). HeMI++ first takes a data set  $D$  as an input and normalizes all attributes separately. It then takes the user defined number of multiple streams as HeMI. The default number of multiple streams in HeMI++ is set to 4.

HeMI++ then produces initial chromosomes for each stream separately through the Population Initialization. It then applies the Selection of Sensible Properties like CSClust to find the necessary properties of a sensible clustering solution. HeMI++ applies the noise-based selection operation like HeMI does.

HeMI++ then sequentially applies the Crossover, Twin Removal, Mutation and Health Improvement operation. HeMI++ applies the cleansing and cloning operation in order to increase the chance that all chromosomes in a population do not contradict with the properties of a sensible solution.

It then performs the Elitist operation to find the best chromosome. In order to take the advantage of multiple streams, HeMI++ then applies the neighbor information sharing component like HeMI does at regular intervals. In this study, the default value of the interval is 10 iterations. At the end of all iterations, HeMI++ applies the Global Best Selection operation like HMI does to find the final clustering solution.

III. EXPERIMENTAL RESULTS AND DISCUSSION

*A. The Data Sets and the Evaluation Criteria*

We empirically compare our proposed technique called HeMI++ with six existing techniques namely K-means [5], K-means ++ [6], AGCUK [3], GAGR [4], GenClust [2] and HeMI [7] on a brain data set (CHB-MIT data set) [24, 25]. HeMI++ is also compared with these existing techniques on 20 natural data sets that are available from the UCI machine learning repository [22]. HeMI++ is compared with these techniques because they are recent, and better than many other techniques as shown in the literature [2-4,7,8]. Detailed information about the data sets is presented in Table 1.

TABLE 1: A brief description of the data sets

Data set	No. of Records
Hepatitis (HT)	155
Glass Identification (GI)	214
Statlog Heart (STH)	270
Vertebral Column (VC)	310
Ecoli (EC)	336
Leaf (LF)	340
Liver Disorder (LD)	345
Credit Approval (CA)	690
Breast Cancer Wisconsin Original (WBC)	699
Blood Transfusion (BT)	748
Pima Indian Diabetes (PID)	768
Statlog Vehicle Silhouettes (SV)	846
Bank Note Authentication (BN)	1,372
Contraceptive Method Choice (CMC)	1,473
Yeast (YT)	1,484
Image Segmentation (IS)	2,310
Wine Quality (WQ)	4,898
Page Blocks Classification (PBC)	5,473
MAGIC Gamma Telescope (MGT)	19,020
Chess (King-Rook vs. King) (CKRK)	28,056

*B. The Parameters used in the Experiments*

For the experimentation of AGCUK [3], GAGR [4] GenClust [2], HeMI [7] and HeMI++ the population size is set to be 20 and the number of iterations/generations is set to be 50. In order to ensure a fair comparison among the techniques we maintain this consistency.

In the experiments, the number of iterations of K-means, K-means++, and the number of iterations of K-means in GenClust set to be 50. The number of clusters  $k$  in GAGR, K-means and K-means++ is generated randomly. The threshold value for K-means is defined as 0.005.

The  $r_{max}$  and  $r_{min}$  values in AGCUK and HeMI are set to 1 and 0 respectively. For the cluster evaluation technique Tree Index [9,10], we need to build a decision tree from a data set where records are labelled on the clustering result that is being evaluated. While building the decision tree we need to assign a minimum number of records for each leaf.



In this study we assign 1% of records of a data set, as long as it stays within the range between 2 to 15. If 1% of records is less than 2 then we assign 2, and if 1% of records is more than 15 then we assign 15. On each data set, we run HeMI++ 20 times and we present the average clustering results of each technique.

### C. Brain Data Set Pre-processing

We prepared the CHB-MIT Scalp EEG data set [2,25] which contains EEG recordings of 22 epileptic patients from different age groups.

Most of the cases 23 channels were used, only in some cases 24 or 26 channel were used. We divided the data in epochs of 10 seconds for each channel. We then calculated the Maximum (Max), Minimum (Min), Mean, Standard deviation (Std), Kurtosis, Skewness, Entropy, Line length and Energy for each epoch. Therefore, from each channel of one-hour data we get 360 records containing nine attributes: Max, Min, Mean, Std, Kurtosis, Skewness, Entropy, Line Length and Energy.

For the experiments reported in this article, we prepared one-hour data of one patient. This data set has the recordings of 23 channels. Hence, from all 23 channels altogether, we obtain  $360 \times 23 = 8280$  records. In this data set, the patient experienced a seizure for around 40 seconds (from the 2996<sup>th</sup> second to 3036<sup>th</sup> second). During this period, we have 5 records. These records are considered as seizure records and all other records are considered as non-seizure records. Therefore, from the chb\_01\_03 data set altogether, we get  $23 \times 5 = 115$  seizure records and 8165 non-seizure records.

### D. Evaluation of HeMI++ and other techniques on the MIT-chb01\_03 data set

In this section, we empirically compare HeMI++ with K-means [5], K-means ++ [6], AGCUK [3], GAGR [4], GenClust [2] and HeMI [7] on a brain data set (MIT-chb01\_03) through visual analysis of clustering results. We also compare all the techniques based on Tree Index [9,10] in order to validate the correctness of Tree Index evaluation. In this section, we use three attributes (Max, Min and Std) of the data set in order to plot the records so that we can see the records and their orientations. Such plots also help us to see clustering results and their appropriateness.

TABLE 2. Clustering results of HeMI++ and other techniques on (MIT-chb01\_03) based on Tree Index

Clustering Techniques	Tree Index (lower the better)
HeMI++	<b>0.55</b>
HeMI	$\infty$
GenClust	5.27
GAGR	19.89
AGCUK	18.19
K-means	27.41
K-means++	31.01

Fig.1 shows the clustering result of HeMI on the CHB-MIT Scalp EEG (chb01-03) data set. HeMI generates two clusters but one cluster contains only one record and all other records belong to the other cluster. Clearly, this does not

appear to be a sensible clustering. From Table 2 we can see that according to Tree Index, HeMI receives a poor evaluation result which is  $\infty$ . Therefore, the evaluation made by Tree Index matches with the manual evaluation (the visual analysis of the plotted records).

Fig.2 shows the clustering result of AGCUK where it generates two clusters: seizure and non-seizure. Mainly, the non-seizure records appear in Cluster 1 and a mixture of seizure and non-seizure records are found in Cluster 2. Cluster 1 has 2836 non-seizure records (dots in Fig.2) and 0 seizure records (plus signs in Fig.2), while Cluster 2 has 5389 non-seizure records (triangles in Fig.2) and 55 seizure records (circles in Fig.2). We can clearly see that while the clustering result is more sensible than the clustering result of HeMI (see Fig.1), it is still not a good clustering result.

Fig.3, Fig.4, Fig.5 and Fig.6 show the clustering results of GAGR, GenClust, K-means and K-means++ where GAGR, GenClust, K-means and K-means++ produce 56, 477, 28 and 13 clusters, respectively. Considering that the data set has only two types of records: Seizure and Non-seizure these clustering results with so many clusters also do not seem appropriate. This is also identified by Tree Index evaluation technique as shown in Table 2.

As we can see in Fig.7, HeMI++ produces a sensible clustering solution as it matches with the original orientation of records in the data set. It produces two clusters: Cluster 1 and Cluster 2. Cluster 1 contains 8219 non-seizure records and 38 seizure records, while Cluster 2 contains 6 non-seizure records and 17 seizure records. As a result, HeMI++ also achieves a good evaluation value based on *Tree Index* as shown in Table 2. This re-confirms that Tree Index produces better evaluation value for better clustering solutions.

### E. Experimental Results on All Techniques on 20 Real Life Data Sets based on Tree Index

We now experimentally evaluate the performance of HeMI++ by comparing it with K-means, K-means++, GAGR, AGCUK, GenClust and HeMI on 20 other real-life data sets. For each data set, we run each technique 20 times.

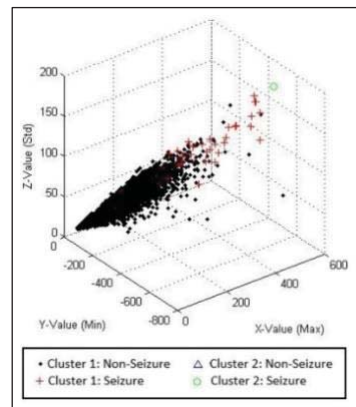


Fig.1. Clustering result of HeMI on the CHB-MIT Scalp EEG (chb01-03) data set

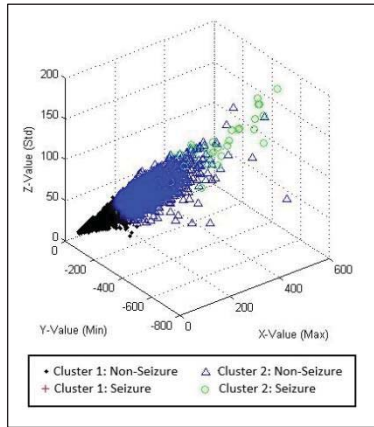


Fig. 2. Clustering result of AGCUK on the CHB-MIT Scalp EEG (chb01-03) data set

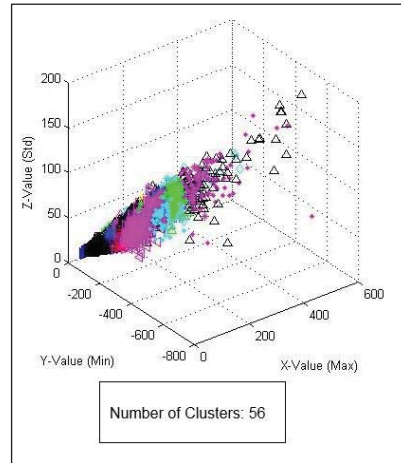


Fig. 3. Clustering result of GAGR on the CHB-MIT Scalp EEG (chb01-03) data set

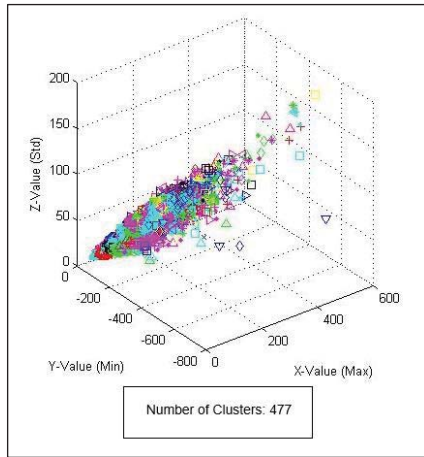


Fig. 4. Clustering result of GenClust on the CHB-MIT Scalp EEG (chb01-03) data set

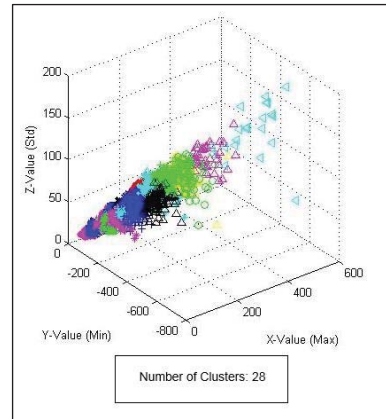


Fig. 5. Clustering result of K-means on the CHB-MIT Scalp EEG (chb01-03) data set

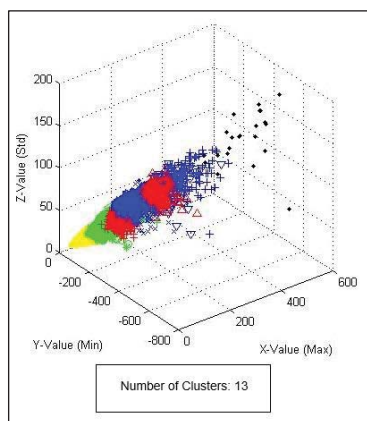


Fig. 6. Clustering result of K-means++ on the CHB-MIT Scalp EEG (chb01-03) data set

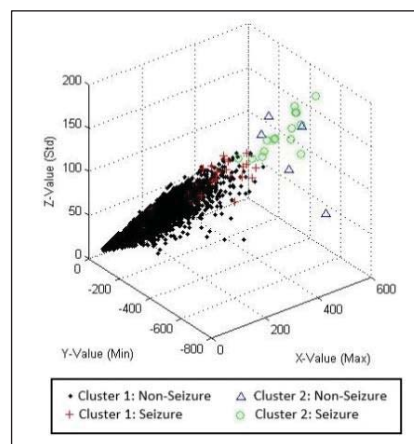


Fig.7. Clustering result of our proposed technique, HeMI++ on the CHB-MIT Scalp EEG (chb01-03) data set

Fig.8 shows the total score of all techniques on 15 numerical data sets based on Tree Index [9,10]. In this scoring system, the technique with the best clustering result gets 7 points and the technique with the worst result get 1 point - for each data set. Fig.8 shows the total scores of a technique over all data sets. The bar graph shows that HeMI++ achieves higher score than all other techniques.

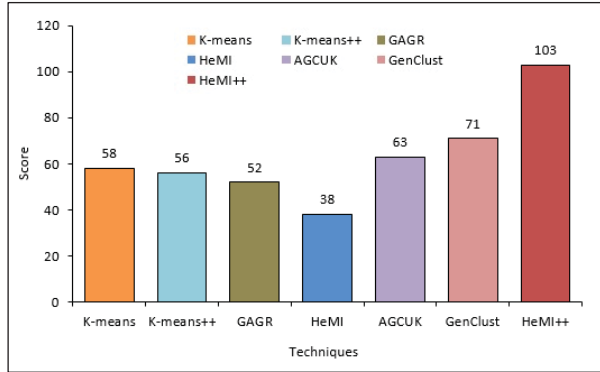


Fig. 8. Scores of the techniques on 15 numerical data sets based on Tree Index

TABLE 3. Clustering results of HeMI ++ and other techniques on 5 categorical data sets based on Tree Index

Data set	GenCslust	HeMI	HeMI++
HT	1.94	0.59	<b>0.46</b>
STH	1.75	$\infty$	<b>1.38</b>
CA	$\infty$	$\infty$	<b>1.57</b>
CMC	<b>0.78</b>	$\infty$	2.51
CKRK	60.39	2.23	<b>1.39</b>

We compare HeMI++ with GenClust and HeMI on 5 categorical data sets (data sets that have only categorical attributes or both the categorical and numerical attributes). For each data set, we ran each technique 20 times and present the average clustering result. Table 3 shows that HeMI++ achieves better results in 4 out of 5 data sets than GenClust. HeMI++ performs better than HeMI in 5 out of 5 categorical data set.

#### F. Statistical Friedman Test

We now carry out statistical Friedman test [23] in order to evaluate the superiority of the results (Silhouette Coefficient) obtained by HeMI++ over the results obtained by the existing techniques including HeMI. We compute the Silhouette Coefficient for each algorithm according to rank-ordering as it is used in the Friedman Test [23]. Among the 7 competing algorithms, the one providing the best Silhouette Coefficient is assigned a Rank of 1, the second best to the Silhouette Coefficient receives a Rank of 2 and so on (hence, the lower the average rank the better result). The result of ties is resolved by assigning the average of the sequential Silhouette Coefficient ranks they would have received. The Silhouette Coefficient Rank of each competing algorithm for each data set is presented within parentheses. The bottom row of Table 4 presents (within parentheses) the average of Silhouette Coefficient Rank (in short, Rank) of each competing algorithm from all data sets considered.

From Table 4, we can see that K-means never provides the best Silhouette Coefficient (Rank: 4.26), K-means++ also for no data sets (Rank: 4.40), GAGR as well for no data sets (Rank: 4.60), AGCUK for no data sets (Rank: 4.20), GenClust for 2 data sets (Rank: 3.50), HeMI for no data sets (Rank: 5.90) whereas HeMI++ achieves the best Silhouette

TABLE 4: Silhouette Coefficient rank of the techniques based on Friedman Test [23]

Data set	Tree Index (lower the better)						
	K-means	K-means++	GAGR	AGCUK	GenClust	HeMI	HeMI++
GI	2.11 (4)	1.87 (3)	3.47 (6)	0.92 (2)	2.47 (5)	$\infty$ (7)	<b>0.31 (1)</b>
VC	4.94 (4)	4.11 (3)	5.37 (5)	$\infty$ (6.5)	3.55 (2)	$\infty$ (6.5)	<b>1.53 (1)</b>
EC	$\infty$ (5)	$\infty$ (5)	6.12 (2)	$\infty$ (5)	$\infty$ (5)	$\infty$ (5)	<b>2.94 (1)</b>
LF	2.64 (3)	3.05 (4)	3.53 (5)	1.32 (2)	3.71 (6)	$\infty$ (7)	<b>0.95 (1)</b>
LD	6.31 (6)	4.85 (5)	7.52 (7)	1.21 (3)	4.28 (4)	0.46 (2)	<b>0.24 (1)</b>
WBC	5.92 (5)	7.07 (6)	8.24 (7)	3.21 (3)	5.58 (4)	2.38 (2)	<b>1.28 (1)</b>
BT	5.81 (4)	5.73 (3)	0.47 (2)	$\infty$ (6)	$\infty$ (6)	$\infty$ (6)	<b>0.27 (1)</b>
PID	13.40 (4)	14.19 (5)	6.20 (3)	$\infty$ (6.5)	<b>3.72 (1)</b>	$\infty$ (6.5)	6.19 (2)
SV	5.18 (6)	3.25 (4)	4.46 (5)	1.2 (2)	3.05 (3)	$\infty$ (7)	<b>0.00 (1)</b>
BN	4.25 (4)	5.59 (6)	4.64 (5)	1.89 (2)	2.51 (3)	$\infty$ (7)	<b>0.77 (1)</b>
YT	13.78 (4)	12.98 (3)	$\infty$ (6)	$\infty$ (6)	4.87 (2)	$\infty$ (6)	<b>2.44 (1)</b>
IS	3.12 (4)	2.48 (3)	5.19 (5)	2.11 (2)	$\infty$ (6.5)	$\infty$ (6.5)	<b>1.53 (1)</b>
WQ	32.64 (4)	47.09 (5)	15.37 (3)	$\infty$ (6.5)	<b>7.98 (1)</b>	$\infty$ (6.5)	13.26 (2)
PBC	13.15 (4)	14.18 (5)	10.21 (3)	$\infty$ (6.5)	4.77 (2)	$\infty$ (6.5)	<b>0.44 (1)</b>
MGT	62.06 (3)	128.61 (6)	100.09 (5)	72.92 (4)	30.67 (2)	$\infty$ (7)	<b>18.89 (1)</b>
<b>Average rank</b>	(4.26)	(4.40)	(4.60)	(4.20)	(3.50)	(5.90)	<b>(1.13)</b>

Coefficient in 13 out of 15 data sets (Rank 1.13). We now conduct a statistical significance test [23] in order to assess the superiority of HeMI++ over the existing techniques. The Friedman [23] test is a non-parametric test used to compare multiple algorithms on multiple data sets. For our instance of the Friedman test, the null hypothesis is that all algorithms are equivalent. If the null hypothesis is rejected, we can proceed with a post-hoc test such as the Bonferroni-Dunn test [23]. The Friedman statistics is distributed according to  $X_F^2$  with  $(k - 1)$  degrees of freedom when  $k$  (the number of competing algorithms) and  $N$  (the number of data sets) are big enough (as a rule of a thumb,  $k > 5$  and  $N > 10$ ) [62]. Iman and Davenport [64] demonstrated that Friedman's  $X_F^2$  is undesirably conservative and derived a better statistic  $F_F = \frac{(N-1)X_F^2}{(k-1)-X_F^2}$ . With 7 algorithms and 15 data sets, the value of  $F_F$  is calculated to be 11.64. With  $\alpha = 0.05$  the critical value of  $F_F$  is calculated to be 2.13.

We can see that the critical value remains lower than the pair wise differences of ranks between the control clustering algorithm (HeMI++) and all other contending algorithms (K-means vs HeMI++: 3.13, K-means++ vs HeMI++: 3.26, GAGR vs HeMI++: 3.46, AGCUK vs HeMI++: 3.06, GenClust vs HeMI++: 2.36 and HeMI vs HeMI++: 4.76) indicating that HeMI++ performs better (in terms of Silhouette Coefficient) than all other algorithms on 15 real-life data sets.

#### IV. CONCLUSION

In this paper, we propose a new clustering technique HeMI++ that first learns important properties of sensible clustering solutions and then applies this information in producing its clustering solutions. When we apply HeMI++ on a brain data set we find that the proposed clustering technique overcomes the existing problem and produces sensible clustering solutions.

We empirically compared our proposed clustering technique (HeMI++) with six existing techniques on 20 publicly available data sets in terms of our Tree Index evaluation technique. We find that HeMI++ achieves the best clustering solutions in 17 out of 20 data sets. Moreover, we graphically visualise the clustering results of HeMI++ on a brain data set and find the results to be more sensible than others.

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