Language Inference with Multi-head Automata through Reinforcement Learning

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Abstract—The purpose of this paper is to use reinforcement learning to model learning agents which can recognize formal languages. Agents are modeled as simple multi-head automaton, a new model of finite automaton that uses multiple heads, and six different languages are formulated as reinforcement learning problems. Two different algorithms are used for optimization. First algorithm is Q-learning which trains gated recurrent units to learn optimal policies. The second one is genetic algorithm which searches for the optimal solution by using evolution-inspired operations. The results show that genetic algorithm performs better than Q-learning algorithm in general but Q-learning algorithm finds solutions faster for regular languages.

Index Terms—finite automata, reinforcement learning, neural network, Q-learning, genetic algorithm

I. INTRODUCTION

Grammatical inference is the process of learning a formal language from a set of labeled examples. It has various applications in the fields of pattern recognition, natural language processing, and computational biology. Its origins date back to the seminal work of Gold in 1960s [1]. Since then, it has been investigated by many researchers including Fu [2], Angluine and Smith [3], Miclet [4].

Considering the different approaches developed for grammatical inference, there has been a great interest in learning languages using recurrent neural networks (RNN). Some early examples include works of Elman [5] and Cleeremans et al. [6] where first order RNNs are trained for regular language recognition. The problem is formulated as sequence prediction task, where the model is presented a single input symbol at each time step and predicts the next symbol. Following the work of Elman and Cleeremans et al., Giles et al. use second order RNNs to learn and extract finite automata for regular languages [7]. Challenging harder languages, Das et al. [8] proposed an RNN model with an external stack to learn context-free languages.

An important line of research was opened by the study of long short-term memory (LSTM) [9] networks in language recognition. Gers et al. [10] showed that LSTM networks can learn context-free and context-sensitive languages such as $a^n b^n$ and $a^n b^n c^n$. In 2018, Weiss et al. [11] showed that LSTM is equivalent to a variant of multilcounter automata [12] and hence perform unbounded counting while recognizing languages like $a^n b^n c^n$ whereas Gated Recurrent Units (GRU) [13] can not, when worked under finite precision regime. Another related work is due to Zaremba et al. [15] where the task is not to learn languages, but simple algorithms which can be carried on by a finite automaton working as a transducer and they use both supervised and reinforcement learning while training GRU and LSTM networks to learn finite automata accomplishing the task.


In this paper, we introduce a new finite automaton model with multiple heads, namely simple multi-head automaton (SMA) and show that intelligent agents modeled as SMA can learn formal languages. The language recognition task is not defined as sequence prediction task as opposed to most of the studies from the literature but the automaton makes the decision of acceptance or rejection as a result of a sequential processing. Accordingly, we use reinforcement learning instead of supervised learning, expanding the previous work on the subject.

Each language is formulated as an environment where agents can act on. At each timestep, an agent receives observation from the environment and it performs an action which either moves one of the heads on the tape or terminates the environment by accepting or rejecting the input string according to its policy. After each action, the agent receives a reward and maximizing this reward leads to the correct and efficient decision on the input string.

Two different algorithms are implemented to optimize the policy of the agents while finding optimal SMA for various languages. The first algorithm is Q-learning, where the policy of the agents are represented with GRUs and optimized by storing an experience buffer which is filled upon interacting with the environment. The second algorithm is genetic algo-

Note that RNNs with infinite precision are Turing complete in theory [14].
rhythm, which does not improve the policy iteratively but instead tries to improve the whole population of agents by evaluating the fitness of each agent and creating new individuals from the best agents with the hope of creating a better generation.

To obtain results about the performance of each algorithm, 6 different languages are tested: 2 regular, 2 context-free and 2 non-context-free languages. Both the agents trained by Q-learning and genetic algorithm accomplished to recognize the regular languages 100% correctly, but the agents trained with Q-learning achieved the results in a shorter time. For the other languages, genetic algorithm showed significantly better performance than Q-learning. Our results suggest that genetic algorithm deserves more attention in the area of grammatical inference.

In Section II, we define our new multi-head automaton model. Section III describes the environment design and how an agent interacts with it. Section IV and V contain information about the insights of Q-learning and genetic algorithm and further details about implementation. We present the results in Section VI and conclude with Section VII.

II. SIMPLE MULTI-HEAD FINITE AUTOMATA

As the main purpose of this research is to model finite automata as learning agents for solving decision problems, a new model of multi-head finite automata is introduced with the motivation of reducing the parameter count that is required to be optimized during the learning process.

A simple multi-head automaton (SMA) is a deterministic finite automaton that uses multiple heads.

Formally, a two-way simple k-head automaton (2SMA(k)) is a 9-tuple \((Q, q_0, F, \Sigma, \$, \#, \delta, k, H)\) where

- \(Q\) is the set of states
- \(q_0 \in Q\) is the initial state
- \(F \subseteq Q\) is the set of accept states
- \(\Sigma\) is the input alphabet.
- \(\delta\) is transition function which maps \(Q \times \tilde{\Sigma}\) into \(Q\)
- \(k\) is the number of heads
- \(H\) is the head assignment function which maps \(Q\) into \(\{\leftarrow, \circ, \rightarrow\} \times \{\text{head}_i | 0 \leq i < k\}\).

A machine is two-way if the tape head can move right (\(\rightarrow\)), left (\(\leftarrow\)) and stay put (\(\circ\)). By restricting the head movements to the set \(\{\circ, \circ\}\), we obtain a one-way simple k-head automaton (1SMA(k)).

SMA uses a single finite input tape and the square with index 1 corresponds to the first symbol of the input string. Let \(n\) denote the length of the input string. Then, the index 0 contains the start-marker $ and the index \((n + 1)\) contains the end-marker #. Note that when the input string is empty, the index of the end-marker is 1.

Initially, all heads start from the square with index 1 and the computation starts from the initial state. At each state, first the head and the direction that are assigned to the state are determined by the head assignment function \(H\). After that, the head is moved 1 step in the assigned direction (no movement if \(\circ\) is assigned) and then the symbol which the head is on is read. Note that the movement occurs before reading. Also, moving beyond start and end-markers is not allowed.

After reading the symbol, SMA performs a transition using \(\delta\) and enters into a new state. If there are no available transitions, the machine halts. If the machine halts in an accept state, the input string is accepted, and rejected otherwise. An SMA is said to recognize a language \(L\) if it accepts all and only the members of \(L\).

It is easy to see that 1SMA(1) is an ordinary deterministic finite automaton (DFA) and recognize exactly the class of regular languages. When compared to the classical multi-head finite automata (DFA\((k)\)) in which there are \(k\) heads reading from an input tape simultaneously \([24],[25]\), it turns out that the two models SMA\((k)\) and DFA\((k)\) are equivalent in terms of language recognition power. The proof is omitted here. Note that the language recognition power of multi-head finite automata increase as the number of heads increase both for one-way and two-way models and two-way models outperform one-way models for a constant number of heads \([25]\).

III. REINFORCEMENT LEARNING

In this section, we will discuss how the components of the reinforcement learning algorithm are defined for the task of language recognition by simple multi-head automata.

A. Environment & Agent

Let’s start by describing the environment and the agent. The agent is a simple multi-head automaton. It can be one-way or two-way depending on the setting.

1) Initial State: As it is mentioned while defining SMA, there is a finite input tape where the first square contains the start-marker and the last square contains end-marker. When the environment is reset, all heads of the SMA will be moved to square 1, which corresponds to the first symbol of the input string. According to the agent’s actions, these heads will change their positions on the tape.

2) Observation: The transition function of an SMA dictates that only a single symbol can be read by a single head at a time. Note that the current state determines which head will be active and reading. Furthermore, a desired property for the observation is that the history of the observations should give all necessary information about the current state of the environment. Thus, the observation contains only a single input symbol, index of the head by which the symbol is read and the direction in which the head moves.

3) Processing the Action: After receiving the observation, the agent will decide on its action. If the agent wants to terminate, which corresponds to the case where there is no valid transition in the current state, the agent can accept and terminate or reject and terminate. If it decides to continue, then it has to determine which head to move and its direction. Therefore, there are \((d \cdot h)\) possible head actions, where \(d\) is the number of directions and \(h\) is the number of heads.
4) Termination & Reward: Theoretically, an SMA may never halt. Due to practical reasons, we put a limit on the maximum number of actions $N$ that the agent can perform during each episode. We set $N$ as $(2 \cdot M + 1) \cdot k + 1$ where $k$ is the number of heads and $M$ is the maximum length of the input string. This limit allows agent to move all heads to the end-marker and back to the start-marker before making a decision. Note that the maximum length of input strings is also limited because of practical reasons.

The environment is terminated when the number of actions performed by the agent reaches $N$ or if the agent decides to terminate early. After each reset, a new input string is generated and it is determined whether it is a member string or not by a hand-crafted test function. When the environment is terminated, the agent receives a reward of $+1$ if it answers correctly, that is, accepts a member string or rejects a non-member string. It receives a reward of $-1$ if the answer is wrong, and no reward for actions without termination. There are 2 special cases for terminal rewards: If the agent answers wrong without reaching the end-marker, it is encouraged to read the whole input string before terminating to make sure that it has the correct answer and therefore it receives a reward of $-10$. If the agent waits until the very end of the episode to reject a string, it receives only a reward of $0.1$ which discourages the agent from waiting too long if it is sure about the answer.

IV. Q-AGENTS

One way to optimize the policy of an agent is $Q$-learning. The agents trained using $Q$-learning algorithm will be called $Q$-agents. In this section, we will describe the details of the $Q$-learning algorithm.

A. Deep $Q$-Learning

$Q$-value is a measure of how good is it to perform action $a$ in state $q$. The function $Q(q,a)$ is defined as

$$Q(q,a) = R(q,a) + \gamma \cdot V(q_{\text{next}})$$

where $R$ is the immediate reward received by performing the action $a$ in state $q$, $\gamma$ is the discount factor which makes the rewards that are received sooner more favorable and $q_{\text{next}}$ is the next state the agent moves in after performing the action.

According to the Bellman Equation [26], the value $V$ of a state $q$ is simply the maximum $Q$-value the agent can get in a given state by performing any action.

$$V(q) = \max_a(Q(q,a))$$

To learn the optimal $Q$ function, it is possible to use either arrays or a neural network to approximate the function. In deep $Q$-learning, a deep neural network is used to approximate the $Q$ function.

B. GRU vs. LSTM

In order to provide internal memory for $Q$-learning agents, gated recurrent units (GRU) are used in this paper. GRU is a simpler alternative to long short-term memory (LSTM). It is known that LSTM is more successful in language recognition as it can perform unbounded counting [11]. The reason why GRU is preferred over LSTM in this paper is to test a new multi-head automaton model focusing on the effect of multiple heads and ability of moving left. As a recurrent neural network model which can perform counting can easily learn languages like $a^nb^n$ or $a^n b^n c^n$ using a single-head and moving in a single direction, GRUs which cannot perform counting suit better the purpose of this paper.

C. Modeling SMA with Neural Networks

The automata defined in this paper have discrete states. However, a continuous state space is needed to train neural networks using gradient descent method.

In the discrete case, each state can be represented by an integer and a boolean lookup table can be used to determine which states are accepting.

In the continuous case, a state can be represented by a real vector. Thus, the transition function $\delta$ takes as input no longer an integer but a vector and the one-hot encoding of an input symbol, and outputs a vector. Instead of a lookup table for determining the acceptance of a state, a new function $A$ maps the state vector to a 3 dimensional stochastic vector, representing a probability distribution over three types of states:

i. rejecting but not halting,
ii. rejecting and halting,
iii. accepting and halting.

So, the function $A$ randomly samples one of these types according to the probability distribution and assigns it as the type of the input state.

Similarly for the head-movement, a function $M$ maps an input state vector to a $2k$-dimensional and $3k$-dimensional stochastic vector for ISMA($k$) and 2SMA($k$), respectively. Then, the function $M$ randomly samples the action for the head movement and assigns it to the input state.

D. Implementation

As explained in Section III-A, the number of possible actions $A$ for the agent is $2 + (d \cdot k)$, where $d$ is the number of directions and $k$ is the number of heads. Therefore, there is a $Q$-network that takes the current internal state, which is the output of the last recurrent unit, as input. Then, there are fully-connected hidden layers, the layer count and the number of neurons in each layer are hyperparameters. The final layer is the output layer with dimension $A$.

We use two methods to improve the stability and convergence of deep $Q$-networks. First, it is possible to store experiences in a buffer [26]. An experience is a tuple $(s_t, action, reward, s_{t+1}, done)$ where $s_t$ is the observation before performing the action, $s_{t+1}$ is the observation after performing the action and $done$ represents if the environment
is terminated after the action. While training, a batch of experiences is sampled uniformly from this buffer.

The second method is using fixed target network [27]. Q-learning uses the estimation for the next state while updating Q-value of the current state. With this method, the estimation will not be taken from the network which is currently being trained but from a fixed Q-network and the weights of the trained Q-network is copied onto the target network periodically.

During training, an agent plays many episodes to fill up the experience buffer. After the buffer is full, the neural network is optimized using the data in the buffer. At the start of each episode, the input string on the tape is changed. Thus, the experience buffer contains different strings with different lengths, which helps the agent to generalize better.

Moreover, Q-learning agents use ϵ-greedy exploration. That is, with ϵ probability an agent chooses a random action and with (1− ϵ) probability it chooses the best action. This hyperparameter handles the exploration-exploitation trade-off: exploration is for trying different actions to achieve better rewards and exploitation is for using the agent’s current knowledge to maximize the rewards.

V. G-AGENTS

Another approach for policy optimization in a reinforcement learning problem is using genetic algorithm. Agents trained with genetic algorithm will be called G-agents.

A. Genetic Algorithm

Genetic algorithm is a black-box optimization technique which uses operations inspired by biological evolution [28]. A population of individuals is randomly initialized and each individual corresponds to a chromosome which is a chain consisting of genes. There exists a fitness function which takes a chromosome as input and returns its fitness value, that is, the performance measure of the chromosome for the given problem. Genetic algorithm works by improving the initial population at each generation.

In this approach, each SMA is represented with a chromosome and its performance is evaluated with a fitness function. Then, at each iteration a collection of chromosomes is improved by eliminating bad solutions and creating new chromosomes using the good solutions, with the aim of finding the most optimal automaton recognizing the language trained for.

B. Representation of SMA with Chromosome

To apply genetic algorithm, we need to represent an SMA with a string of integers making up a chromosome. The individual integers are called the genes.

Let n be the number of states in the SMA and let |Σ| = m where Σ = Σ ∪ {§, #}. There might be a transition between any pair of two states with any one of the m symbols as its label. For each state, each possible transition is represented with a gene g→ which holds the information about the target state of the transition. The range of each gene is [0, n], where 0 means that there is no transition and the remaining integers are the indices of the states. For each state, m genes are required to represent all possible outgoing transitions from the state for each symbol.

Moreover, head assignment function which assigns the head and the direction for each state is stored with a single gene gk in the range [0, d·k], where d is the number of directions and k is the number of heads. Lastly, for each state a single gene ga in the range [0, 1] is required to store whether it is an accept state or not. As a result, a chromosome is a sequence of genes

\((m \cdot g→) \cdot n + g_k \cdot n + g_a \cdot n\)

where multiply represents duplication and plus represents concatenation.

C. Fitness

Initially, a training set is formed with N strings which are generated randomly by the environment. This training set is used for computing the fitness value of an individual.

Each individual is tested for N different episodes, which contain the input strings on the tape chosen from the training set. For each episode, the total episode reward is stored and the sum of all episode rewards is used as the fitness value.

Similar to Q-learning algorithm, the rewards are multiplied by a discount factor γ to make sooner rewards more favorable.

Moreover, when the best individual in a generation achieves 100% correct prediction rate, a new training set is formed and all fitness values are recomputed so that if there exist some strings that are not accepted even by the best individual, the individual can improve itself further.

VI. RESULTS

A. Languages

During training, agents are taught 6 different languages:

i. \(L_1 = \{0^w1 \mid w \in \{0, 1\}^*\}\)
ii. \(L_2 = \{w \mid w \in \{0, 1\}^* \text{ and length of } w \text{ is even} \}\)
iii. \(L_3 = \{a^n b^n \mid n \geq 0\}\)
iv. \(L_4 = \{w \mid w \in \{0, 1\}^* \text{ and } w \text{ is palindrome} \}\)
v. \(L_5 = \{a^n b^n c^n \mid n \geq 0\}\)
vi. \(L_6 = \{ww \mid w \in \{0, 1\}^*\}\)

Note that \(L_1\) and \(L_2\) are regular and both can be recognized by 1SMA(1). \(L_3\) and \(L_4\) are non-regular but context-free and \(L_5\) and \(L_6\) are non-context-free languages. \(L_3\) can be recognized by a 1SMA(2) but for \(L_4\), 2SMA(2) is needed as the tape head should be able to move to both directions. \(L_5\) is recognized by a 1SMA(2) and \(L_6\) is recognized either by a 1SMA(3) or 2SMA(2) but not with a 1SMA(1).

All languages except \(L_4\) are trained on a 1SMA. \(L_1\) and \(L_2\) are trained with a single head, \(L_1\) with 2 heads and finally \(L_5\) and \(L_6\) are trained with 3 heads. Note that for \(L_5\) an extra head is added to test whether the algorithms can optimize and use less heads.
B. Hyperparameters

The hyperparameters for Q-learning are given below:
- The output size of a recurrent unit is 32.
- The discount factor $\gamma$ is 0.999.
- The Q-network which takes the output of the last recurrent unit as input has 1 hidden layer with 32 neurons that use $\arctan$ as activation function.
- The experience buffer size is 25000.
- $\epsilon$ for exploration is 0.05.

The hyperparameters for genetic algorithm are as follows:
- The population size is 100.
- The state size of SMA is 32.
- The chromosome length $C$ of an individual is $(m + 2) \cdot n$, where $m$ is the number of symbols and $n$ is the number of states.
- The maximum number of mutations is 3 for regular languages, $(C/20)$ for other languages.
- The discount factor $\gamma$ is 0.999.
- The training set size is 1000.

C. Discussion

Fig. 1 shows the performance of different algorithms for different languages. First column is the model name, second column is the average reward, third column is the correct prediction rate and the fourth column is the average episode length. The data is collected by running the algorithms for 10000 episodes, that is, 10000 different input strings. Note that the maximum length of the input strings is set to 20, because of practical reasons mentioned before.

The number in the model name represents the language the agent is taught and the rightmost letter represents the algorithm that the agent uses. $R$ is the random algorithm that performs a random action at each step, $Q$ and $G$ represent the Q-agent and G-agent respectively.

An algorithm is commonly evaluated according to 3 criteria: correctness, memory usage and running time. The solutions found by Q-agent and G-agent can be also evaluated similarly. In the results, correct prediction rate shows the correctness of the solution and the average episode length shows the running time. Note that optimizing the memory usage is not a concern in this paper.

The table in Fig. 2 further supports this result. This table provides statistics about head movement in different situations. First column is the model name which represents the same models as in Fig. 1, next three columns show the usage of each head compared to others and the last three columns show which direction the heads are moved mostly.

1) Random Algorithm: The result of the random algorithm is included in order to better assess the performance of the other two algorithms. A random agent has no knowledge of the environment and it does not change its policy according to the state it is currently in. Any well designed algorithm is expected to perform better than the random algorithm.

As expected, the random agents for all languages performed the worst. Note that the correct prediction rates for random agents are approximately 0.5, which means they made the correct decision for half of the strings. This is expected as with probability 0.5, the input string is chosen from the language whereas with probability 0.5 it is predicted randomly.

2) Regular Languages: For the regular languages $L_1$ and $L_2$, both Q-agent and G-agent achieved 100% correct prediction. For the Q-agent, the average reward is higher and the average episode length is smaller in each case which shows that the Q-agent have learned more efficient solutions for these languages.

Figure 3 and Figure 4 display prediction rates during training for G-agents and Q-agents respectively. Note that during training, the average correct prediction rates for Q-learning algorithm can be lower as the agents perform random
actions with $\epsilon$ probability due to $\epsilon$-greedy exploration.

Prediction rates of genetic algorithm for $L_1$ and $L_2$.

![Graph showing prediction rates for $L_1$ and $L_2$.](image)

Fig. 3. Correct prediction rates of the best individuals in each generation during the training of regular languages with genetic algorithm.

Prediction rates of $Q$-learning algorithm for $L_1$ and $L_2$.

![Graph showing prediction rates for $L_1$ and $L_2$.](image)

Fig. 4. The change of the average correct prediction rates for the regular languages during training with $Q$-learning algorithm.

As the head is allowed to stay or move in both directions while processing the input string, moving the heads efficiently reduces the time to reach the answer. Since $L_1$ and $L_2$ are regular, by definition they can be recognized by a real-time DFA in which the head always moves right. Looking at Figure 2, we see that $Q$-agent always moved the head right for $L_1$ whereas the $G$-agent stayed at the same position for 25% of the steps. This explains how the $Q$-agent can terminate earlier for $L_1$.

Early termination is another factor which reduces the solution time. For instance, in $L_1$ there is no string that starts with a 1, and therefore it is possible to terminate immediately if the automaton reads 1 at the beginning. However, in $L_2$ the automaton has to read all the input string to check whether the length of string is even or not. In fact the results show that the agents took less time to reach the answer for $L_1$. Figure 5 displays the average episode length during training of the $Q$-agents for both languages.

![Graph showing average episode lengths for $L_1$ and $L_2$.](image)

Fig. 5. The change of the average episode lengths for the regular languages during training with $Q$-learning algorithm.

3) Nonregular Languages: Even though $Q$-agent performed better for regular languages, it was not successful for the remaining languages. Nevertheless, for all languages it gained more reward than the random agent and it is possible to say that the agents managed to find sub-optimal solutions. However, this does not necessarily imply higher correct prediction rates. $Q$-agent has higher correct prediction rate than random agent only for $L_3$.

The reward function punishes heavily the agents which answer wrong without reading the whole input string. So, for an agent which can not find the correct answer, it is better to reach the end of the string first before terminating. This is how the $Q$-agents may have gained higher rewards than random agents.

On the other hand, $G$-agents performed significantly better for non-regular languages. For $L_3$ $G$-agent achieved 100% correct prediction rate and for $L_5$ it rarely answers wrong. There is an important detail in Fig. 2 for $L_5G$. Even though there are 3 heads, the second head is not used at all which is expected for an efficient agent as theoretically $L_5$ can be recognized by a 2SMA(2).

Furthermore, there is a critical observation about the input generation algorithm. As discussed earlier, half of the time the input string is generated randomly and half of the time it is chosen from the language, and the maximum length of the generated strings is 20. So, if agents can understand if a string
is randomly-generated or not, then they can easily understand whether it is a member string or not.

There is an important difference between $L_5$, and $L_4$ and $L_6$. In $L_4$ and $L_6$, first half of the string can actually be random and only the second half must obey some format regarding the first half. Therefore, it is possible to say that strings that are in $L_4$ and $L_6$ look more random than $L_5$. For instance, if a string starts with 5 $a$’s and continues with 5 $b$’s, then it already looks like a very organized string, thus an agent may assume the rest of the string will contain 5 $c$’s. So, at that step the agent may guess that the string is in the language and most of the time makes a correct guess.

This can also explain why $G$-agents performed the worst in $L_4$ and $L_6$. As determining if the input string is random or not is harder for these languages, learning these languages is harder for the agents.

VII. CONCLUSION

In this paper, two different algorithms are analyzed and tested for training simple multi-head automata to recognize several decision problems. According to the results, genetic algorithm performed better overall.

A. Q-Learning vs. Genetic

Since Q-learning algorithm uses neural networks and applies gradient descent to optimize weights, it involves calculation with continuous values and calculus. On the other hand, genetic algorithm involves integers and uses evolution-inspired operations for optimization.

Running a neural network is more costly while in genetic algorithm, integer arrays are used for simulating the automata making it faster. Additional cost of the neural networks could be justified with higher correct prediction rates whereas this is not the case. In fact, agents that use neural networks only learned to recognize regular languages. Thus, it is possible to say that the genetic algorithm turned out to be more effective and more efficient.

B. Future Work

In this paper, it is shown that a state of an automaton can be represented with continuous values and the transition function can map a state vector into another. This can also be done for the alphabet. Currently, a head reads a symbol which is a member of the finite set named alphabet. However, a symbol can actually be a real number.

Continuous symbols are not necessarily useful for decision problems but can be useful when there is an output tape. A transducer automaton can write symbols on an output tape [29]. In future work, a new transducer automaton model can be defined which optionally uses continuous states or continuous input/output symbols to learn different algorithms.

Furthermore, as genetic algorithm looks promising, more advanced algorithms for population management and different methods for creating new individuals can be investigated. Also, testing with harder languages which require more than 3 heads and changing the input generation algorithm in a way that it tries to find corner cases for agents which they fail can improve the effectiveness of training and thus help the agents to generalize better.

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