

# Total Internal Reflection at Conductive Interfaces: Monolayer Graphene for Terahertz Modulation

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**Abstract**—We have derived the Fresnel reflection coefficients incorporating both total internal reflection (TIR) and a conductive interface. Using this result we show that the reflectance in the TIR regime has a larger dependency on the optical conductivity of the conductive layer than the transmittance in the normal incidence regime. This suggests that a TIR prism with a controllable conductive layer such as back-gated graphene could be used to create an efficient terahertz modulator.

## I. INTRODUCTION

A high performance terahertz (THz) modulator is one solution to speed up terahertz image acquisition rate. Such a modulator needs to be broadband, and ideally possess characteristics that allow the terahertz modulation to be tuned, such as controllable conductivity. Graphene, a cutting-edge 2D material with an atomically thin thickness, shows ultra-high optical conductivity in the terahertz region due to intraband transitions [1]. The optical conductivity of graphene can be tuned by manipulating its Fermi level in active terahertz modulators by applying a back-gate voltage [1, 2]. However, existing designs, that focus on controlling the transmittance of normal incidence illuminated graphene structures are not able to achieve high modulation or a large bandwidth [2].

Here, we investigate non-normal incidence and formulate the equations to describe the total internal reflection (TIR) from a conductive interface such as graphene: we find that for a given optical conductivity, the reflectance can be decreased.

## II. RESULTS

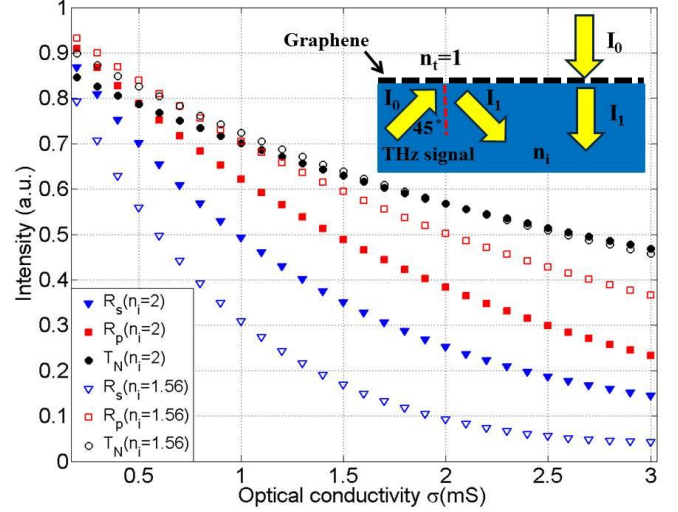
Graphene can be regarded as a thin conductive film in the terahertz region due to its atomic level thickness. The optical conductivity of monolayer graphene at 1 THz can be tuned between 0.2 mS and 1.5 mS by applying a back-gate voltage [1]. By increasing the quality of graphene, the optical conductivity in the terahertz region can be further increased to 2.4 mS [3]. Higher conductivity large-area graphene can hopefully be manufactured in the future. This gives graphene the potential to be used as a material in an active terahertz modulator. Based on the thin conductive film Fresnel equations [4], with an incident angle larger than the critical angle, the TIR reflection coefficients of *s*-polarized and *p*-polarized light can be interpreted as:

$$r_s = \frac{n_i \cos \theta_i - i \cdot \sqrt{n_i^2 \sin^2 \theta_i - n_t^2} - Z_0 \sigma_s}{n_i \cos \theta_i + i \cdot \sqrt{n_i^2 \sin^2 \theta_i - n_t^2} + Z_0 \sigma_s} \quad (1),$$

$$r_p = \frac{i \cdot n_t \sqrt{n_i^2 \sin^2 \theta_i - n_t^2} - n_t^2 \cos \theta_i - i \cdot Z_0 \sigma_s \cos \theta_i \sqrt{n_i^2 \sin^2 \theta_i - n_t^2}}{i \cdot n_t \sqrt{n_i^2 \sin^2 \theta_i - n_t^2} + n_t^2 \cos \theta_i + i \cdot Z_0 \sigma_s \cos \theta_i \sqrt{n_i^2 \sin^2 \theta_i - n_t^2}} \quad (2),$$

where  $n_i$  and  $n_t$  are the refractive indices of incident and transmitted side dielectric material.  $\theta_i$  is the incident angle and  $\sigma_s$  is the optical conductivity of graphene.

In our calculation, two types of substrates are taken into



**Fig. 1.** Terahertz reflectance for TIR at 45° incidence and transmittance at normal incidence as a function of interface conductivity. Two different refractive indices ( $n_i=1.56$  and 2) are considered.  $R_s$  and  $R_p$  represent the reflectance of *s* and *p*-polarized light in TIR.  $T_N$  represents the transmittance at normal incidence. Inset shows the TIR and transmission structure with graphene on the interface.

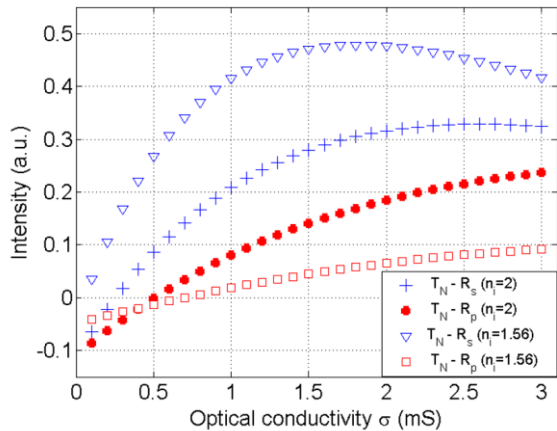
consideration: fused silica and TOPAS (from TOPAS Advanced Polymer Company). The refractive index of fused silica and TOPAS in the THz region are  $\sim 2$  and 1.56.

Using equations (1) and (2), the attenuation of an incident terahertz signal in TIR at 45° incident angle increases along with optical conductivity of graphene (Fig. 1). Using published back-gate controllable optical conductive range of graphene (0.2 to 1.5 mS) [1], the modulation range of *s*-polarized light with TOPAS substrate is from 80% to 17%. If graphene's conductivity is further increased, as reported in [3], the minimum reflectance value reaches 4% at 3 mS. For *s*-polarized light with fused silica substrate, the modulation range is from 89% to 14%. The attenuation of *s*-polarized light is higher than for *p*-polarized light with the same optical conductivity due to the stronger interaction between the in-plane electric field and the graphene. For *p*-polarized light with fused silica substrate, the modulation range is from 93% to 23%. For TOPAS substrate, the modulation range of *p*-polarized light is from 96% to 37%.

Comparing with the transmittance in normal incidence, TIR reflectance shows a higher modulation range. Figure 2 shows the intensity of normal incident transmittance minus TIR reflectance ( $T_N - R$ ). When the optical conductivity is lower than 0.5 mS, the  $T_N$  is lower than TIR reflectance. This is due to the reflection from air-dielectric interface in normal incidence. In TIR, the reflection is lossless when the interface is non-conductive. The attenuation of TIR reflectance over transmittance increases with increasing interface optical conductivity. For *s*-polarized light with TOPAS substrate, the intensity difference of ( $T_N - R$ ) reaches a maximum value of

48% at optical conductivity of 1.8 mS. The intensity difference of  $(T_N - R)$  decreases gradually to 40% when optical conductivity continuously increases. This result could come from the more metallic-like behavior of graphene interface when its optical conductivity goes higher. Under high optical conductivity situation, the reflection from graphene interface takes dominance over absorption. For  $p$  and  $s$ -polarized light under other situations, the advantages of TIR reflectance increase with optical conductivity.

Thus, by controlling the Fermi level of a graphene layer



**Fig 2.** The intensity difference between normal incident transmittance and TIR reflectance. The equations are  $T_N - R_s$  and  $T_N - R_p$ .

with a back-gate voltage it will be possible to modulate a terahertz beam intensity between 80% and 4%, which is nearly a factor of two greater than that possible using a normal transmittance configuration.

### III. SUMMARY

In conclusion, in this paper, we proposed a new THz modulator configuration based on total internal reflection and formulated equations to describe the absorption form a conductive interface. The theoretical results suggest that  $s$ -polarized light with TOPAS substrate has the largest modulation range, which is from 80% to 4%. Comparing with normal incident transmittance, the modulation range is increased two-fold.

### IV. ACKNOWLEDGEMENTS

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