

# AN EFFICIENT INFORMATION EXCHANGE STRATEGY IN A DISTRIBUTED COMPUTING SYSTEM

## *Application to the CARP*

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Abstract: Distributed computation models have been widely used to enhance the performance of traditional evolutionary algorithms, and have been implemented on parallel computers to speed up the computation. In this paper, we introduce a multi-agent model conceived as a conceptual and practical framework for distributed genetic algorithms used both to reduce execution time and get closer to optimal solutions. Instead of using expensive parallel computing facilities, our distributed model is implemented on easily available networked personal computers (PCs). In order to show that the parallel co-evolution of different sub-populations may lead to an efficient search strategy, we design a new information exchange strategy based on different dynamic migration window methods and a selective migration model. To evaluate the proposed approach, different kinds of experiments have been conducted on an extended set of Capacitated Arc Routing Problem(CARP). Obtained results are useful for optimization practitioners and show the efficiency of our approach.

## 1 INTRODUCTION

Genetic Algorithms, a special class of Evolutionary Algorithms (EAs), are proven to be successful in a wide range of applications, especially in cases of optimization. In order to solve more difficult problems, two inherent features of EAs, *premature convergence* and *computation time* must be improved. To overcome the two problems, the idea of parallelizing EAs has been proposed by different researchers, and it has been proven to be a promising method (Cantù-Paz, 2000). Conceptually, the parallelism is to divide a big population in a sequential EA into multiple smaller sub-populations that are distributed to separate processors and can then be evaluated simultaneously. According to the sub-population size, the parallel EAs are categorized into two types: *coarse-grain* and *fine-grain*, and they are usually implemented on distributed memory and massively parallel computers, respectively. All though parallel computers can speed up EAs, they are not easily available and it is very expensive to upgrade their processing power and memory. A promising alternative without expensive hardware facilities is to construct the parallel evolutionary computation (EC) framework on a set of net-

worked personal computers.

To make the parallel EAs more realistic, we propose in this paper a mobile agent-based methodology to support parallelism on networked computers in a flexible and adaptive way. In addition, we design a new information exchange strategy. The idea is that an EA periodically selects some promising individuals from each sub-population and sends them to other sub-populations, according to certain criteria. To evaluate the proposed approach, different kinds of experiments have been conducted on an extended set of Capacitated Arc Routing Problem (CARP) and the obtained results show the promise and efficiency of our approach.

## 2 THE CARP

The Capacitated Arc Routing Problem (CARP) is a vehicle routing problem raised by applications like urban waste collection, snow plowing, sweeping, gritting, etc. It is defined on an undirected network  $G=(V,E)$ , with a set  $V$  of  $n$  nodes and a set  $E$  of  $m$  edges. A fleet of identical vehicles with capacity  $W$  is based at a depot node  $s$ . Each edge  $e$  can be traversed

any number of times, each time with a cost  $c_e$ , and has a non-negative demand  $q_e$ . All costs and demands are integers. The  $\tau$  edges with non-zero demands are called required edges or tasks and require service by a vehicle. The goal is to determine a set of vehicle trips of minimum total cost, such that each trip starts and ends at the depot, each required edge is serviced by one single trip, and the total demand handled by any vehicle does not exceed  $W$ .

Since the CARP is *NP-hard*, large scale instances must be solved in practice using heuristics. Among fast constructive methods, one can cite Path-Scanning (Golden et al., 1983) and Ulusoy's splitting technique (Ulusoy, 1985). Available meta-heuristics are very recent and include tabu search methods (Belenguer and Benavent, 2003; Hertz et al., 2000), guided local search (Beullens et al., 2003) and genetic algorithm (Lacomme et al., 2001). All these heuristics algorithms can be evaluated through lower bounds (Amberg and Voß, 2002).

### 3 AGENT-BASED APPROACH

The DGA-MAS<sup>1</sup> developed in this work uses several components of the genetic algorithm algorithm proposed by (Lacomme et al., 2001) for the CARP. The common parts are described below:

**Solution Encoding:** The network is coded as a symmetric digraph, in which each edge is replaced by two opposite arcs. A chromosome is an ordered list of the  $\tau$  tasks, in which each task may appear as one of two directions. The implicit shortest paths are assumed between successive tasks. The chromosome does not include trip delimiters and can be viewed as a giant trip for an incapacitated vehicle. A procedure *Split* optimally partitions (subject to the sequence) the giant trip into feasible trips. The fitness function of the genetic algorithm (GA) is the total cost of the resulting CARP solution.

**Initialization:** The global population  $P$  of chromosomes is initialized with the solutions of the two CARP heuristics cited in introduction (PS and UH)(Golden et al., 1983; Ulusoy, 1985), completed by random permutations. The distributed genetic algorithm (DGA) forbids clones (identical chromosomes).

**Selection and Crossover:** At each iteration, two parents are selected by a biased roulette wheel (Goldberg, 1989). Three crossovers were defined for the giant trip representation, LOX (Linear Order Crossover), a modified version of the classical order

crossover OX and X1 (crossing in a point).

**Mutation:** Several mutation operators have been proposed for the CARP, such as inversion, insertion, displacement (MOVE), and reciprocal exchange mutation (SWAP). Reciprocal exchange mutation selects two positions at random and swaps the tasks on these positions.

Several researchers are trying to compare the performance of using *coarse-grain* and *fine-grain* models to parallelize genetic algorithms. Some prefer *fine-grain* models but others favor *coarse-grain* ones (Cantù-Paz, 2000). As our goal is to develop a distributed genetic framework without using a powerful connection machine, we choose to implement a *coarse-grain* model on a set of networked PCs. By using the concept of *coarse-grained* parallelization, the population is divided into a few large sub-populations. These sub-populations evolve independently and concurrently on different processors. After a predefined period of time, some selected individuals are exchanged via a migration process.

Our distributed genetic algorithms with multiple sub-populations uses the master-slave (Luque et al., 2005) multi-agent model for the CARP. The inter-connection topology is logically a star, with the master in the center. Our new migration process is based on different dynamic migration window methods (Kim, 2002) and the selective migration model (Eldos, 2006).

In the master-slave multi-agent model, the master agent maintains the lists of partial results that are sent from slaves. At first, the master agent generates the population and divides them into sub-populations. It sends them to slave agents. The slaves execute a conventional genetic algorithm on their sub-population: fitness evaluation, selection, crossover, mutation and periodically return their best partial results to the master agent. Pseudo-code of the conventional genetic algorithm is shown in section 3.1. The subroutine *Migration* is an extension to a general *coarse-grained* model. The master stores the partial results in lists. Then, the master agent searches the lists and selects two slaves that have bad partial results and sends the migration window size to selected slaves. The selected slaves exchange individuals according to the migration window methods. However, in the proposed model, individuals are screened and examined at both the source and the destination to qualify for migration. The source gives or denies a visa based on local qualification criteria and the destination grants or denies a residency based on local qualification criteria. The simplest form of qualification criteria is through the individual's relative fitness. Every individual in a very sub-population is ranked locally;

<sup>1</sup>Distributed Genetic Algorithm using Multi-agent System

an individual qualifies for a visa at the source sub-population if its rank is within a range, typically the middle class. On the destination sub-population, an immigrant is accepted as a new member of the population if its rank is better than a threshold set by that receiving sub-population.

### 3.1 The Algorithm

The Pseudo-code of the algorithm in each slave Agent is described as below:

```

initialize the population, P
while generation < max_generation begin
  evaluate P
  select P1' from P using roulette
    wheel selection
  select parents randomly from P1'
  apply genetic operators to create
    the rest of the new population, P2'
  merge P1' and P2' to P'
  replace P with P'
  if an interval of K generations is reached
    Migration
  end
  generation = generation + 1
end
subroutine Migration
begin
  Pick a random number (1 - pop_size)
  to nominate
    an immigrant X
  If the rank of X is within limits then
    Send X to the Master
    Mark X as "dead" to be killed
  end
  If an immigrant Y is received then
    If the rank of Y exceeds threshold
      Add to the population
      Update Fitness and Ranking
      Pick a random number (1 - pop_size)
        to nominate a victim V
      Discard the victim V
    end
  end
end
end

```

## 4 EXPERIMENTS AND RESULTS

Following our computational experiments and the agent's methodology, we conducted two series of experiments to compare the corresponding performance for genetic computation with and without individual's exchange. The first series examines whether the parallel implementation can improve search quality. The second series of experiments evaluates the performance of using Multi-agent and the individuals exchange strategies in order to exploit the computational

power of multiple machines.

Both the pure Parallel Genetic Algorithm (PGA) and the Distributed Genetic Algorithm (DGA-MAS), including the multi-agent strategies, are implemented on a network of PCs, connected with a 100Mbit/sec Ethernet. In the experiments, we arranged eight networked computers running Suse Linux operating system as a distributed computing environment to support our Multi-agent system.

One computer played the role of "master" and ran the multi-agent platform. Once the platform was activated, the master agent instantiated other agents (slave agents) and sent each one towards a machine in the network. Each machine in this framework had a slave agent to take care of the computation for each sub-population. Also, the master agent allowed activation of the communication phase described in Section 3 for exchanging individuals among sub-populations.

In the experiments, we use three crossover types (LOX, OX, X1) and two mutation types (MOVE, SWAP). Seven values for crossover rate are used ranging from 0.2 to 0.7 in increments of 0.1. Also, seven mutation rates are allowed varying from 0.1 to 0.4 in increments of 0.05. Our results are obtained with small sub-populations of 30 solutions. Clones (identical solutions) are forbidden in each sub-population, to have a better dispersion of solutions and to diminish the risk of premature convergence. The number of generations is fixed to 5000 for all slave agents. The migration interval is 500 generations. Whenever migration occurs, the dynamic migration window size varies at random from 1 to  $\theta$ . The  $\theta$  value is generated at random within 20% of the sub-population size. The threshold value is fixed to the mean fitness of the sub-population.

These tests are done on a standard set of undirected instances in which all edges are required. Table 1 contain 23 instances from (DeArmon, 1981) with 7 to 27 nodes and 11 to 55 edges. All these files can be obtained at <http://www.uv.es/~belengue/carp.html>.

In the Table 1, *Pb* gives the instance number and *N,M* the numbers of nodes and edges. *LBB* is a lower bound from (Belenguer and Benavent, 2003). *TS* is the result of Carpet (Hertz et al., 2000) with the parameter setting yielding the best results on average (the same setting for all instances). *Best* gives the best solution published, generally obtained by Carpet with various parameter settings. *GA* is the solution of GA from (Lacomme et al., 2001). Our results are shown in the pure parallel genetic algorithm (*PGA*) and the distributed genetic algorithm including the Multi-agent strategy (*DGA*) columns.

Table 1: Results of the DGA-MAS on DeArmon's instances vs best known results.

Pb	N	M	LBB	Best	TS	GA	PGA	DGA
1	12	22	316	316	316	316	316	316
2	12	26	339	339	339	339	339	339
3	12	22	275	275	275	275	275	275
4	11	19	287	287	287	287	287	287
5	13	26	377	377	377	377	377	377
6	12	22	298	298	298	298	298	298
7	12	22	325	325	325	325	325	325
8	27	46	344	348	352	350	355	344
9	27	51	303	311	317	303	323	305
10	12	25	275	275	275	275	275	275
11	22	45	395	395	395	395	403	395
12	13	23	448	458	458	458	462	452
13	10	28	536	544	544	540	544	540
14	7	21	100	100	100	100	100	100
15	7	21	58	58	58	58	58	58
16	8	28	127	127	127	127	129	127
17	8	28	91	91	91	91	91	91
18	9	36	164	164	164	164	164	164
19	11	11	55	55	55	55	58	55
20	11	22	121	121	121	121	123	121
21	11	33	156	156	156	156	158	157
22	11	44	200	200	200	200	203	200
23	11	55	233	233	233	235	237	233

## 5 DISCUSSION

We can observe that *DGA-MAS* obtained solutions as good as our *PGA*. Furthermore, within 48% of the solved problems, *DGA-MAS* outperformed our *PGA* implementation of evolutionary system by a mean advantage of 0.98% in term of solution cost. *DGA-MAS* is very efficient: on all instances, it is at least as good as Carpet. On the 23 DeArmon's instances, it outperforms Carpet 4 times, improves 4 best known solutions with one to optimality, and reaches *LBB* 20 times. The average deviation to *LBB* is roughly divided by 3 compared to Carpet and becomes 0.19%. Moreover, the mean speed up factor for the execution times between *DGA-MAS* and *PGA* is approximately 1.7, in spite of overhead communication time spent in *DGA-MAS*. Hence, the mean execution time spent to find a solution using *PGA* and *DGA-MAS* are respectively 40.3 and 24.5 seconds.

## 6 CONCLUSIONS

In this paper, we have proposed *DGA-MAS*, an efficient distributed genetic algorithm which combines

the two advantages of parallelism: the computational power and co-evolution. We implemented an information exchange strategy based on the dynamic migration window methods that control the size and the frequency of migration and the selective migration model for the choice of individuals to migrate. Results confirm the positive impact of using *MAS<sup>2</sup>* strategy in regard to the pure parallel *GA*. They also point out that such strategies are, at a minimum, as good as the best known methods.

In future work, we will improve the performance of our information exchange system by the addition of intelligent modules, thus allowing the study of the exchange semantics of the requests for improving information. We will test also our framework on other *NP-complete* problems such as planning and scheduling problems.

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